



# **Data Mining and Exploration** **(a quick and *very* superficial intro)**

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AyBi 199b, April 2011

# A Quick Overview Today

- A general intro to data mining
  - What is it, and what for?
- Clustering and classification
  - An example from astronomy: star-galaxy separation
- Exploratory statistics
  - An example from multivariate statistics: Principal Component Analysis (PCA) and multivariate correlations
- Some practical data mining resources
- More in the upcoming lectures

**Note: This is just a very modest start!**

**We posted some web links for you to explore, and go from there.**

# What is Data Mining (DM)?

## (or: KDD = Knowledge Discovery in Databases)

- Many different things, but generally what the name KDD says
  - It includes data discovery, cleaning, and preparation
  - Visualization is a *key* component (and can be very problematic)
  - It often involves a search for patterns, correlations, etc.; and automated and objective classification
  - It includes data modeling and testing of the models
- It depends a lot on the type of data, the study domain (science, commerce, ...), the nature of the problem, etc., etc.
- Generally, DM algorithms are computational embodiments of statistics

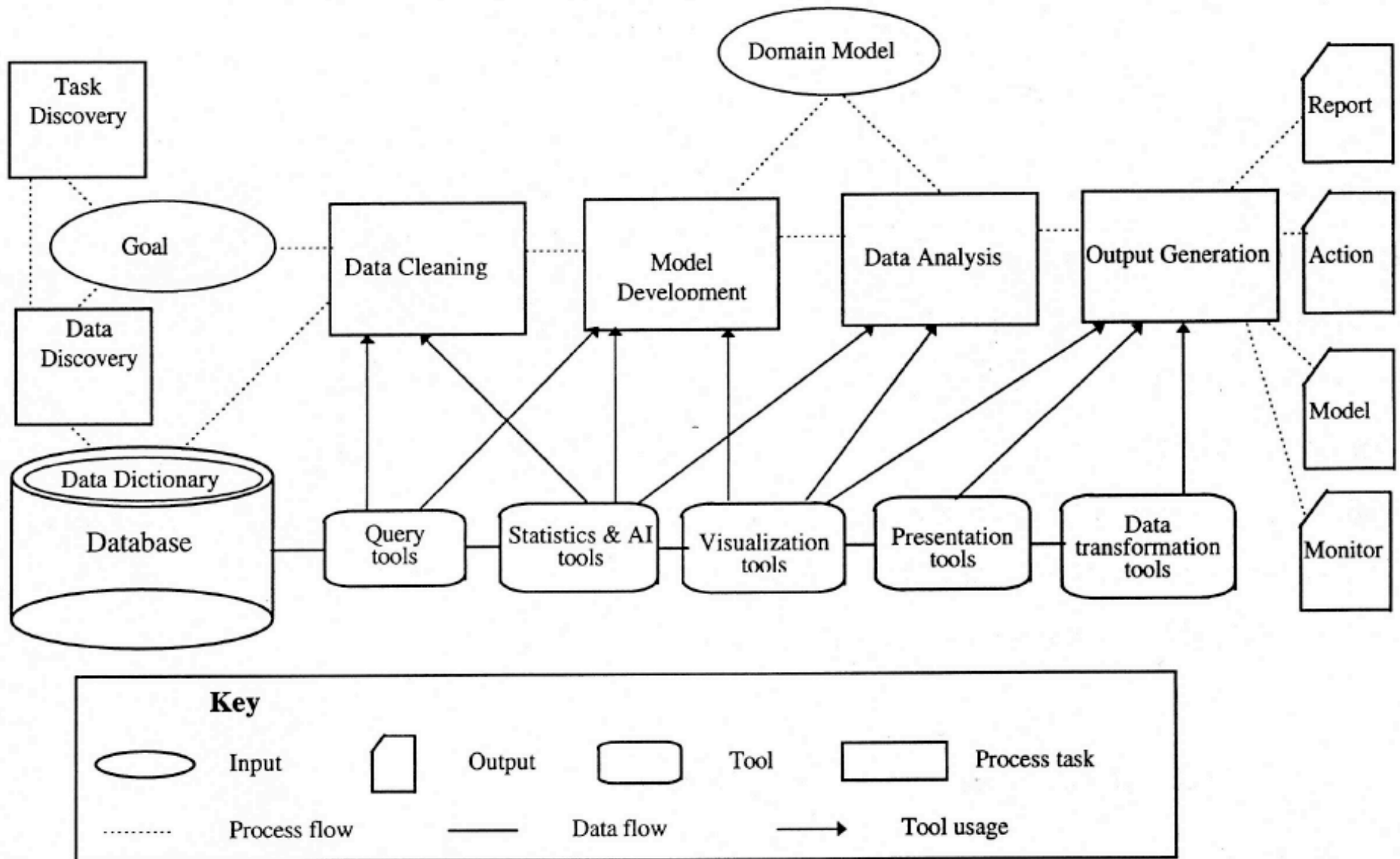
This is a **Huge, HUGE**, field! Lots of literature, lectures, software... And yet, lots of unsolved applied CS research problems

# So what is Data Mining (DM)?

- The job of science is *Knowledge Discovery*; data are incidental to this process, representing the empirical foundations, but not the understanding *per se*
  - A lot of this process is pattern recognition (including discovery of correlations, clustering/classification), discovery of outliers or anomalies, etc.
- DM is *Knowledge Discovery in Databases (KDD)*
- DM is defined as “*an information extraction activity whose goal is to discover hidden facts contained in (large) databases*”
- *Machine Learning* (ML) is the field of Computer Science research that focuses on algorithms that learn from data
- DM is the application of ML algorithms to large databases
  - And these algorithms are generally computational representations of some statistical methods



# A Schematic View of KDD



# Data Mining Methods and Some Examples

Clustering

Classification

Associations

Neural Nets

Decision Trees

Pattern Recognition

Correlation/Trend Analysis

Principal Component Analysis

Independent Component  
Analysis

Regression Analysis

Outlier/Glitch Identification

Visualization

Autonomous Agents

Self-Organizing Maps (SOM)

Link (Affinity Analysis)

Group together similar items and separate dissimilar items in DB

Classify new data items using the known classes & groups

Find unusual co-occurring associations of attribute values among DB items

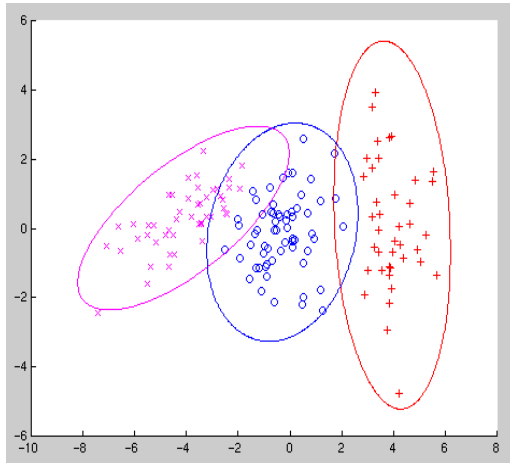
Predict a numeric attribute value

Organize information in the database based on relationships among key data descriptors

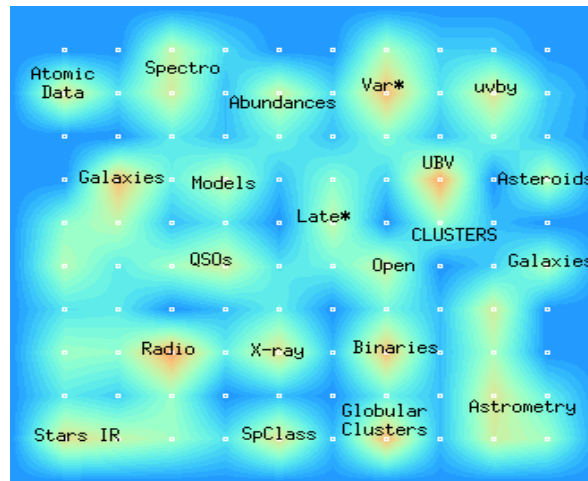
Identify linkages between data items based on features shared in common

# Some Data Mining Techniques Graphically Represented

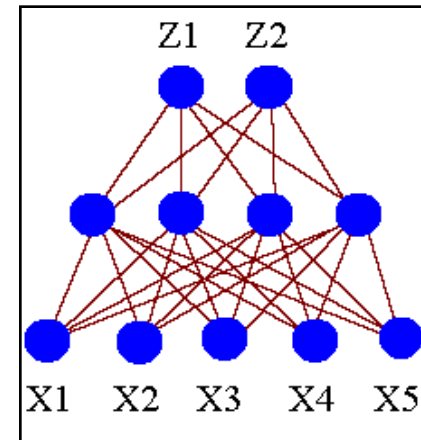
## Clustering



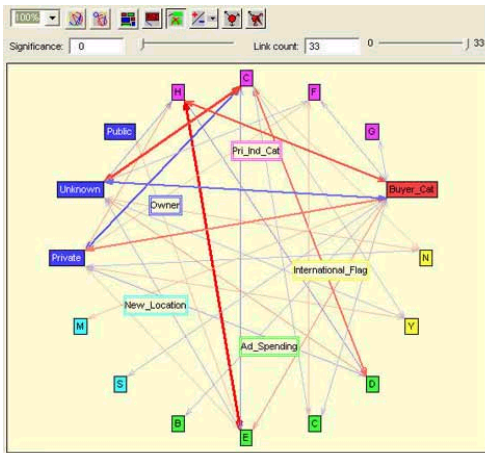
## Self-Organizing Map (SOM)



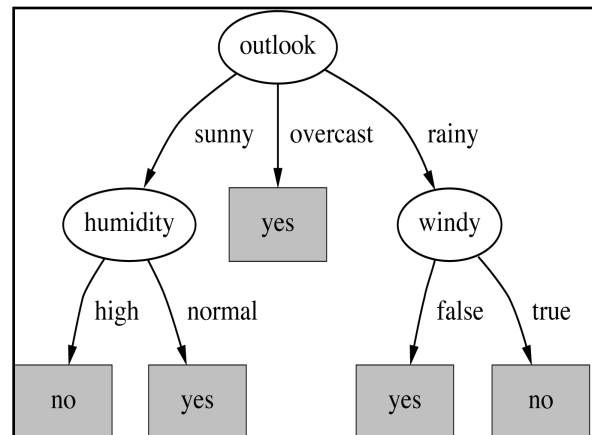
## Neural Network



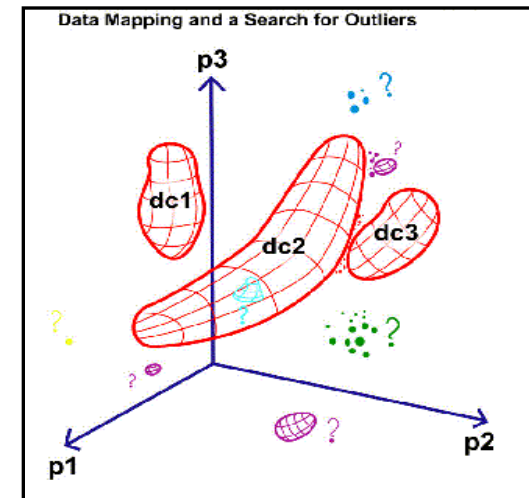
## Link Analysis



## Decision Tree



## Outlier (Anomaly) Detection



**Here we show selected Kirk Borne's slides  
from the NVO Summer School 2008,**

**[http://nvo-twiki.stsci.edu/twiki/bin/view/  
Main/NVOSS2008Sched](http://nvo-twiki.stsci.edu/twiki/bin/view/Main/NVOSS2008Sched)**

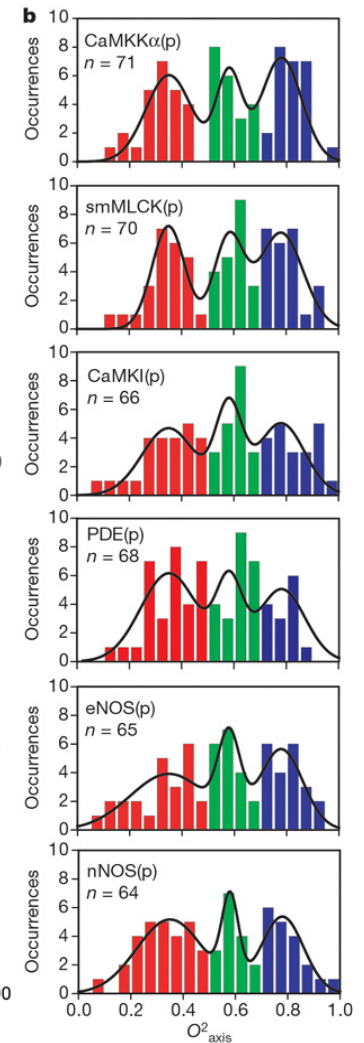
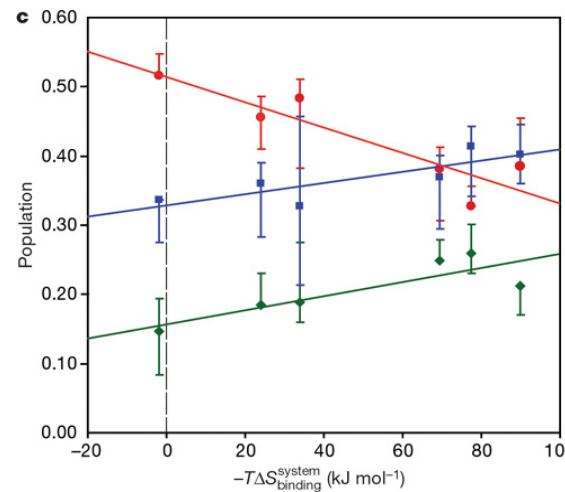
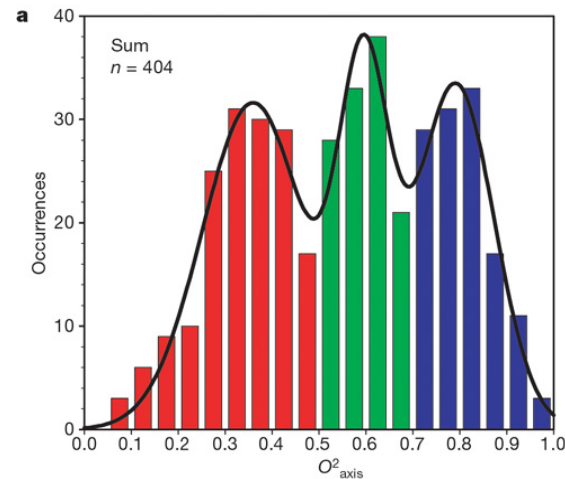


# Clustering and Classification

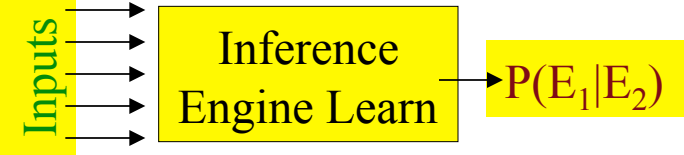
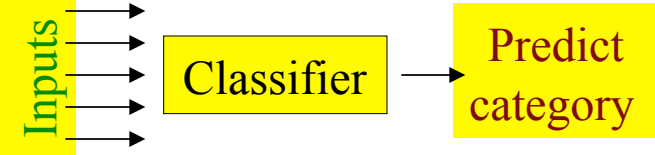
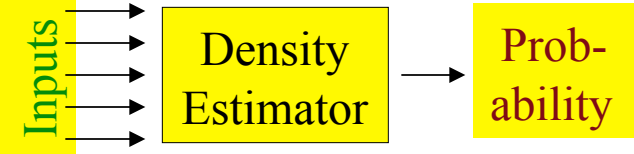

- Answering the questions like:
  - How many statistically distinct kinds of things are there in my data, and which data object belongs to which class?
  - Are there anomalies/outliers? (e.g., extremely rare classes)
  - I know the classes present in the data, but would like to classify efficiently all of my data objects
- Clustering can be:
  1. **Supervised:** a known set of data objects (“ground truth”) can be used to train and test a classifier
    - Examples: Artificial Neural Nets (ANN), Decision Trees (DT)
  2. **Unsupervised:** the class membership (and the number of classes) is not known a priori; the program should find them
    - Examples: Kohonen Nets (SOM), Expectation Maximization (EM), various Bayesian methods...

# Classification ~ Mixture Modeling

- A lot of DM involves automated classification or mixture modeling
  - How many kinds of data objects are there in my data set?
  - Which object belongs to which class with what probability?
- Different classes often follow different correlations
  - Or, correlations may define the classes which follow them
- Classes/clusters are defined by their probability density distributions in a parameter space



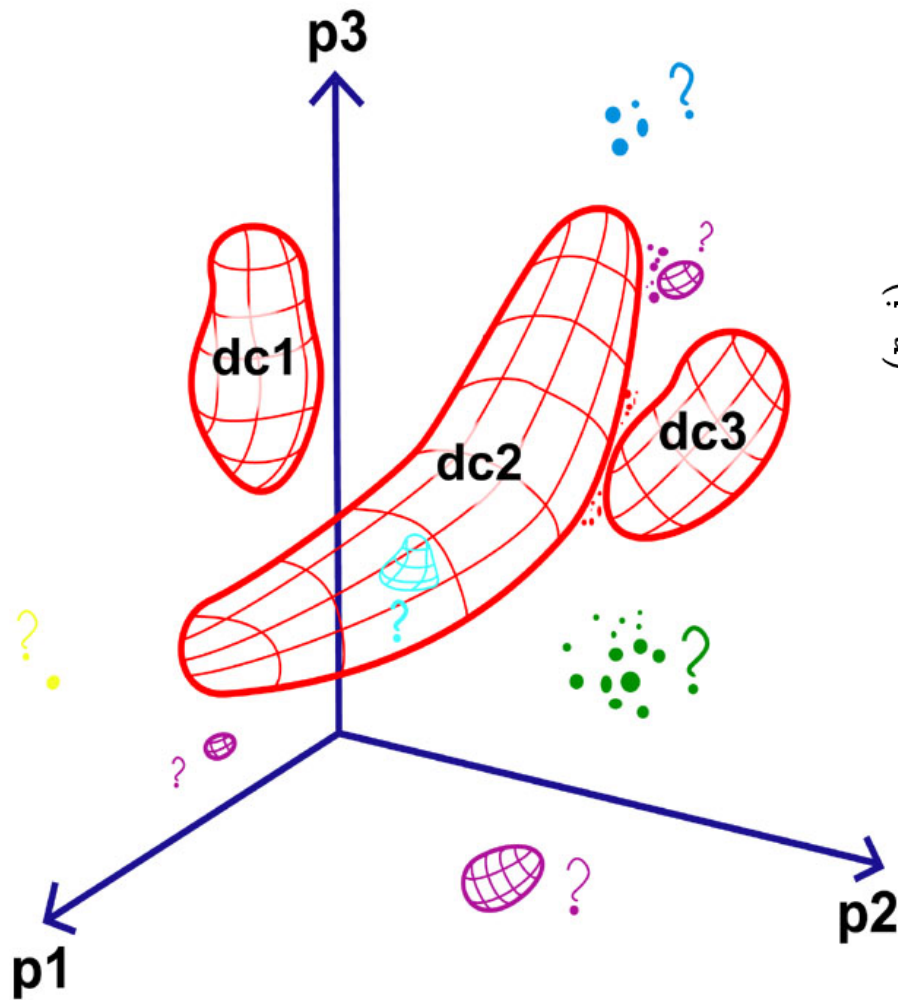
# There are many good tools out there, but you need to choose the right ones for your needs

	Joint DE, Bayes Net Structure Learning
	Dec Tree, Sigmoid Perceptron, Sigmoid N.Net, Gauss/Joint BC, Gauss Naïve BC, N.Neigh, Bayes Net Based BC, Cascade Correlation
	Joint DE, Naïve DE, Gauss/Joint DE, Gauss Naïve DE, Bayes Net Structure Learning, GMMs
	Linear Regression, Polynomial Regression, Perceptron, Neural Net, N.Neigh, Kernel, LWR, RBFs, Robust Regression, Cascade Correlation, Regression Trees, GMDH, Multilinear Interp, MARS

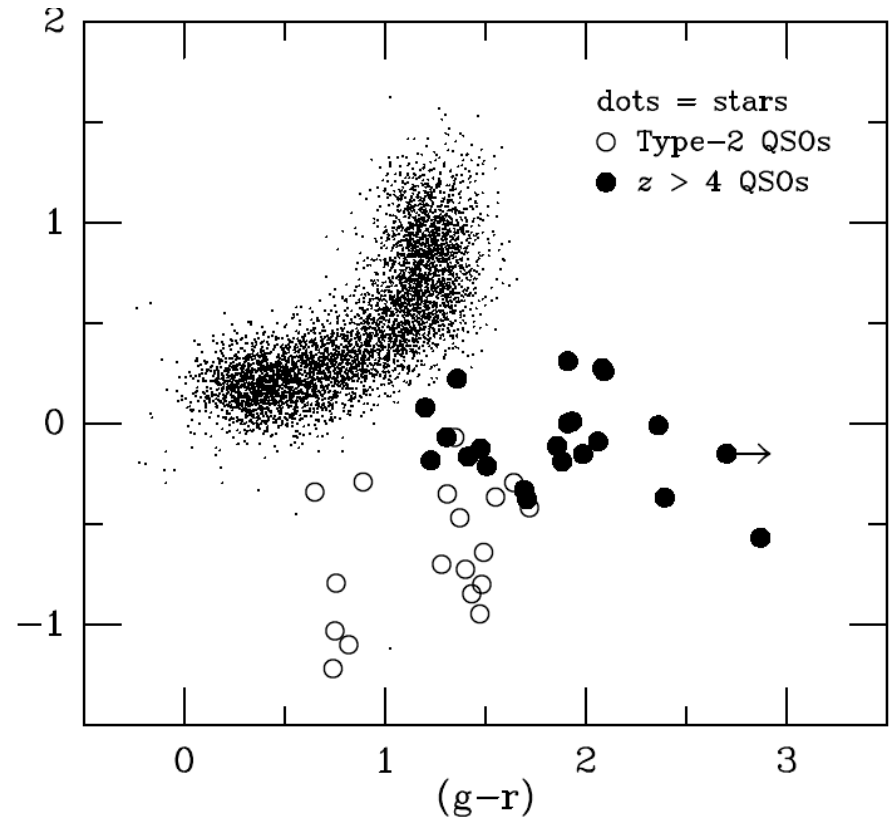
(from Moore 2002)

# Exploration of observable parameter spaces and searches for rare or new types of objects

A Generic Machine-Assisted Discovery Problem:  
Data Mapping and a Search for Outliers



A simple, real-life example:



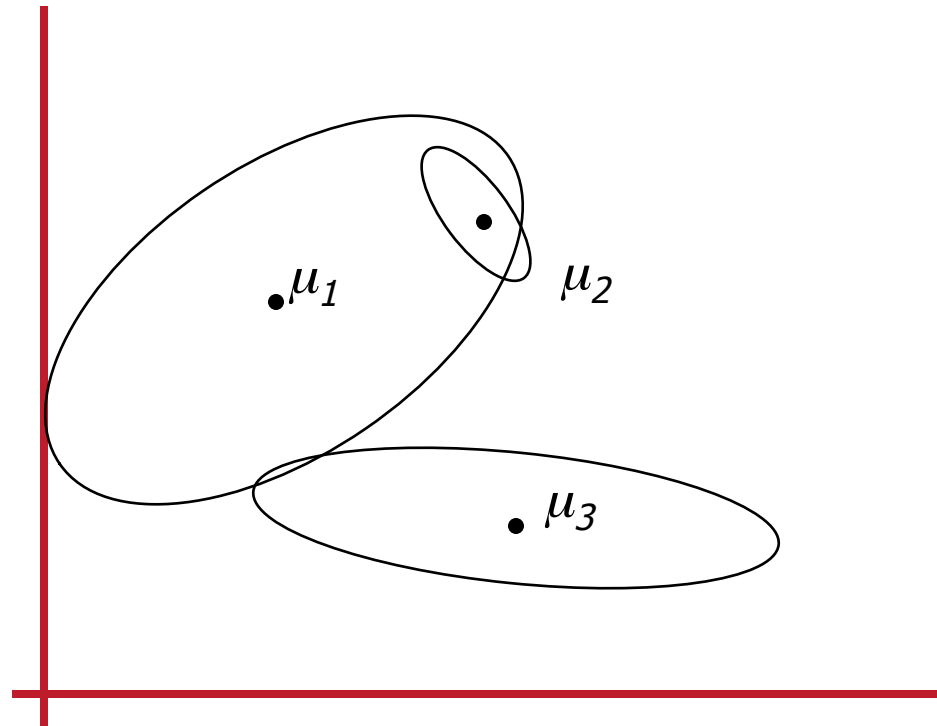
Now consider  $\sim 10^9$  data vectors  
in  $\sim 10^2 - 10^3$  dimensions ...

# Gaussian Mixture Modeling

- Data points are distributed in some  $N$ -dimensional parameter space,

$$x_j, j = 1, \dots, N$$

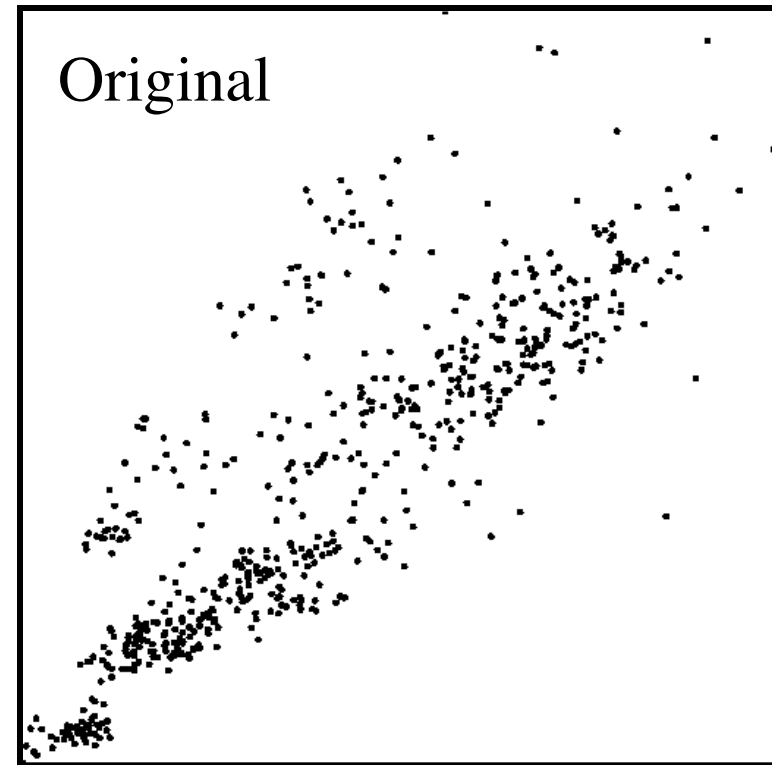
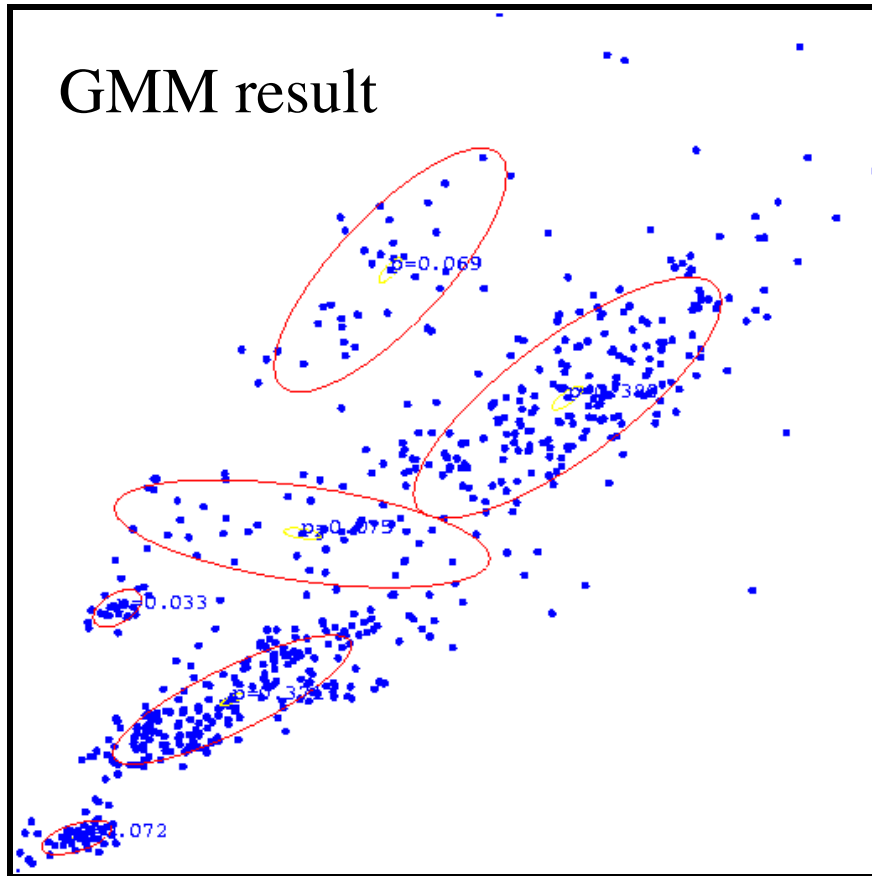
- There are  $k$  clusters,  $w_i$ ,  $i = 1, \dots, k$ , where the **number of clusters,  $k$** , may be either given by the scientist, or derived from the data themselves
- Each cluster can be **modeled as an  $N$ -variate Gaussian** with mean  $\mu_i$  and covariance matrix  $S_i$
- Each data point has an association probability of belonging to each of the clusters,  $P_i$



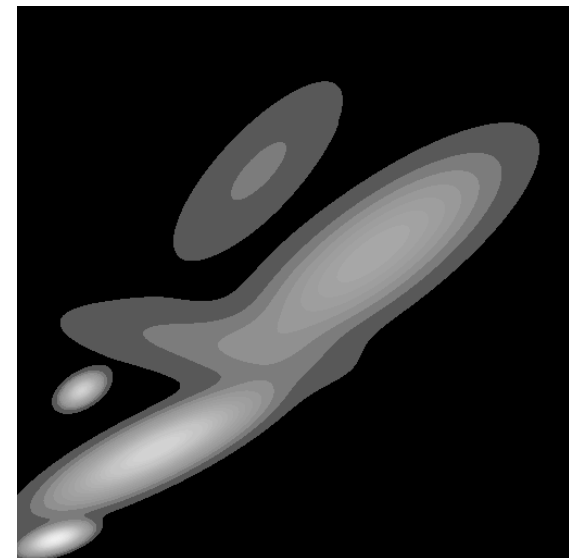


# An Example

(from Moore et al.)

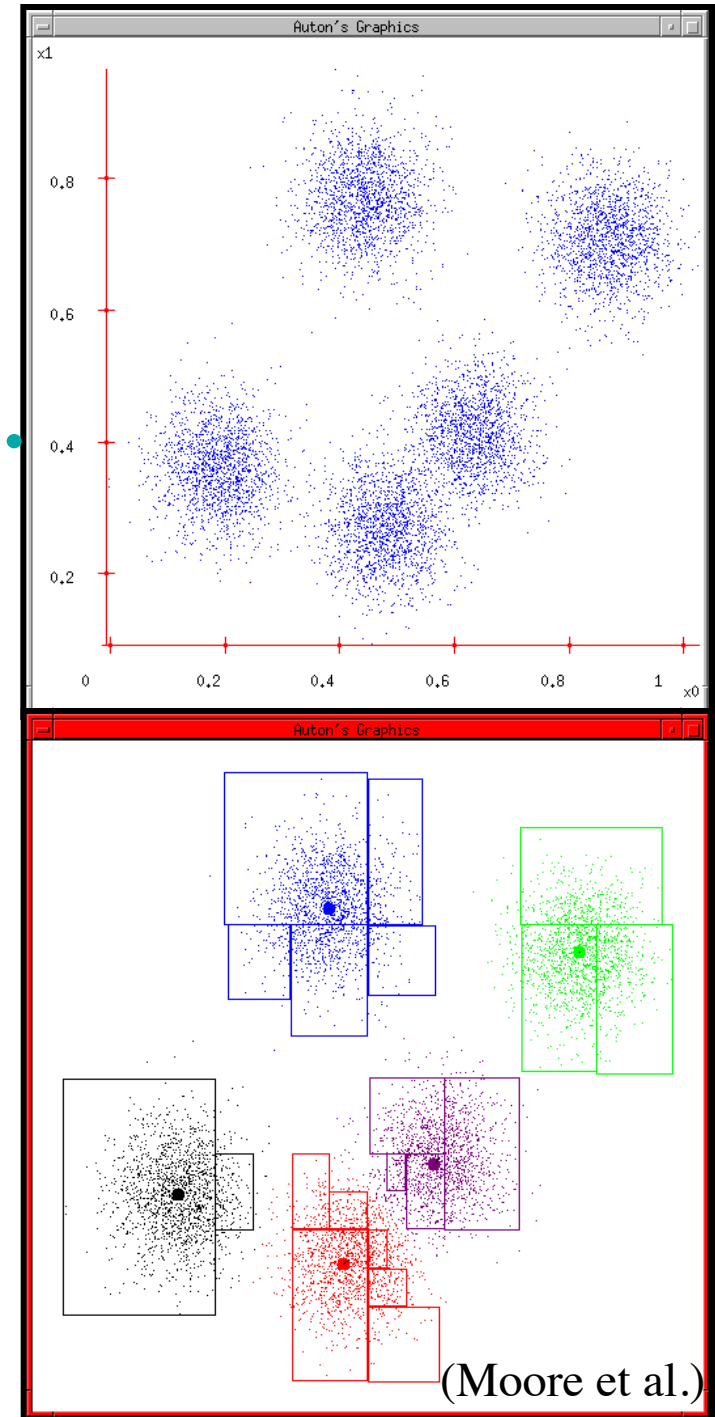


Model density distribution  $\Rightarrow$



# A Popular Technique: K-Means

- Start with  $k$  random cluster centers
- Assume a data model (e.g., Gaussian)
  - In principle, it can be some other type of a distribution
- Iterate until it converges
  - There are many techniques; Expectation Maximization (EM) is very popular; multi-resolution  $kd$ -trees are great (Moore, Nichol, Connolly, et al.)
- Repeat for a different  $k$  if needed
- Determine the optimal  $k$  :
  - Monte-Carlo Cross-Validation
  - Akaike Information Criterion (AIC)
  - Bayesian Information Criterion (BIC)



# Core methods of statistics, machine learning, data mining, and their scaling

- **Querying:** nearest-neighbor  $O(N)$ , spherical range-search  $O(N)$ , orthogonal range-search  $O(N)$ , contingency table
- **Density estimation:** kernel density estimation  $O(N^2)$ , mixture of Gaussians  $O(N)$
- **Regression:** linear regression  $O(D^3)$ , kernel regression  $O(N^2)$ , Gaussian process regression  $O(N^3)$
- **Classification:** nearest-neighbor classifier  $O(N^2)$ , nonparametric Bayes classifier  $O(N^2)$ , support vector machine
- **Dimension reduction:** principal component analysis  $O(D^3)$ , non-negative matrix factorization, kernel PCA  $O(N^3)$ , maximum variance unfolding  $O(N^3)$
- **Outlier detection:** by robust  $L_2$  estimation, by density estimation, by dimension reduction
- **Clustering:** k-means  $O(N)$ , hierarchical clustering  $O(N^3)$ , by dimension reduction
- **Time series analysis:** Kalman filter  $O(D^3)$ , hidden Markov model, trajectory tracking
- **2-sample testing:** n-point correlation  $O(N^n)$
- **Cross-match:** bipartite matching  $O(N^3)$

*(from A. Gray)*

**In modern data sets:  $D_D \gg 1, D_S \gg 1$**

Data Complexity  $\rightarrow$  Multidimensionality  $\rightarrow$  Discoveries

But the bad news is ...

**The computational cost of clustering analysis:**

K-means:  $K \times N \times I \times D$

Expectation Maximization:  $K \times N \times I \times D^2$

Monte Carlo Cross-Validation:  $M \times K_{\max}^2 \times N \times I \times D^2$

$N$  = no. of data vectors,  $D$  = no. of data dimensions

$K$  = no. of clusters chosen,  $K_{\max}$  = max no. of clusters tried

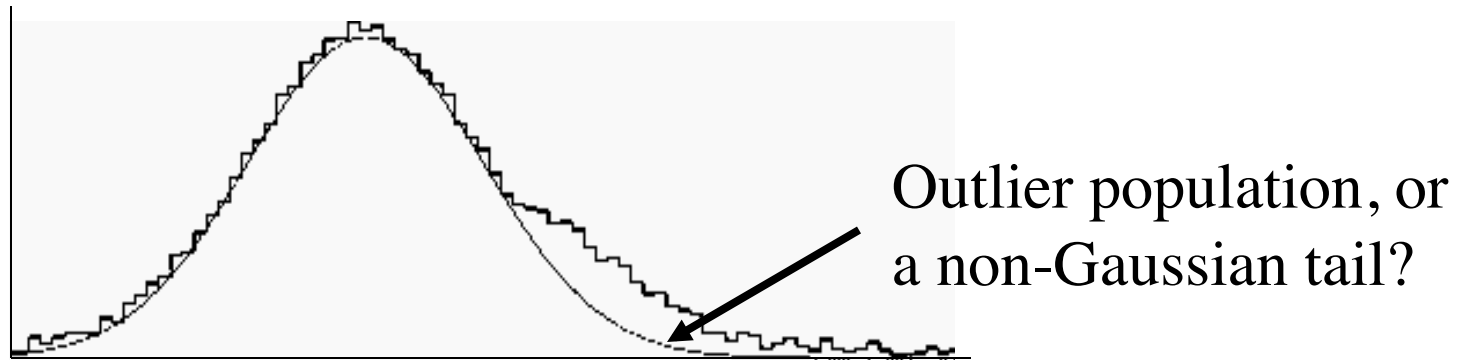
$I$  = no. of iterations,  $M$  = no. of Monte Carlo trials/partitions

 *Terascale (Petascale?) computing and/or better algorithms*

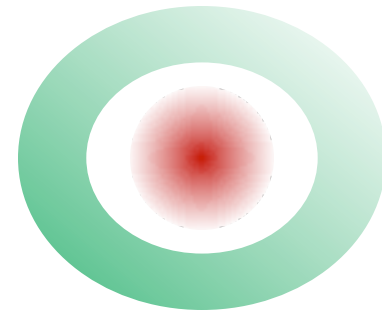
Some dimensionality reduction methods do exist (e.g., PCA, class prototypes, hierarchical methods, etc.), but more work is needed

# Some Practical and Theoretical Problems in Clustering Analysis

- Data heterogeneity, biases, selection effects ...
- Non-Gaussianity of clusters (data models)



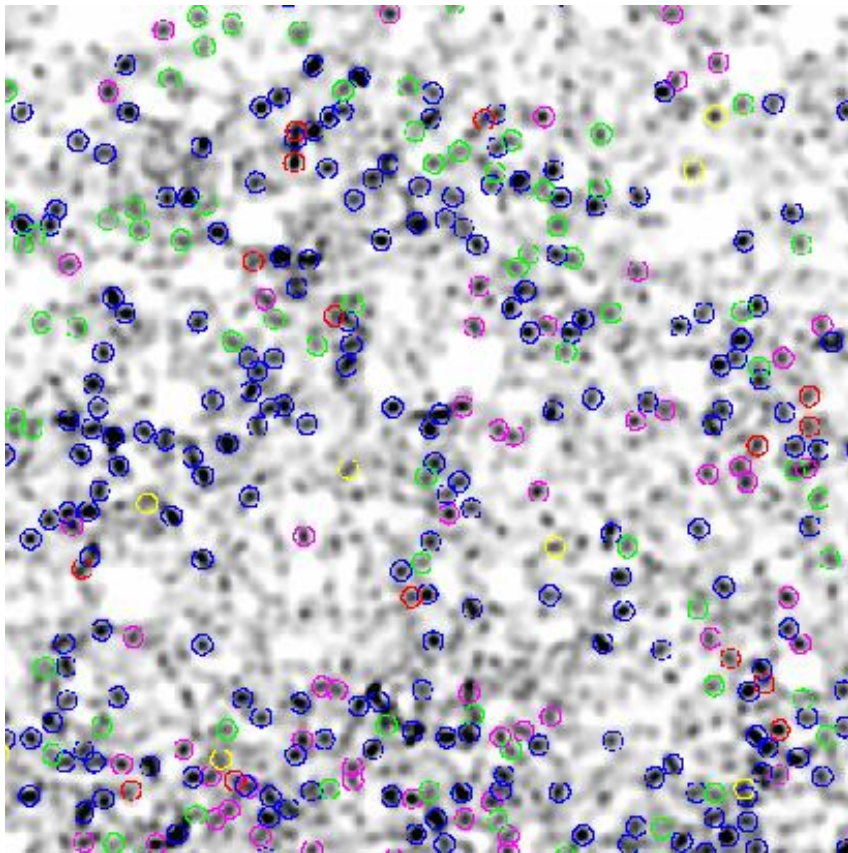
- Missing data, upper and lower limits
- Non-Gaussian (or non-Poissonian) noise
- Non-trivial topology of clustering
- Useful vs. “useless” parameters ...





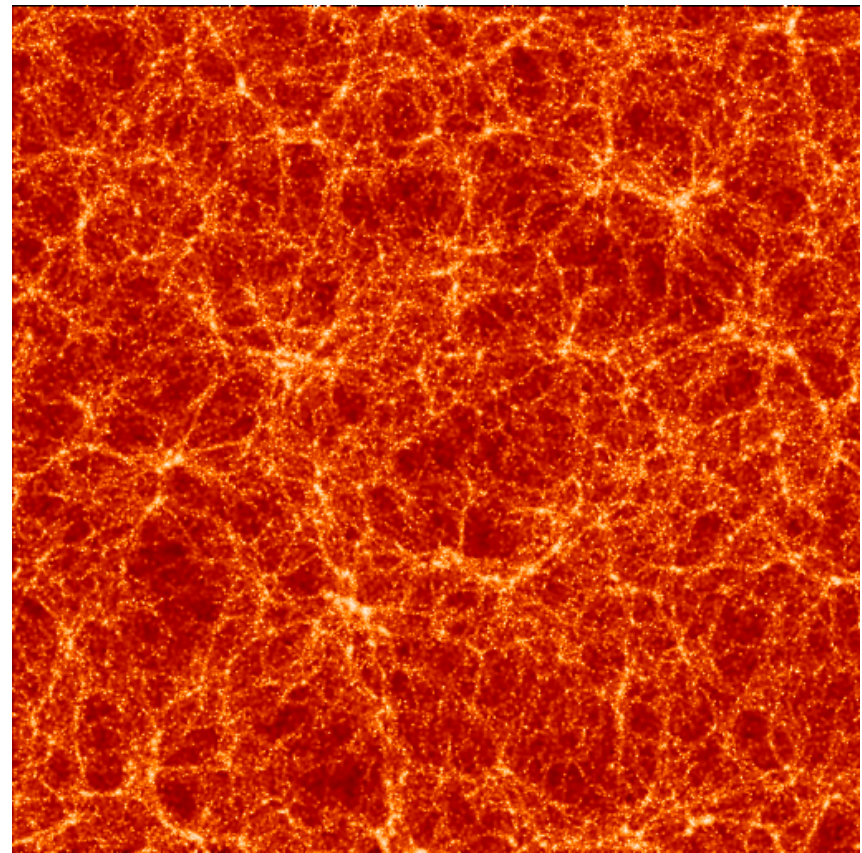
# Some Simple Examples of Challenges for Clustering Analysis from “Standard” Astronomical Galaxy Clustering Analysis

Clustering on a clustered background



DPOSS Clusters (Gal et al.)

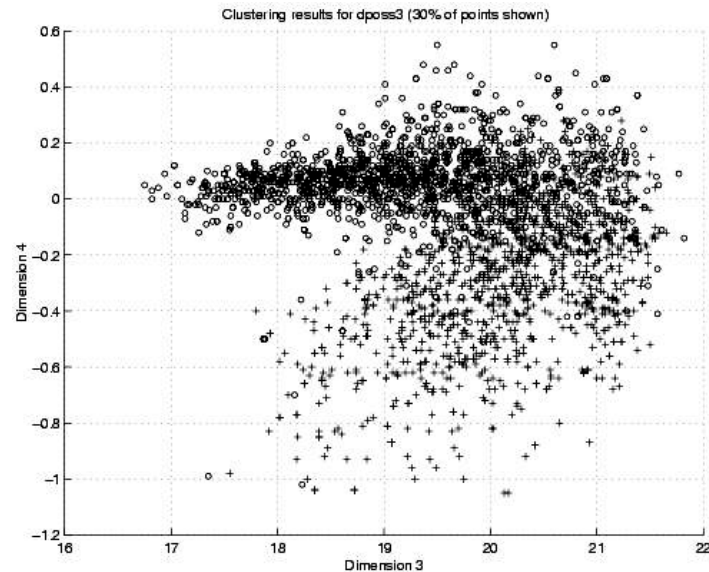
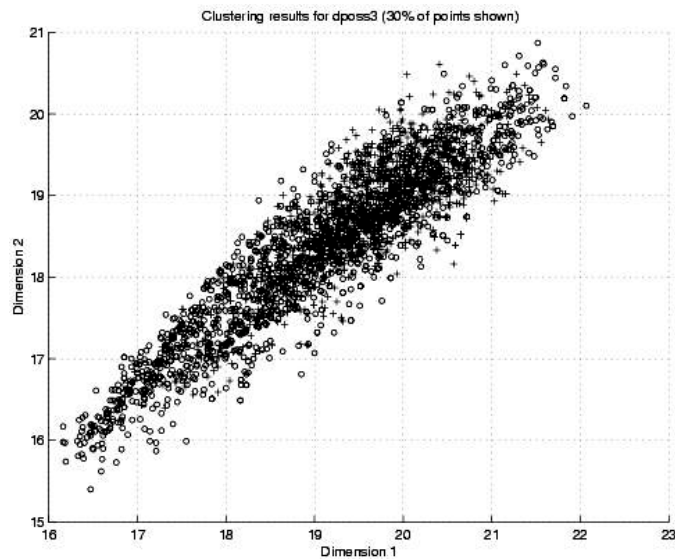
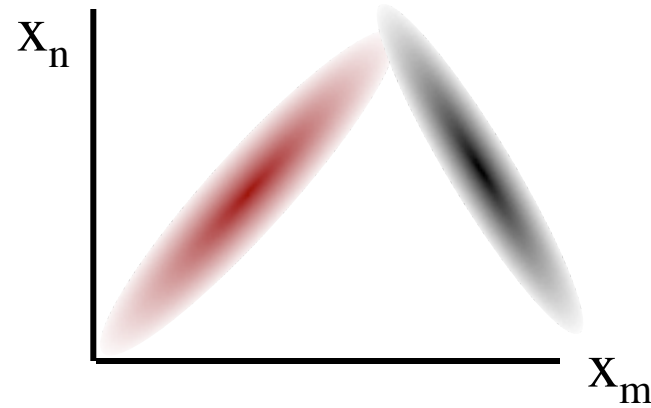
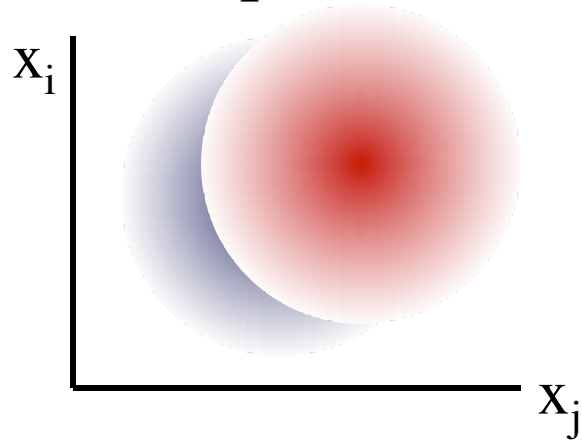
Clustering with a nontrivial topology



LSS Numerical Simulation (VIRGO)

# Useful vs. “Useless” Parameters:

Clusters (classes) and correlations may exist/separate in some parameter subspaces, but not in others

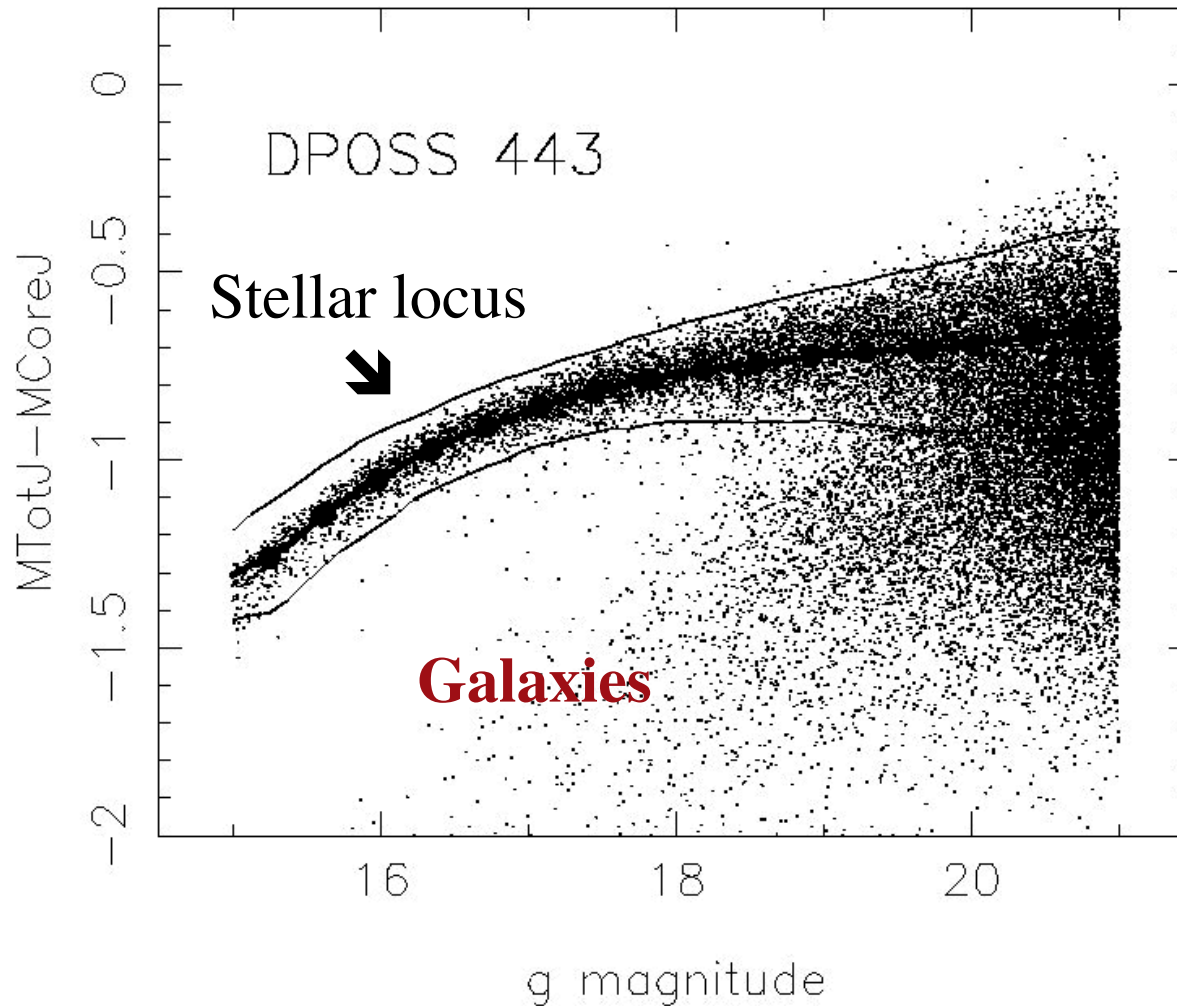


# A Relatively Simple Classification Problem: Star-Galaxy Separation

- Important, since for most astronomical studies you want either stars ( $\sim$  quasars), or galaxies; the depth to which a reliable classification can be done is the effective limiting depth of your catalog - not the detection depth
  - There is generally more to measure for a non-PSF object
- You'd like to have an automated and objective process, with some estimate of the accuracy as a  $f(\text{mag})$ 
  - Generally classification fails at the faint end
- Most methods use some measures of light concentration vs. magnitude (perhaps more than one), and/or some measure of the PSF fit quality (e.g.,  $\chi^2$ )
- For more advanced approaches, use some *machine learning method, e.g., neural nets or decision trees*



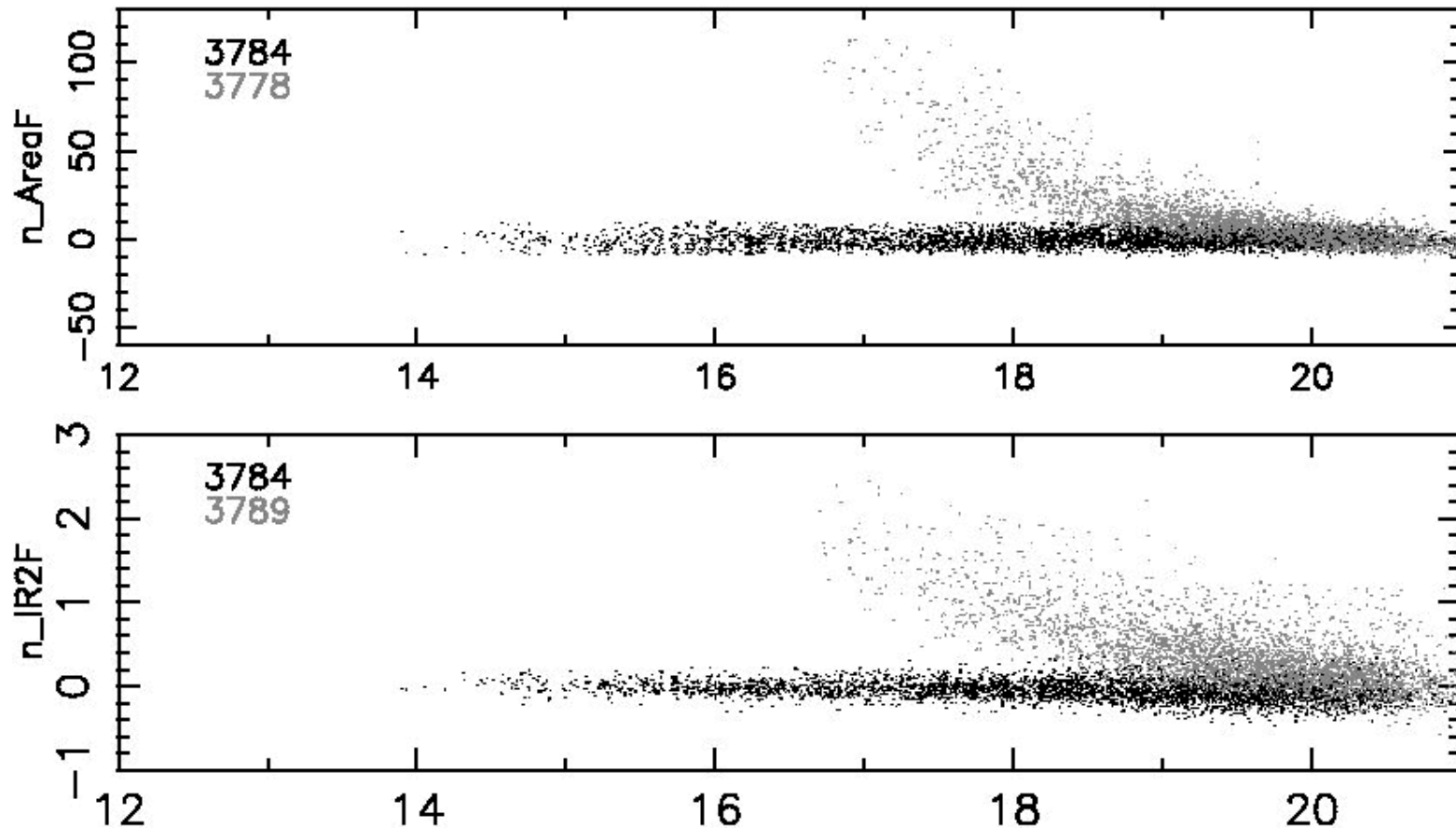
# Typical Parameter Space for S/G Classif.



(From DPOSS)

A set of such parameters can be fed into an automated classifier (ANN, DT, ...) which can be trained with a “ground truth” sample

# More S/G Classification Parameter Spaces: Normalized By The Stellar Locus



Then a set of such parameters can be fed into an automated classifier (ANN, DT, ...) which can be trained with a “ground truth” sample



# Automated Star-Galaxy Classification: Artificial Neural Nets (ANN)

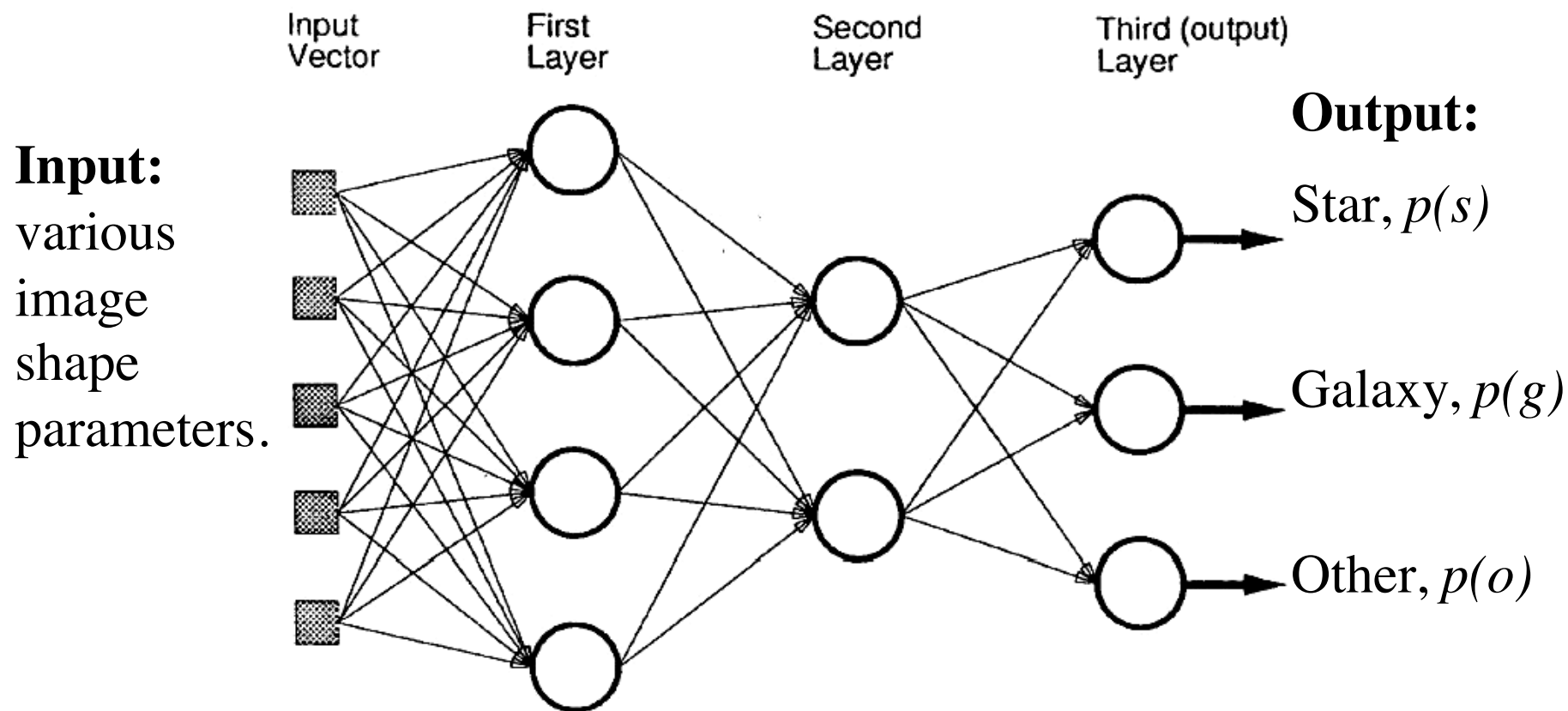


FIG. 6. Schematic illustration of a network with an input vector of length five, four nodes in the first layer, two nodes in the second layer, and three in the output layer. As a shorthand, such a network can be written as (5:4,2,3).

*(Odewahn et al. 1992)*

# Automated Star-Galaxy Classification: Decision Trees (DTs)

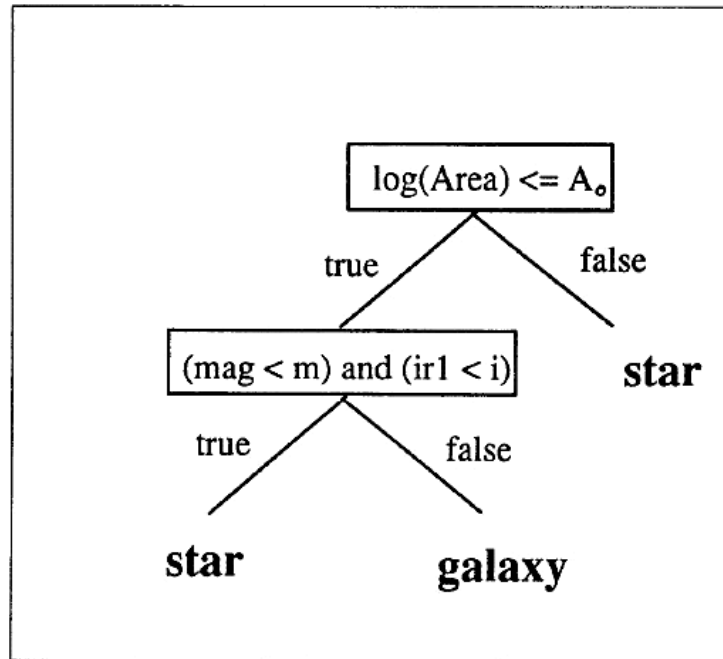


FIG. 1. In this sample decision tree, one starts at the top node(root), following the appropriate path to a final leaf (class) based upon the truth of the assertion at each node.

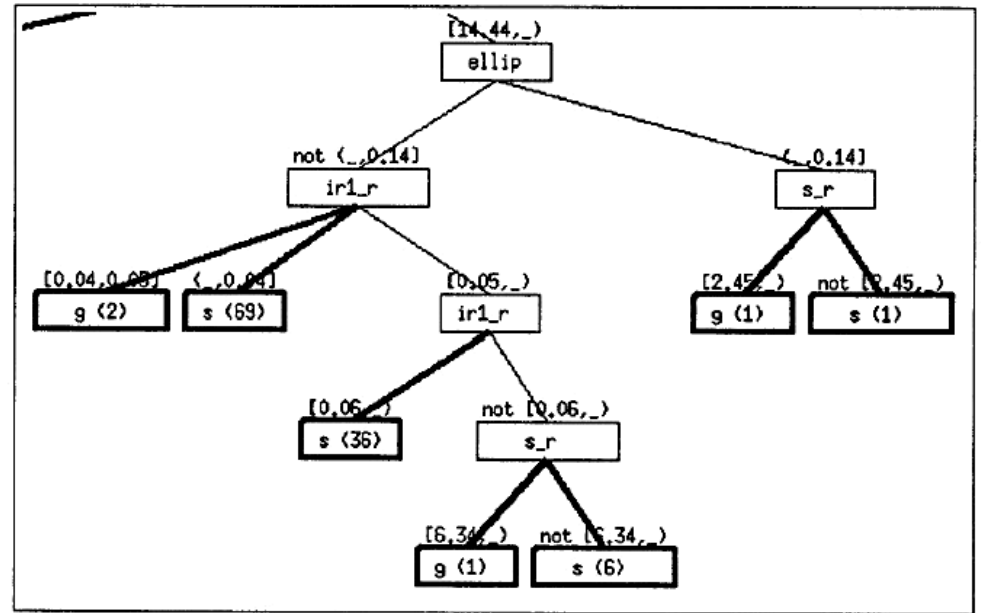
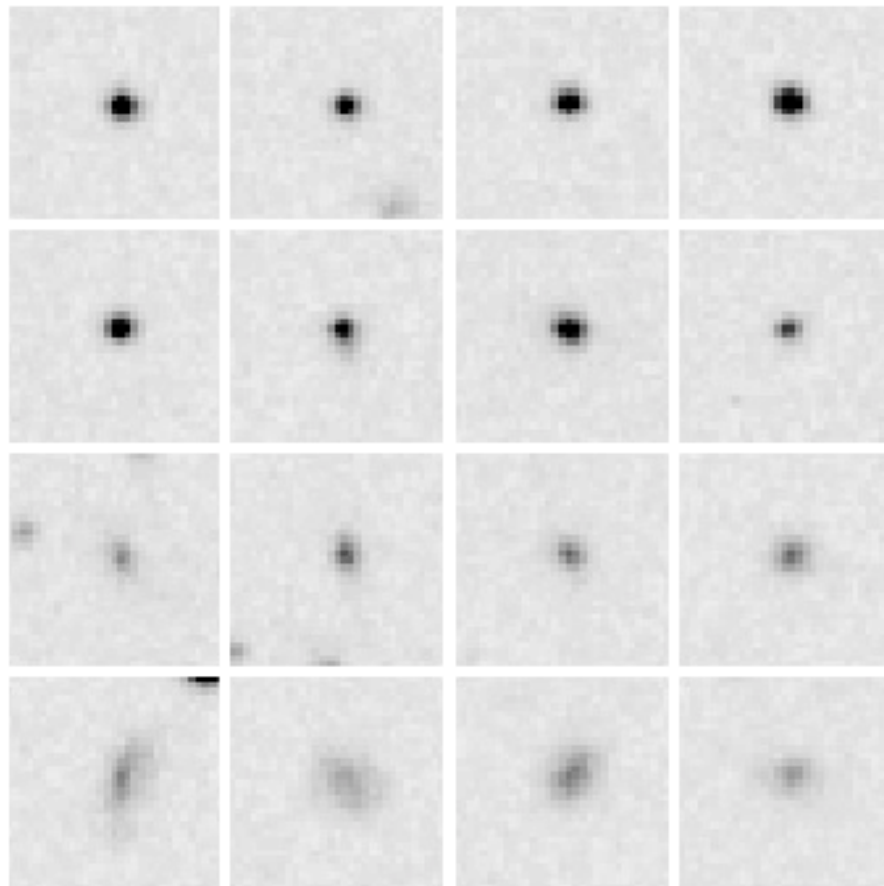


FIG. 2. A portion of a much larger actual decision tree generated by the O-Btree algorithm for performing star/galaxy classification. The interval appearing above each node indicates the range in value of the attribute specified in the node above that an object must meet for it to pass along that branch. The dark branches lead to actual classifications. The number in parentheses within each leaf indicates the number of training examples classified correctly at that node.

*(Weir et al. 1995)*

# Automated Star-Galaxy Classification: Unsupervised Classifiers

No training data set - the program decides on the number of classes present in the data, and partitions the data set accordingly.



Star

Star+fuzz

Gal1 (E?)

Gal2 (Sp?)

An example:

AutoClass

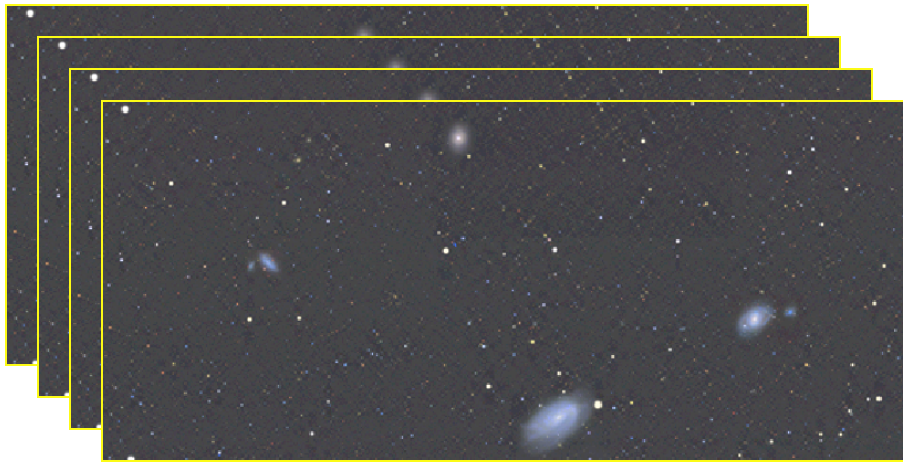
(*Cheeseman et al.*)

Uses Bayesian approach in machine learning (ML).

This application from DPOSS (*Weir et al. 1995*)

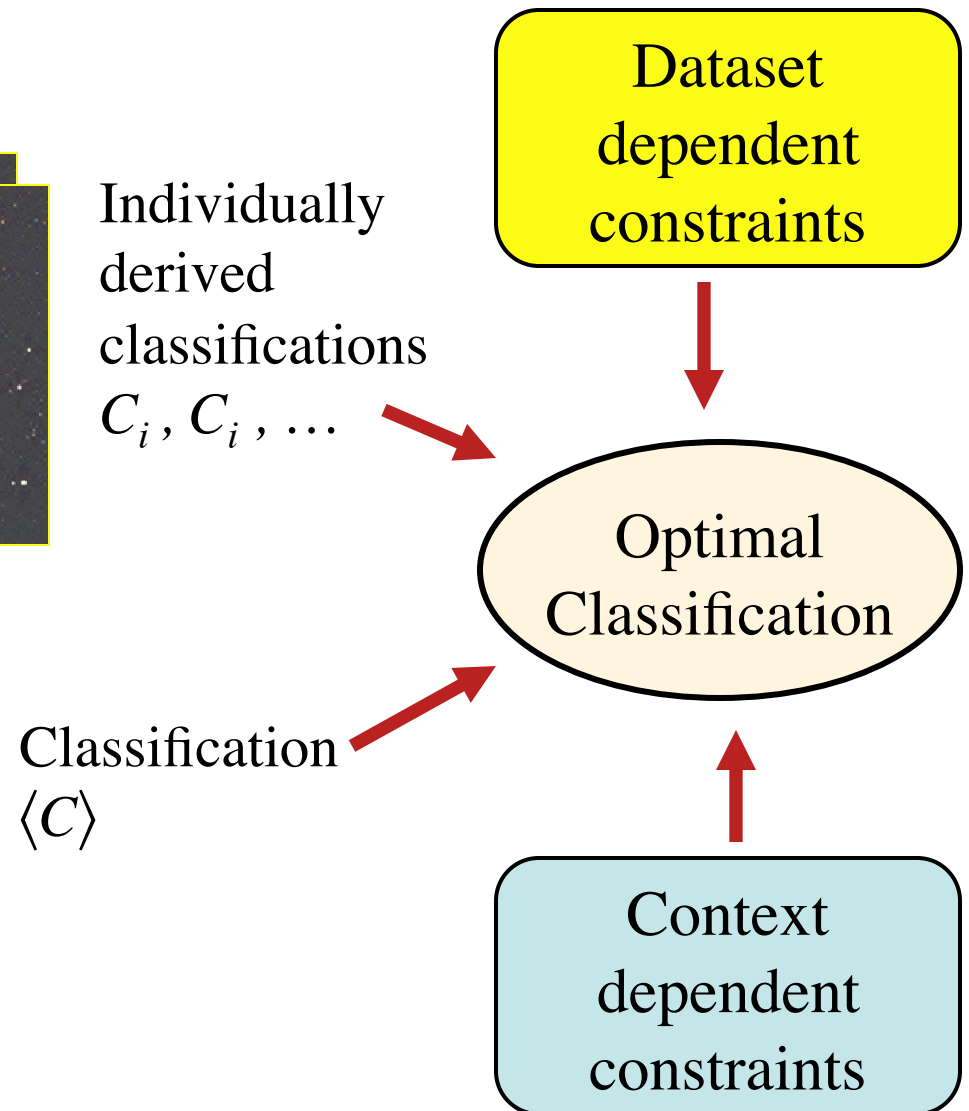
# Star-Galaxy Classification: The Next Generation

Multiple imaging data sets



Individually  
derived  
classifications  
 $C_1, C_2, \dots$

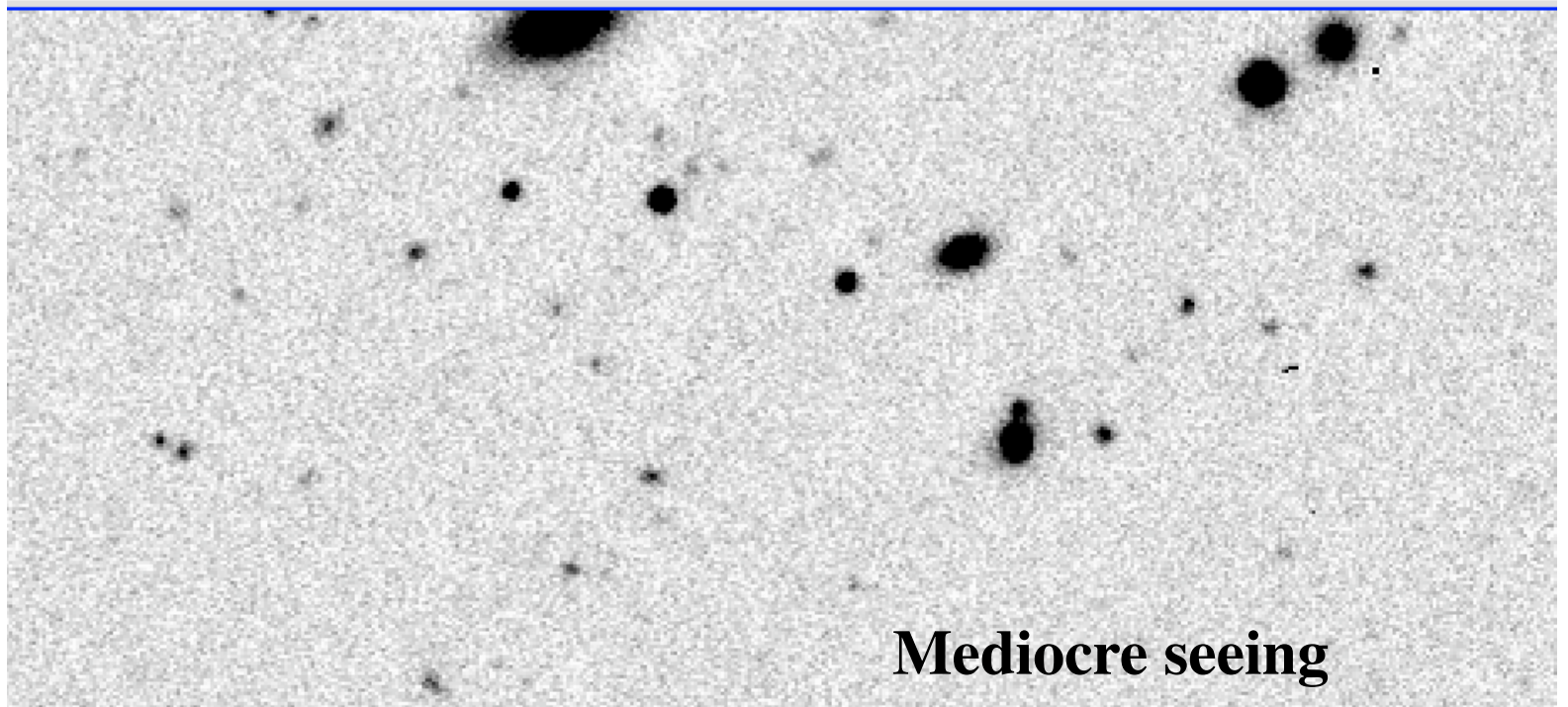
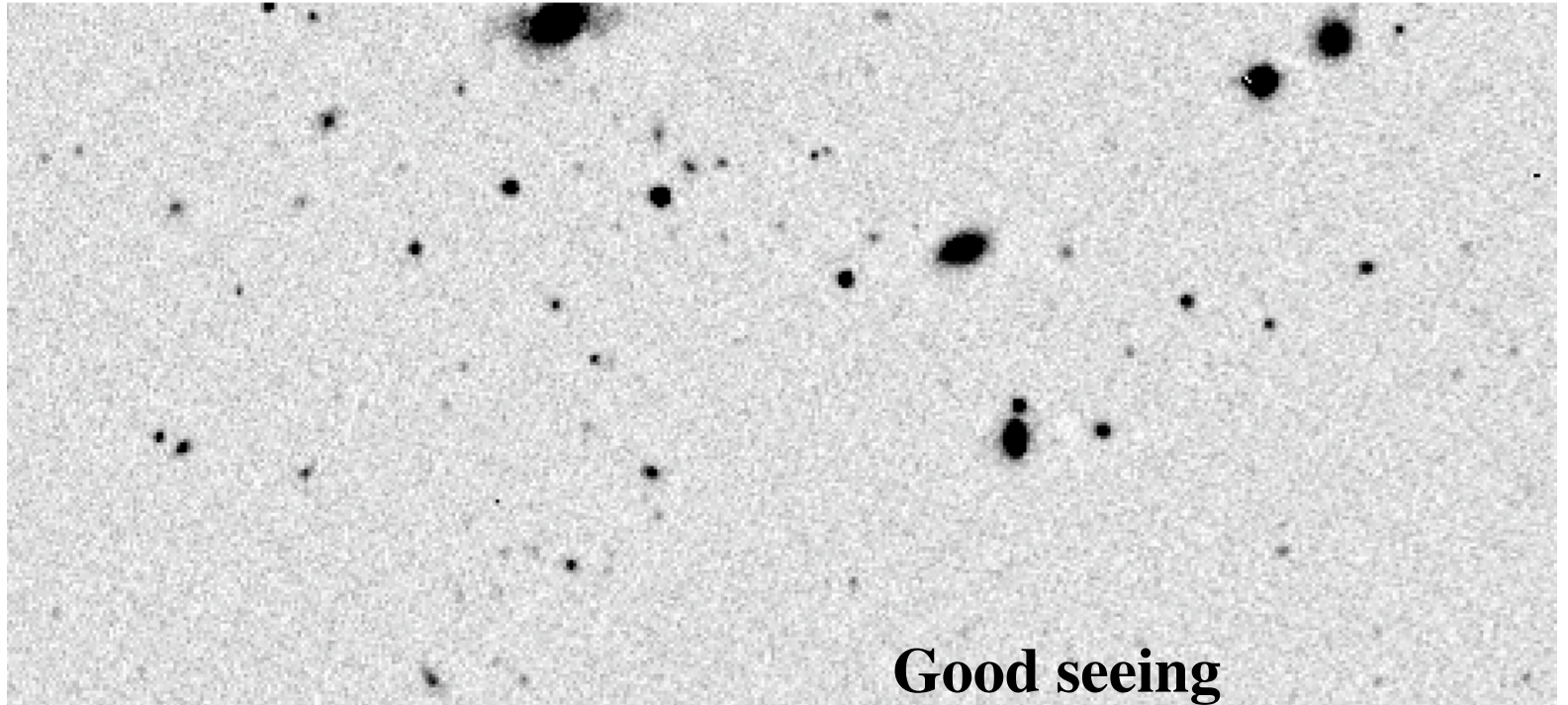
Optimally combined imagery





**One key external constraint is the “seeing” quality for multiple imaging passes**

(quantifiable e.g., as the PSF FWHM)





# How to Incorporate the External or A Priori (Contextual) Knowledge?

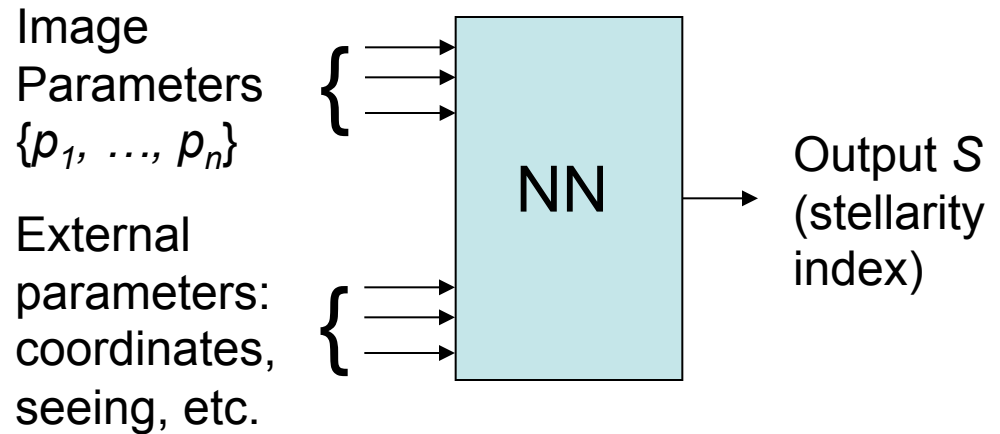
- Examples: seeing and transparency for a given night; direction on the sky, in Galactic coordinates; continuity in the star/galaxy fraction along the scan; etc.
- Still an open problem in the machine learning
- In principle, it should lead to an improved classification
- The problem occurs both in a “single pass” classification, and in combining of multiple passes
- In machine learning approaches, must somehow convert the external or a priori knowledge into classifier inputs - but the nature of this information is qualitatively different from the usual input (individual measurement vectors)

# Two Approaches Using ANN:

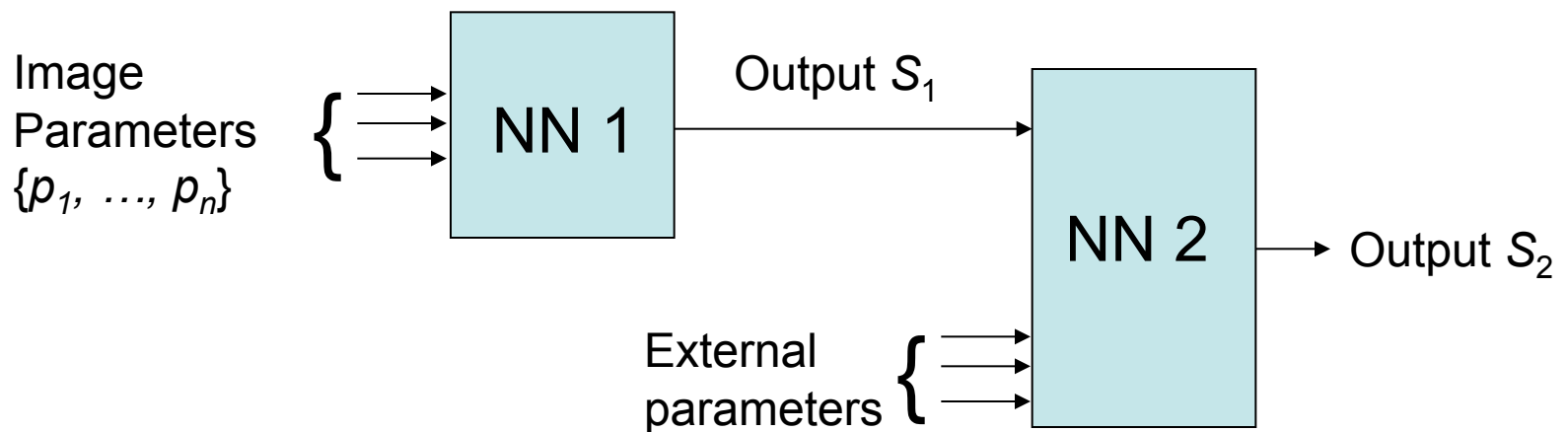
## 1. Include the external knowledge among the input parameters

Object dependent

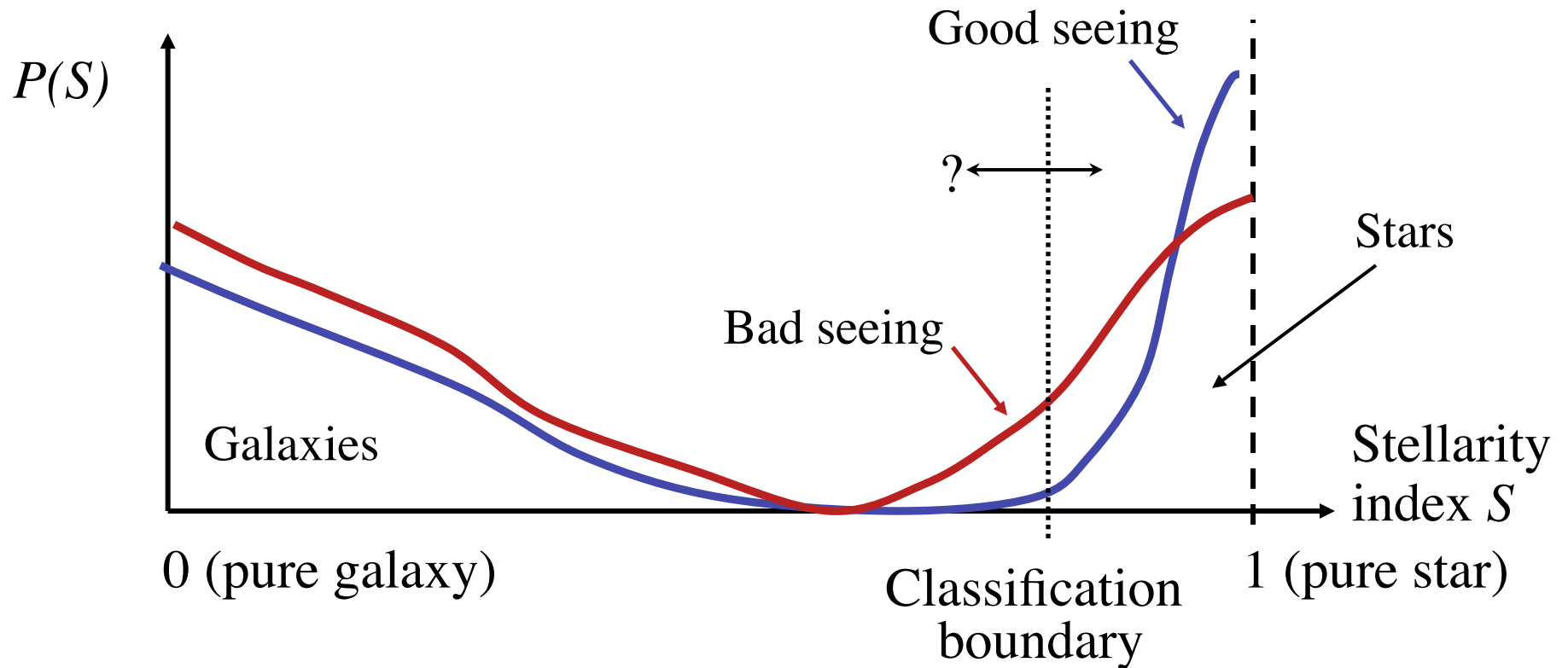
Dataset dependent



## 2. A two-step classification:



# Classification Bias and Accuracy

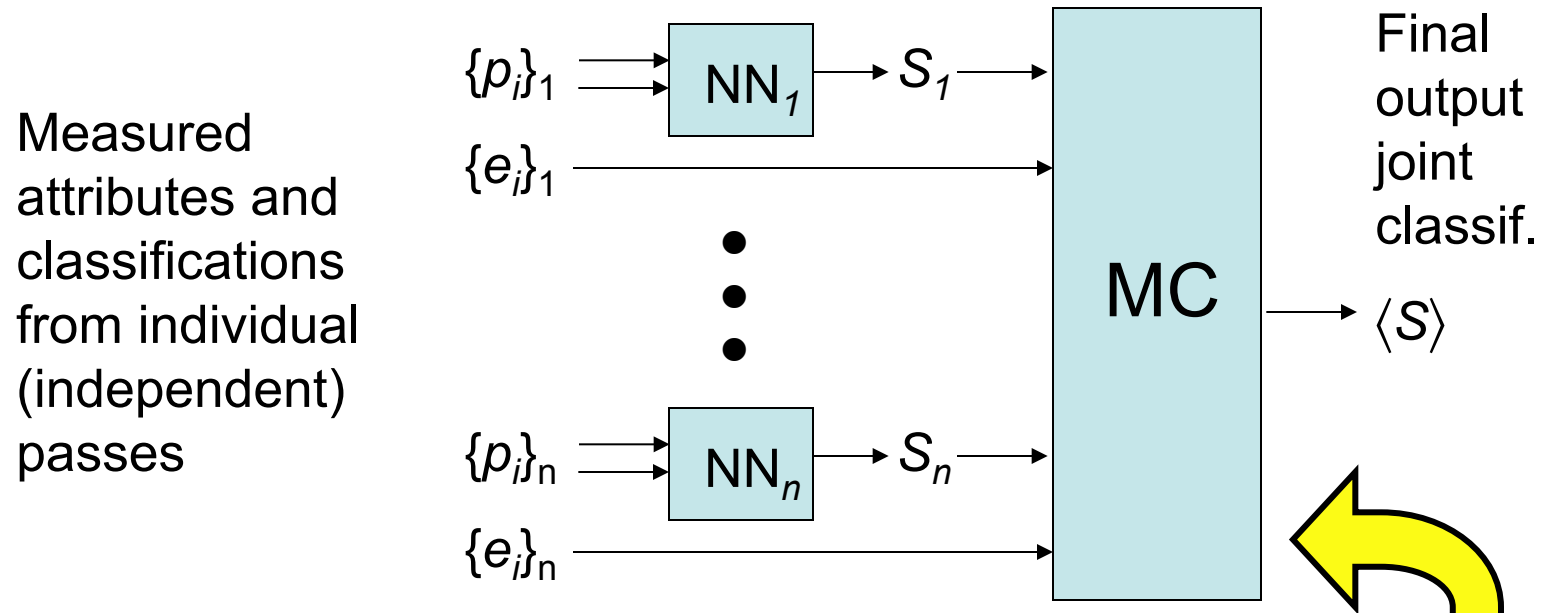


Assuming a classification boundary divider (stars/galaxies) derived from good quality data, and applying it to poorer quality data, would lead to a ***purier, but biased sample***, as some stars will be misclassified as galaxies.

Shifting the boundary (e.g., on the basis of external knowledge) would ***diminish the bias, but also degrade the purity***.

# Combining Multiple Classifications

Metaclassifier, or a committee of machines with a chairman?



Note: individual classifiers **J** may be optimized or trained differently

Design?  
Weighting algorithm?  
Training data set?  
Validation data set?

# The (Proper) Uses of Statistics

- Hypothesis testing
- Model fitting
- **Data exploration:**
  - Multivariate analysis (MVA) and correlation search
  - Clustering analysis and classification
  - Image processing and deconvolutions
- **Data Mining (or KDD):**
  - Computational/algorithmic implementations of statistical tools

**NB: Statistical Significance  $\neq$  Scientific Relevance!**

## **BAD uses of statistics:**

- As a substitute for data (quantity or quality)
- To justify something *a posteriori*

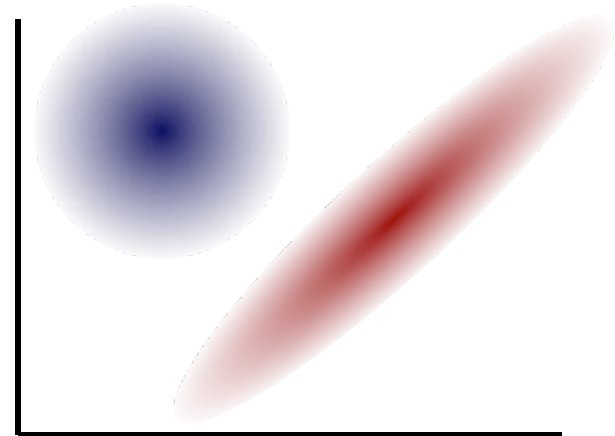
# Multivariate Analysis (MVA)

## Multivariate Correlation Search:

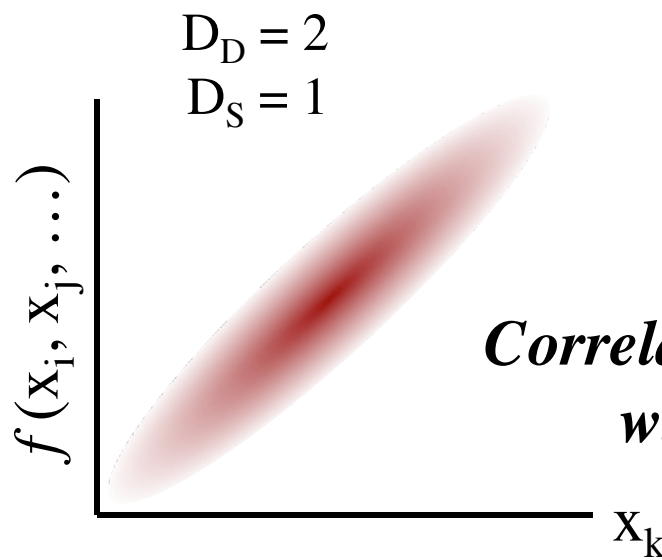
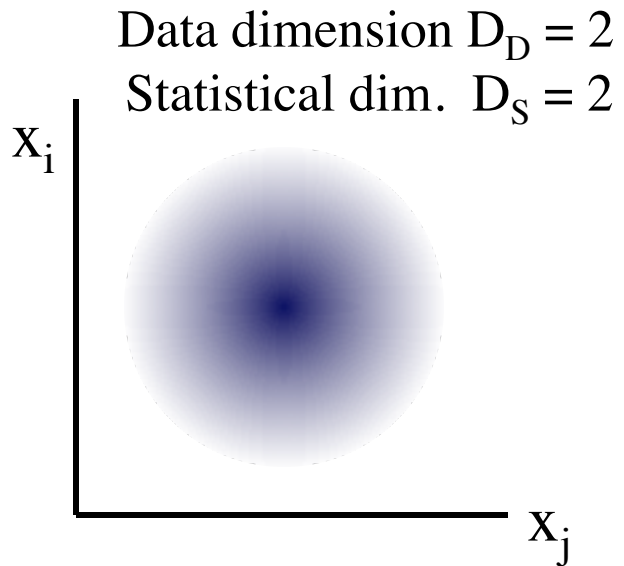
- Are there significant, nontrivial correlations present in the data?
- Simple monovariate correlations are rare: multivariate data sets can contain more complex correlations
- What is the statistical dimensionality of the data?

## Clusters vs. Correlations:

“Physics” → Correlations  
Correlations → reduction of  
the statistical  
dimensionality



# Correlation Searches in Attribute Space

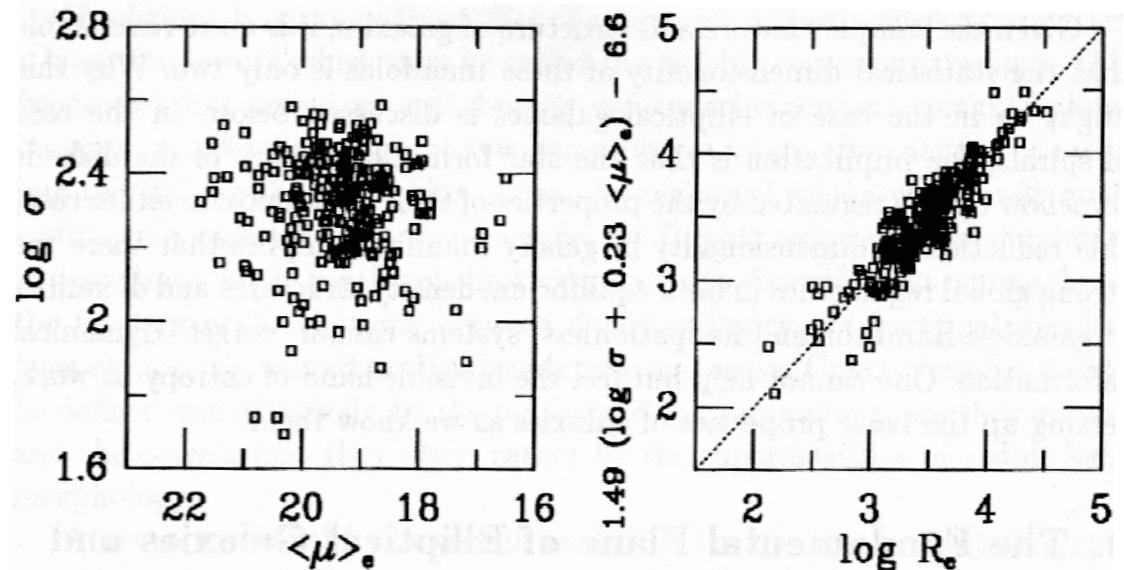


If  $D_S < D_D$ ,  
correlations  
are present

*Correlations are clusters  
with dimensionality  
reduction*

## A real-life example:

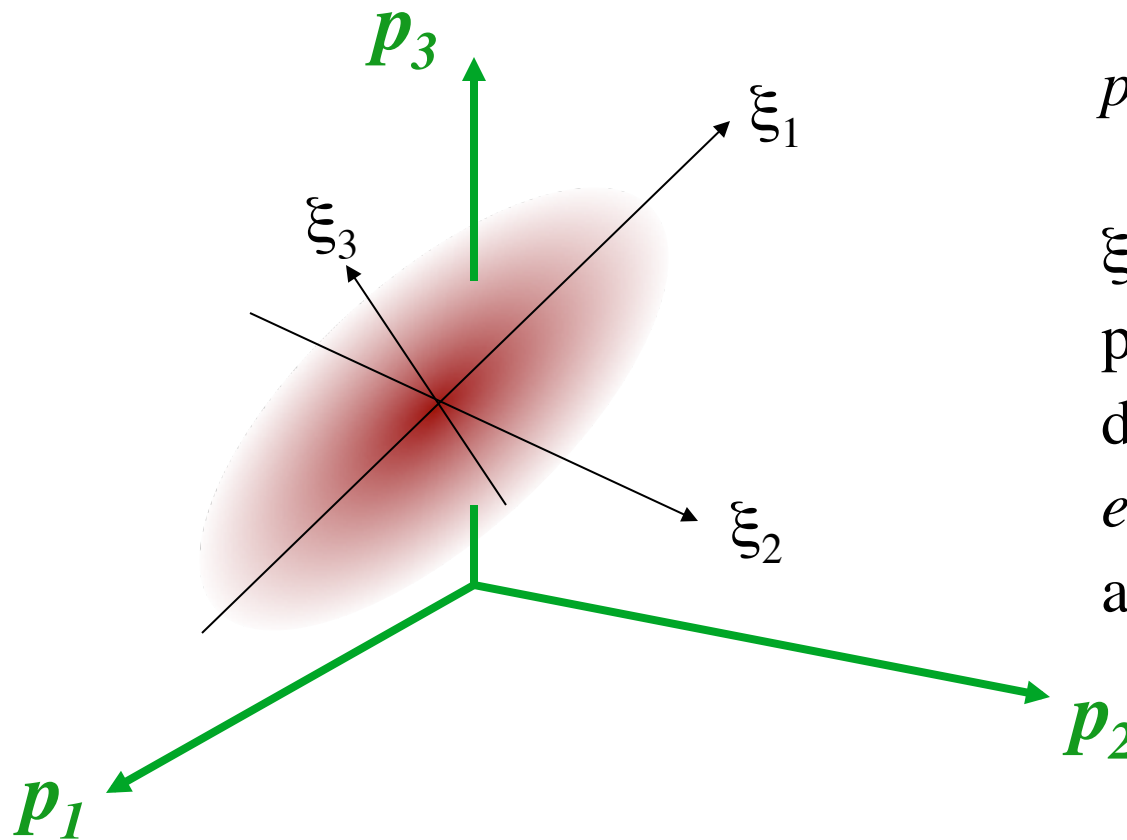
“Fundamental Plane” of elliptical galaxies, a set of bivariate scaling relations in a parameter space of  $\sim 10$  dimensions, containing valuable insights into their physics and evolution





# Principal Component Analysis

Solving the eigen-problem of the data  
hyperellipsoid in the parameter space of measured  
attributes



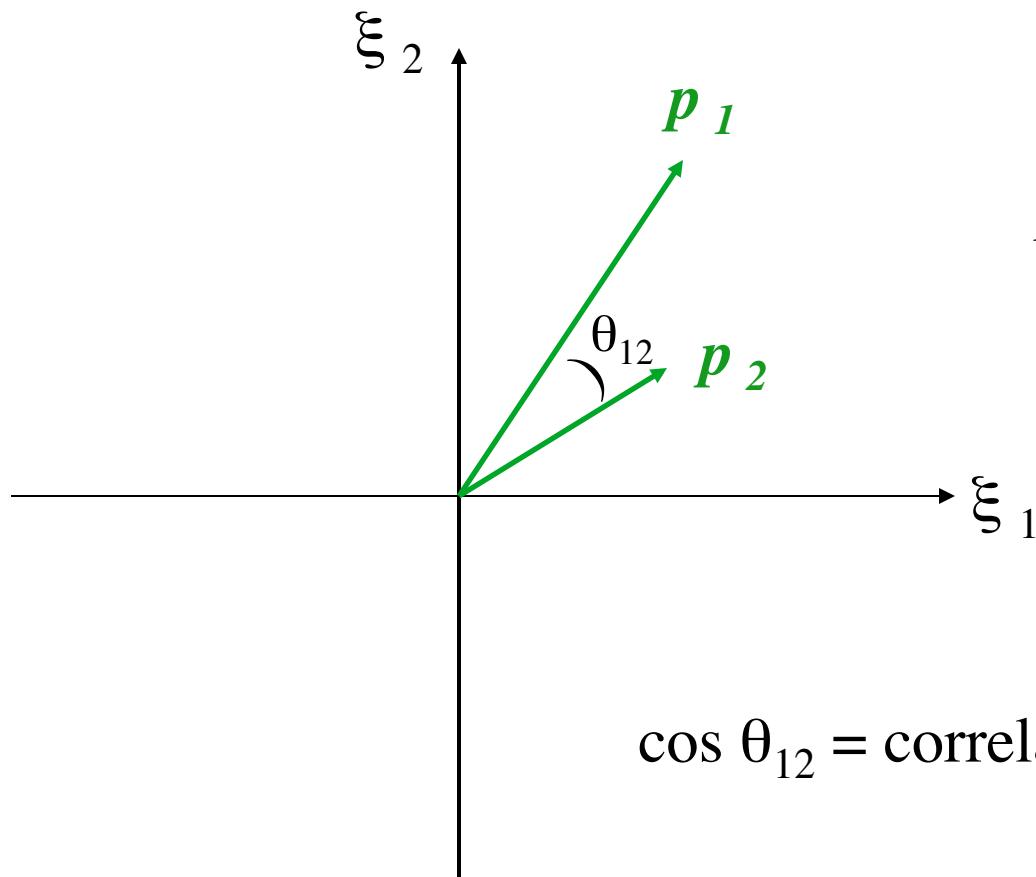
$p_i$  = observables  
( $i = 1, \dots, D_{\text{data}}$ )

$\xi_j$  = eigenvectors, or  
principal axes of the  
data hyperellipsoid

$e_j$  = eigenvalues, or  
amplitudes of  $\xi_j$   
( $j = 1, \dots, D_{\text{stat}}$ )

# Correlation Vector Diagrams:

Projections of the data and observable axes onto the planes defined by the eigenvectors



$$\xi_i = a_{i1} p_1 + a_{i2} p_2 + \dots$$
$$p_i = b_{i1} \xi_1 + b_{i2} \xi_2 + \dots$$

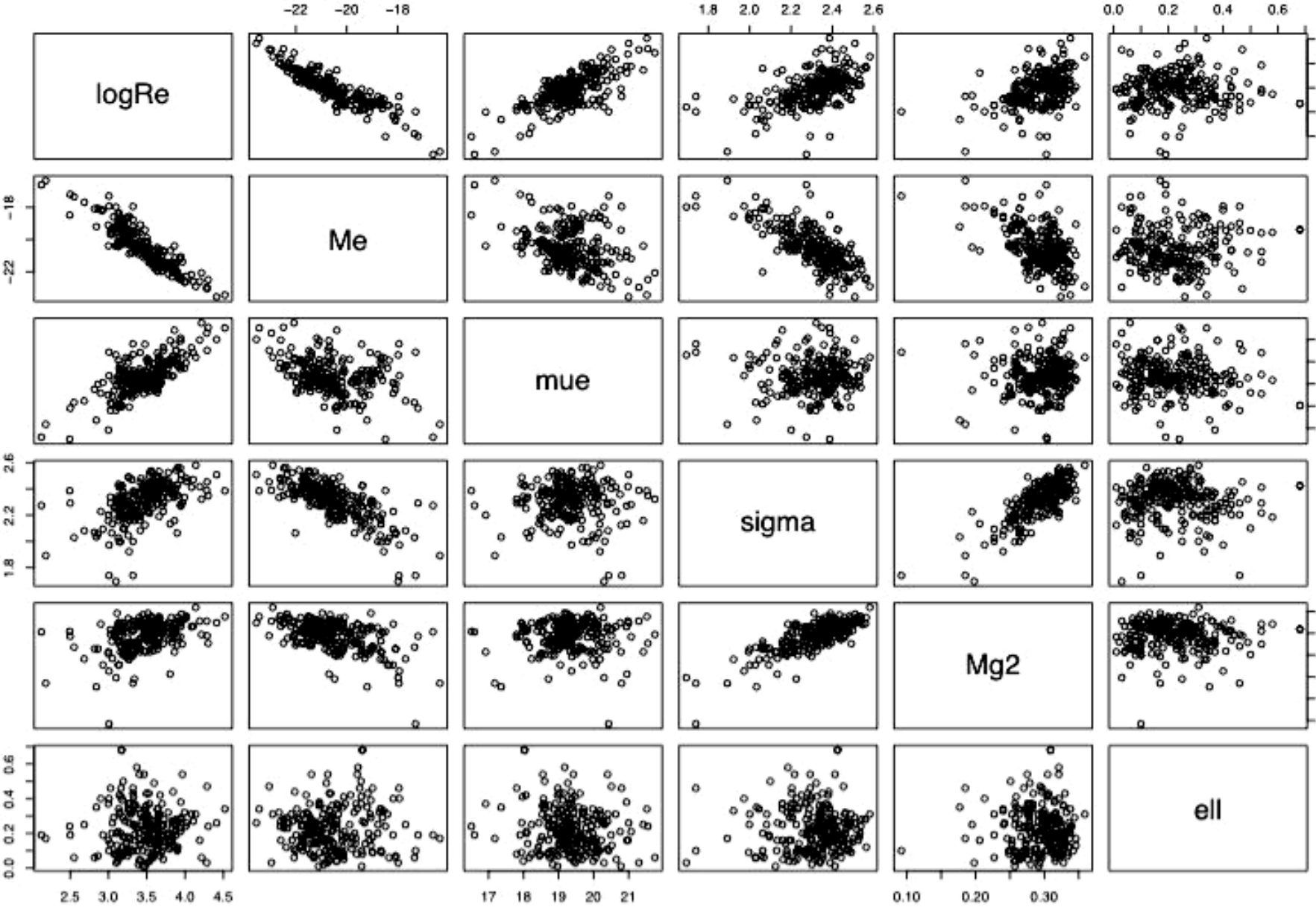
$\cos \theta_{12} = \text{correlation coef. of } p_1 \text{ and } p_2$

# An Example, Using VOSTat

Here is a data file, with 6 observed and 5 derived quantities (columns) for a few hundred elliptical galaxies (rows, data vectors):

```
# Ellipticals from the Djorgovski et al. survey
#
logRe  M_e   mu_e  sigma  Mg2   M/L  logM  rho_M  rho_L  f_eff  ell  GalID
#
3.863  -22.35  19.70  2.479  0.336  8.98  11.36  -0.847  -1.546  -0.205  .06  1016
3.442  -20.64  19.01  2.310  0.316  8.78  10.61  -0.344  -0.970  0.806  .29  1052
3.943  -22.46  19.78  2.468  0.325  8.90  11.42  -1.030  -1.742  -0.354  .23  1060
3.282  -19.65  19.38  2.299  0.246  9.07  10.42  -0.045  -0.883  1.137  .17  1172
3.509  -20.53  19.53  2.315  0.297  8.93  10.68  -0.467  -1.214  0.667  .24  1199
3.457  -20.55  19.29  2.322  0.297  8.90  10.64  -0.349  -1.050  0.764  .22  1199
3.463  -20.75  18.55  2.412  0.305  8.78  10.83  -0.181  -0.988  0.662  .54  1209
3.066  -18.60  19.16  2.207  0.301  9.01  10.02  0.204  -0.655  1.661  .29  1339
3.132  -18.66  19.36  2.158  0.282  8.93  9.99  -0.027  -0.831  1.578  .34  1351
3.141  -18.99  19.43  2.273  0.310  9.18  10.23  0.185  -0.726  1.445  .09  1374
3.477  -19.41  20.78  2.125  0.257  9.08  10.27  -0.784  -1.565  0.921  .01  1379
3.526  -21.02  19.22  2.396  0.313  8.95  10.86  -0.339  -1.069  0.552  .18  1395
3.257  -20.29  18.71  2.491  0.334  9.21  10.78  0.389  -0.552  0.995  .09  1399
3.265  -20.06  18.57  2.213  0.279  8.59  10.23  -0.184  -0.670  1.257  .37  1403
3.180  -20.16  18.42  2.353  0.317  8.89  10.43  0.266  -0.376  1.287  .12  1404
3.552  -20.97  19.42  2.438  0.327  9.09  10.97  -0.307  -1.167  0.458  .16  1407
```

# Pairwise Plots for Independent Observables



## Their Correlation Matrix:

	logRe	Me	mue	sigma	Mg2	e11
logRe	1.00	-0.90	0.73	0.53	0.41	0.03
Me	-0.90	1.00	-0.38	-0.74	-0.54	0.03
mue	0.73	-0.38	1.00	-0.01	0.04	-0.13
sigma	0.53	-0.74	-0.01	1.00	0.79	-0.01
Mg2	0.41	-0.54	0.04	0.79	1.00	0.00
e11	0.03	0.03	-0.13	-0.01	0.00	1.00

You can learn a lot just from the inspection of this matrix, and comparison with the pairwise (bivariate) plots ...

# Now Let's Do the Principal Component Analysis (PCA):

Principal Component Analysis(m) for logRe M\_e mu\_e sigma Mg2 :

Importance of components:

	PC1	PC2	PC3	PC4	PC5
Standard deviation	1.4	0.8	0.090	4e-02	2e-02
Proportion of Variance	0.8	0.2	0.003	6e-04	2e-04
Cumulative Proportion	0.8	1.0	0.999	1e-00	1e+00

**5** independent observables, but only **2** significant dimensions: the first 2 components account for all of the sample variance! The data sit on a plane in a 5-dim. parameter space: this is the Fundamental Plane of elliptical galaxies. Any one variable can be expressed as a combination of any 2 others, within errors.



# PCA Results in More Detail

(This from a slightly different data set ...)

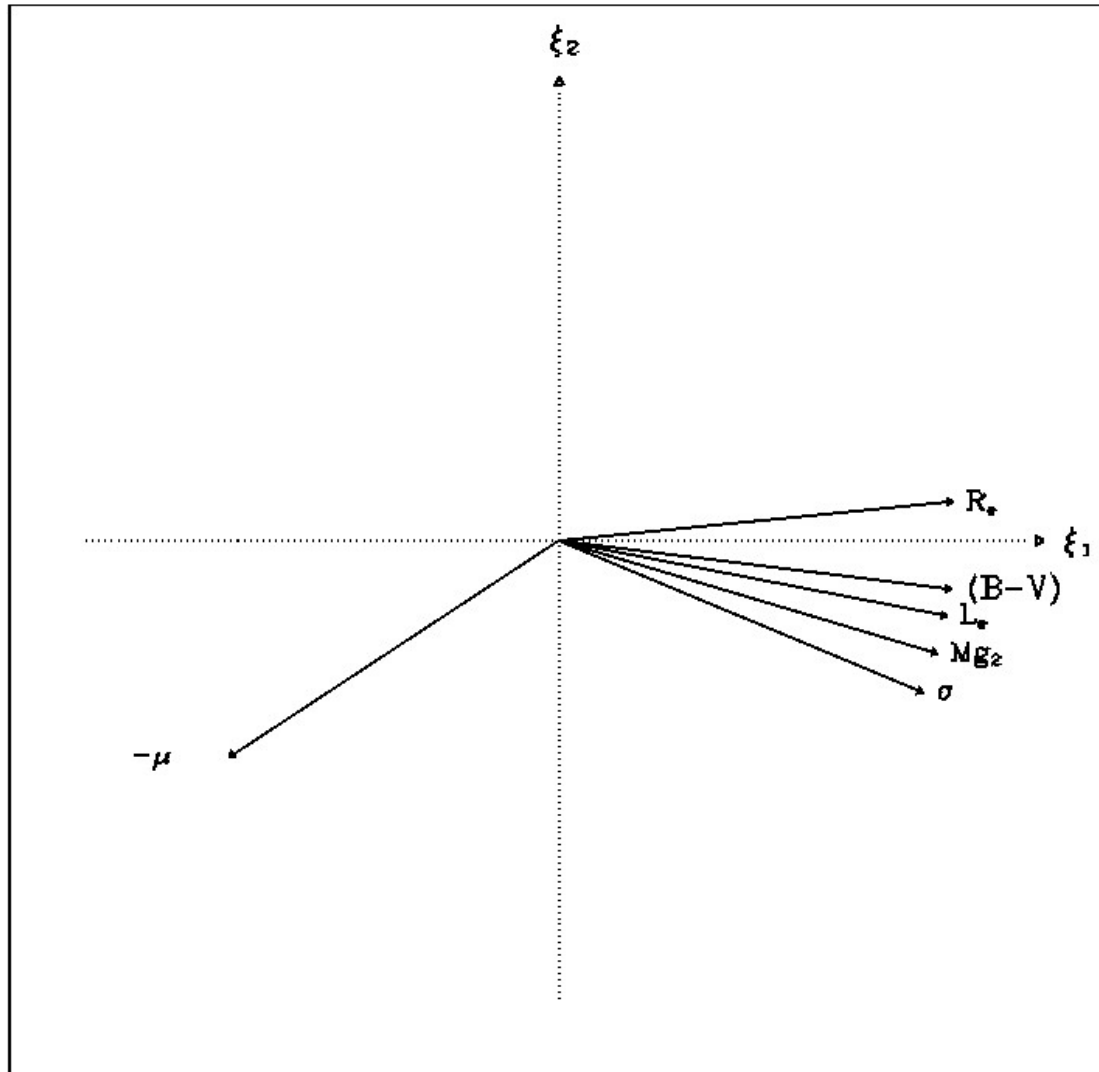
Eigenvalues	As Percentages	Cumul. Percentages
3.1359	62.7189	62.7189
1.3574	27.1482	89.8671
0.3883	7.7670	97.6341
0.1110	2.2199	99.8540
0.0073	0.1460	100.0000

Eigenvectors and projections of parameter axes:

VBLE.	EV-1	EV-2	EV-3	EV-4	EV-5
logRe	-0.5119	0.3443	0.1649	0.1563	0.7535
M_e	0.5291	-0.0310	-0.5158	-0.3689	0.5630
<mu>e	-0.2764	0.6991	-0.4679	-0.3181	-0.3388
sigma	-0.4614	-0.4399	0.1187	-0.7610	0.0194
Mg2	-0.4108	-0.4453	-0.6883	0.3989	-0.0077

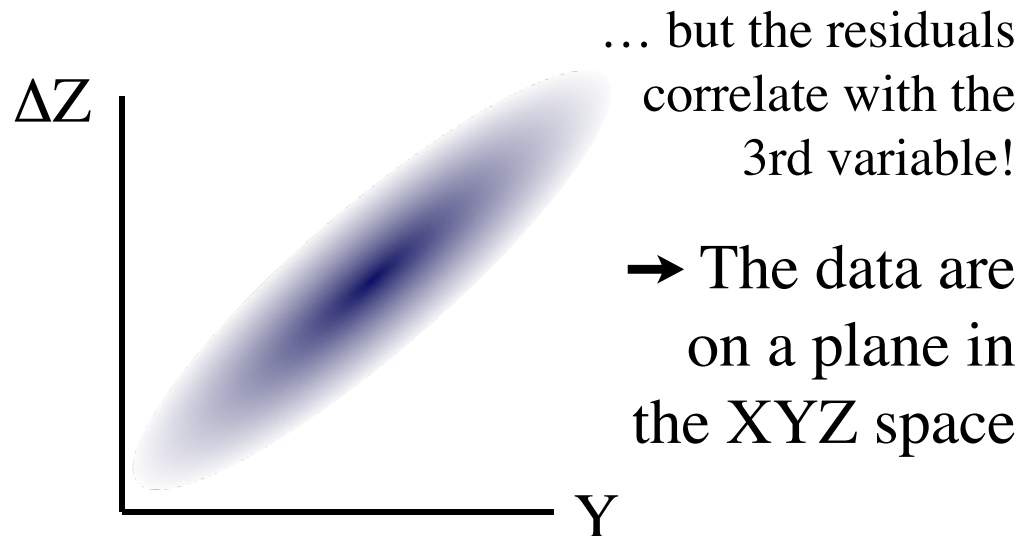
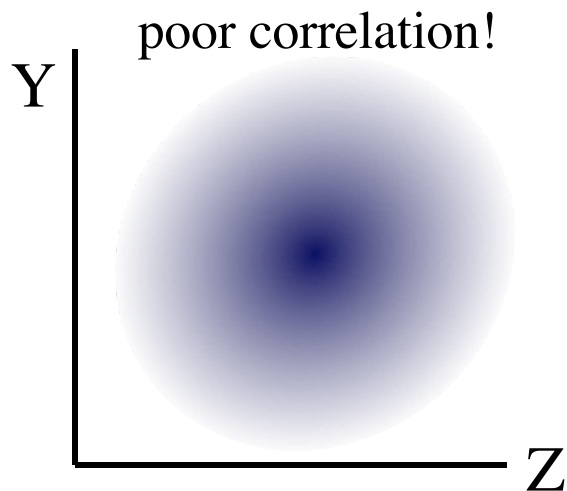
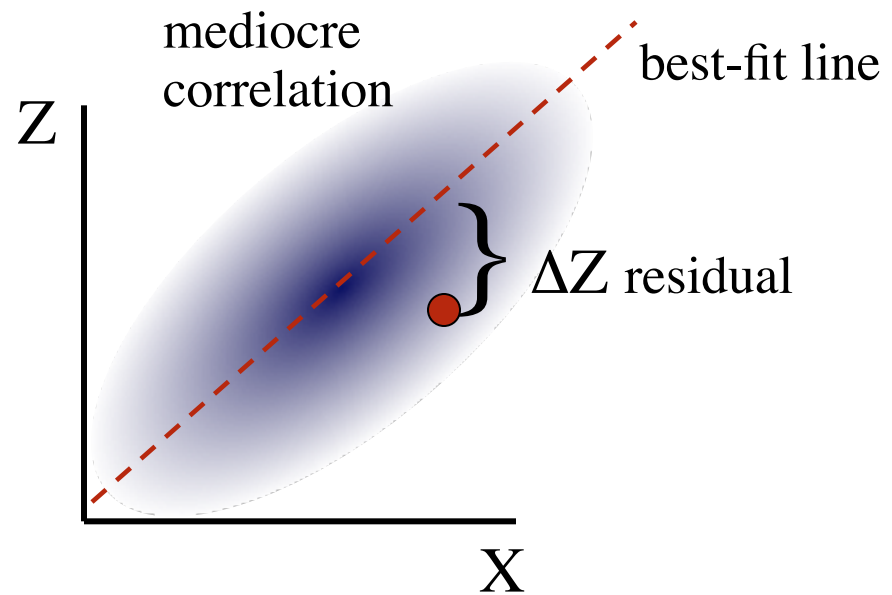
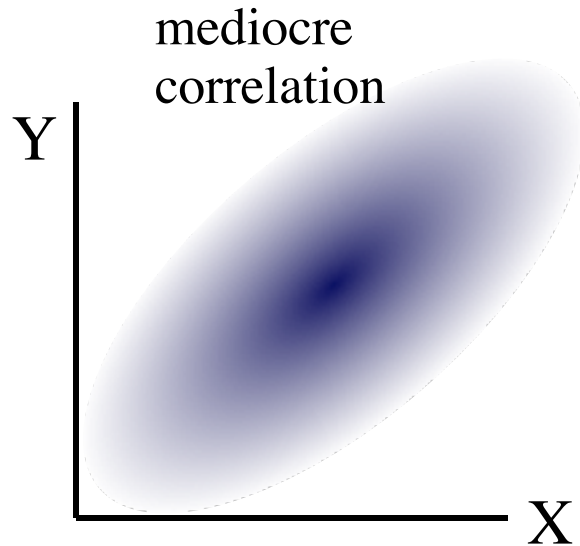


## Now Project the Observable Axes Onto the Plane Defined by the Principal Eigenvectors:



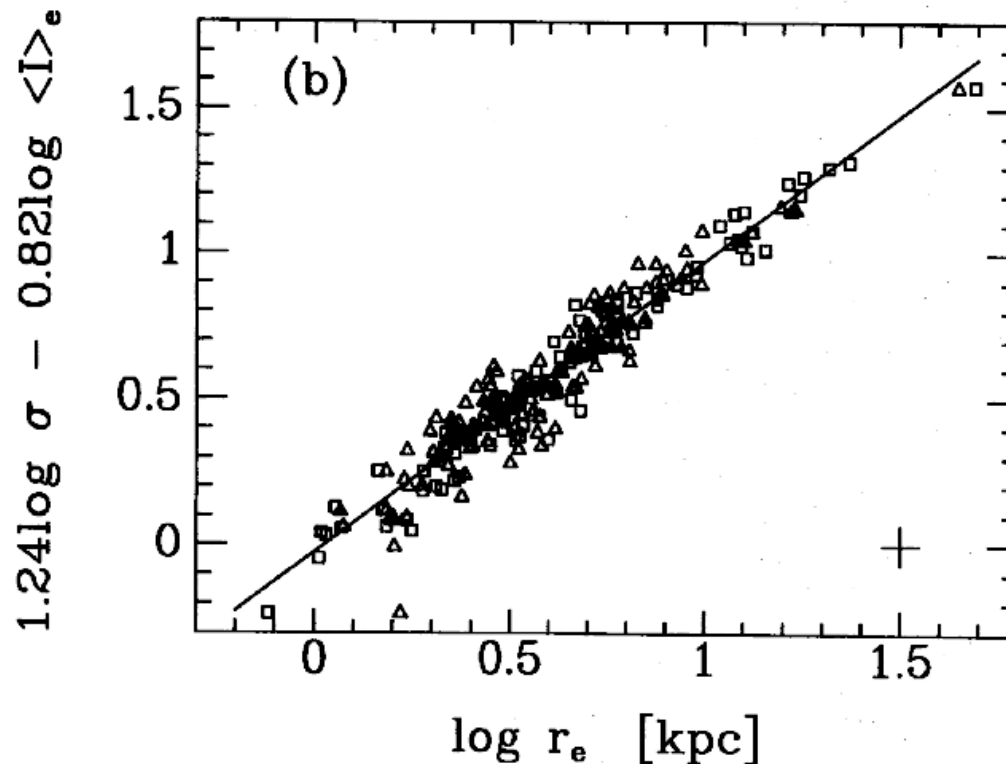
Compare with the correlation matrix: Cosines of angles between parameter axes give the correlation coefficients.

# Another Approach: Correlated Residuals



# Bivariate Correlations in Practice

Once the dimensionality has been established from PCA, one can either derive the optimal bivariate combinations of variables from the PCA coefficients, or optimize the mixing ratios for any two variables vs. a third one (for a 2-dimensional manifold; the generalization to higher dimensional manifolds is obvious).



# Some Data Mining Software & Projects

General data mining software packages:

- Weka (Java): <http://www.cs.waikato.ac.nz/ml/weka/>
- RapidMiner: <http://www.rapidminer.com/>
- Orange: <http://orange.biolab.si/>
- DAME: <http://dame.dsf.unina.it/>

Packages:

- FANN (C): <http://leenissen.dk/fann/wp/>
- SOM (Matlab): <http://www.cis.hut.fi/somtoolbox/>
- Netlab (Matlab):  
<http://www1.aston.ac.uk/eas/research/groups/ncrg/resources/netlab/>
- LibSVM: <http://www.csie.ntu.edu.tw/~cjlin/libsvm/>

# Some Data Mining Software & Projects

Astronomy-specific software and/or user clients:

- AstroWeka: <http://astroweka.sourceforge.net/>
- OpenSkyQuery: <http://www.openskyquery.net/>
- ALADIN: <http://aladin.u-strasbg.fr/>
- MIRAGE: <http://cm.bell-labs.com/who/tkh/mirage/>
- AstroBox: <http://services.china-vo.org/>

Astronomical and/or Scientific Data Mining Projects:

- GRIST: <http://grist.caltech.edu/>
- ClassX: <http://heasarc.gsfc.nasa.gov/classx/>
- LCDM: <http://dposs.ncsa.uiuc.edu/>
- F-MASS: <http://www.itsc.uah.edu/f-mass/>
- NCDM: <http://www.ncdm.uic.edu/>

# Examples of Data Mining Packages: **DAME**

<http://dame.dsf.unina.it/>

- **Web-based**, distributed DM infrastructure specialized in Massive Data Sets exploration with machine learning methods
- Contains tools for classification, regression, clustering, visualization: Neural Networks, SOM, SVM, GA, etc.
- Lots of documentation

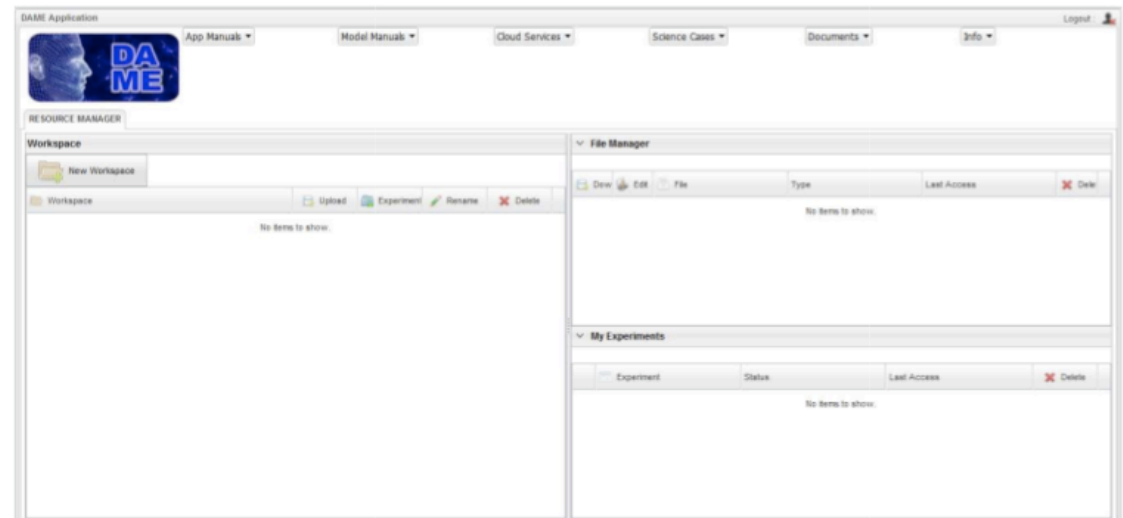


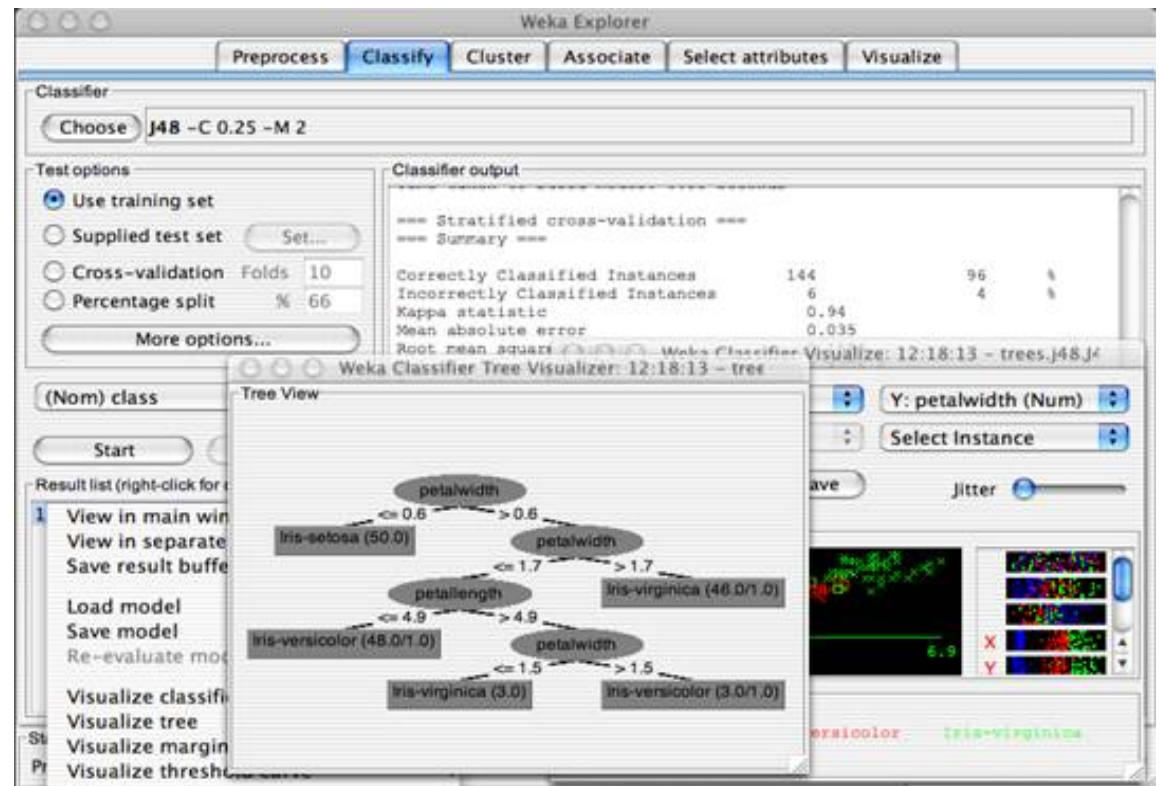
Fig. 5 – The Web Application starting main page (Resource Manager)



# Examples of Data Mining Packages: **Weka**

<http://www.cs.waikato.ac.nz/ml/weka/>

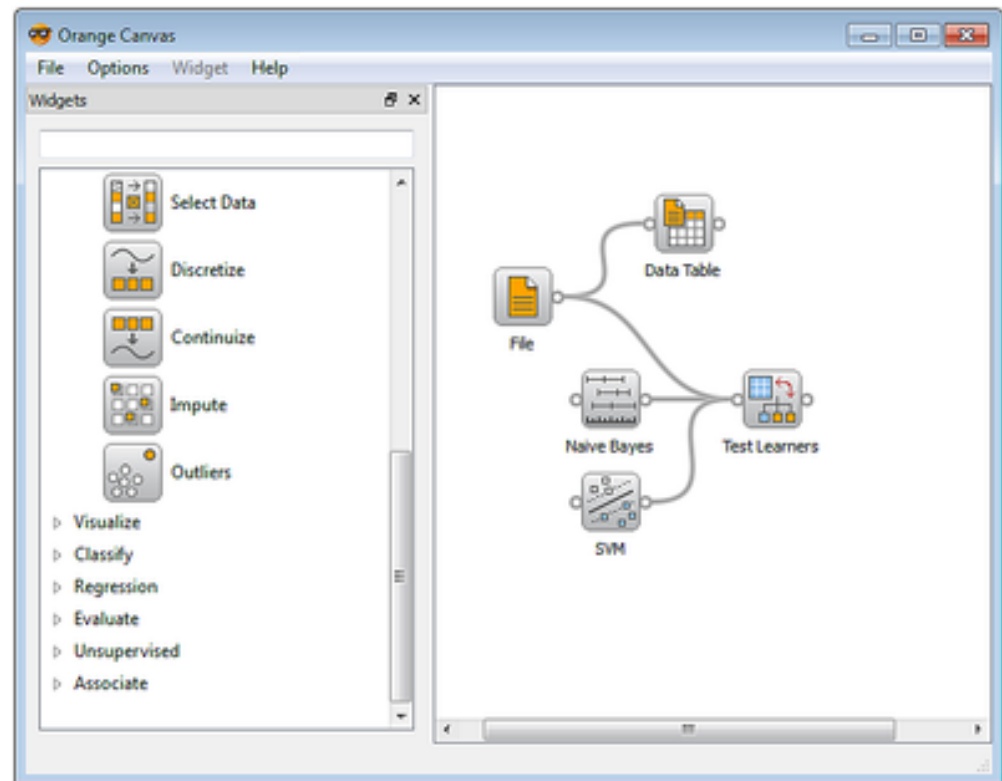
- A collection of open source machine learning algorithms for data mining tasks
- Algorithms can either be applied directly to a dataset or called from your own Java code
- Comes with its own GUI
- Contains tools for data pre-processing, classification, regression, clustering, association rules, and visualization



# Examples of Data Mining Packages: Orange

<http://orange.biolab.si/>

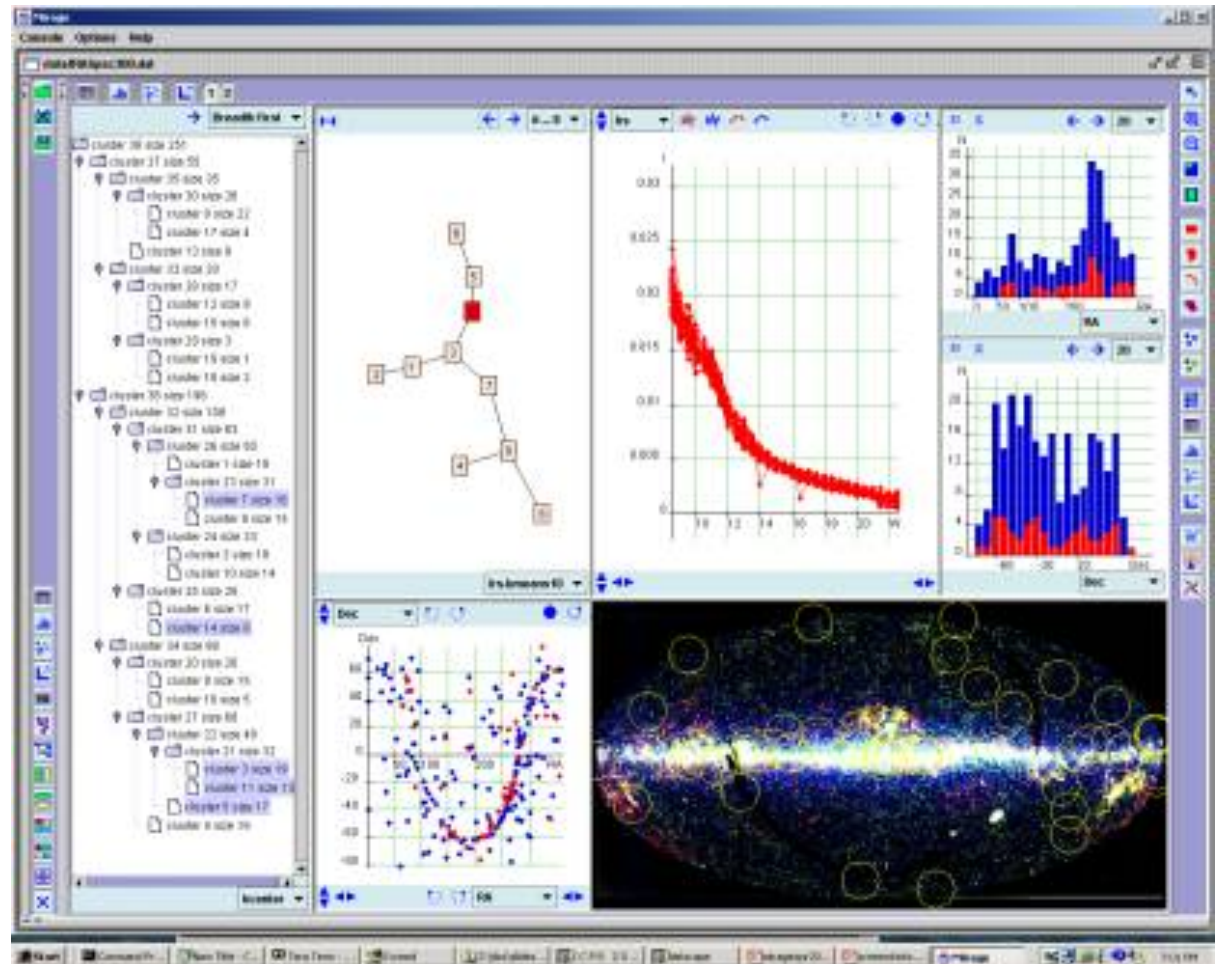
- Open source data visualization and analysis
- Data mining through visual programming or Python scripting
- components for machine learning
- extensions for bioinformatics and text mining
- Available for Windows, Mac, Linux



# Examples of Data Mining Packages: **Mirage**

<http://cm.bell-labs.com/who/tkh/mirage/>

Java Package for  
exploratory data  
analysis (EDA),  
correlation mining,  
and interactive  
pattern discovery.



## Here are some useful books:

- I. Witten E, Frank & M. Hall, *Data Mining: Practical Machine Learning Tools and Techniques, 3rd Ed.*, Morgan Kaufmann, 2011
- P. Janert, *Data Analysis with Open Source Tools*, O'Reilly, 2010
- J. Han, M. Kamber, & J. Pei, *Data Mining: Concepts and Techniques, 2nd Ed.*, Morgan Kaufmann, 2005
- P.-N. Tan, M. Steinbach, & V. Kumar, *Introduction to Data Mining*, Addison Wesley, 2005
- M. Dunham, *Data Mining: Introductory and Advanced Topics*, Prentice-Hall, 2002. ISBN: 9780130888921
- R. J. Roiger & M. W. Geatz, *Data Mining: A Tutorial-Based Primer*, Addison-Wesley, 2002. ISBN: 9780201741285
- ***Lots*** of good links to follow from the class webpage!