Dark Matter Candidates from Particle Physics and Methods of Detection

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Abstract
The identity of dark matter is a question of central importance in both astrophysics and particle physics. In the past, the leading particle candidates were cold and collisionless, and typically predicted missing energy signals at particle colliders. However, recent progress has greatly expanded the list of well-motivated candidates and the possible signatures of dark matter. This review begins with a brief summary of the standard model of particle physics and its outstanding problems. I then discuss several dark matter candidates motivated by these problems, including weakly interacting massive particles (WIMPs), superWIMPs, light gravitinos, hidden dark matter, sterile neutrinos, and axions. For each of these, I critically examine the particle physics motivations and present their expected production mechanisms, basic properties, and implications for direct and indirect detection, particle colliders, and astrophysical observations. Upcoming experiments will discover or exclude many of these candidates, and progress may open up an era of unprecedented synergy between studies of the largest and smallest observable length scales.
1. INTRODUCTION

The evidence that dark matter is required to make sense of our Universe has been building for some time. In 1933, Fritz Zwicky found that the velocity dispersion of galaxies in the Coma cluster of galaxies was far too large to be supported by the luminous matter (Zwicky 1933). In the 1970s, Vera Rubin and collaborators (Rubin & Ford 1970; Rubin, Thonnard & Ford 1980) and Albert Bosma (1978) measured the rotation curves of individual galaxies and also found evidence for nonluminous matter. This and other “classic” evidence for nonluminous matter (see, e.g., Trimble 1987) has now been supplemented by data from weak (Refregier 2003) and strong (Tyson, Kochanski & Dell’Antonio 1998) lensing, hot gas in clusters (Lewis, Buote & Stocke 2003), the Bullet Cluster (Clowe et al. 2006), Big Bang nucleosynthesis (BBN) (Fields & Sarkar 2008), further constraints from large scale structure (Allen et al. 2003), distant supernovae (Riess et al. 1998, Perlmutter et al. 1999), and the cosmic microwave background (CMB) (Komatsu et al. 2010).

Together, these data now provide overwhelming evidence for the remarkable fact that not only is there nonluminous matter in our Universe, but most of it is not composed of baryons or any of the other known particles. Current data imply that dark matter is five times more prevalent than normal matter and accounts for about a quarter of the Universe. More precisely, these data constrain the energy densities of the Universe in baryons (B), nonbaryonic dark matter (DM), and dark energy (Λ) to be (Komatsu et al. 2010), respectively,

\[ \Omega_B \simeq 0.0456 \pm 0.0016, \]  
\[ \Omega_{DM} \simeq 0.227 \pm 0.014, \]  
\[ \Omega_{\Lambda} \simeq 0.728 \pm 0.015. \]  

Despite this progress, all of the evidence for dark matter noted above is based on its gravitational interactions. Given the universality of gravity, this evidence does little to pinpoint what dark matter is. At the same time, the identity of dark matter has far-reaching implications: In astrophysics, the properties of dark matter determine how structure forms and impact the past and future evolution of the Universe; in particle physics, dark matter is the leading empirical evidence for new particles, and there are striking hints that it may be linked to attempts to understand electroweak symmetry breaking, the leading puzzle in the field today. The identity of dark matter is therefore of central importance in both fields and ties together studies of the Universe at both the largest and smallest observable length scales.

This review examines some of the leading dark matter candidates and their implications for experiments and observatories. The wealth of recent cosmological data does constrain some dark matter properties, such as its self-interactions and its temperature at the time of matter-radiation equality. Nevertheless, it is still not at all difficult to invent new particles that satisfy all the constraints, and there are candidates motivated by minimalism, particles motivated by possible experimental anomalies, and exotic possibilities motivated primarily by the desire of clever iconoclasts to highlight how truly ignorant we are about the nature of dark matter.

Here I focus on dark matter candidates that are motivated not only by cosmology, but also by robust problems in particle physics. For this reason, this review begins with a brief summary of the standard model of particle physics, highlighting its basic features and some of its problems. Particle physics provides strong motivation for new particles, and in many cases, these particles have just the right properties to be dark matter. Many of them predict signals that are within reach of current and near future experiments. Unusual predictions for astrophysics emerge, and cold and collisionless dark matter is far from a universal prediction, even for candidates with impeccable particle physics credentials. At the same time, even in favorable cases, a compelling solution to the
Table 1  Summary of dark matter particle candidates, their properties, and their potential methods of detection

<table>
<thead>
<tr>
<th></th>
<th>WIMPs</th>
<th>SuperWIMPs</th>
<th>Light $\tilde{G}$</th>
<th>Hidden DM</th>
<th>Sterile $\nu$</th>
<th>Axions</th>
</tr>
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<tbody>
<tr>
<td>Motivation</td>
<td>GHP</td>
<td>GHP</td>
<td>GHP/NPFP</td>
<td>GHP/NPFP</td>
<td>$v$ Mass</td>
<td>Strong CP</td>
</tr>
<tr>
<td>Naturally Correct</td>
<td>Yes</td>
<td>Yes</td>
<td>No</td>
<td>Possible</td>
<td>No</td>
<td>No</td>
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<tr>
<td>Production Mechanism</td>
<td>Freeze Out</td>
<td>Decay</td>
<td>Thermal</td>
<td>Various</td>
<td>Various</td>
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<tr>
<td>Mass Range</td>
<td>GeV-TeV</td>
<td>GeV-TeV</td>
<td>eV-keV</td>
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<td>keV</td>
<td>$\mu$eV−meV</td>
</tr>
<tr>
<td>Temperature</td>
<td>Cold</td>
<td>Cold/Warm</td>
<td>Cold/Warm</td>
<td>Cold/Warm</td>
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<td>Cold</td>
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<td>Collisional</td>
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<tr>
<td>Early Universe</td>
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<tr>
<td>Direct Detection</td>
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<td>$\checkmark\checkmark$</td>
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<td>Indirect Detection</td>
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<td>Particle Colliders</td>
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</tbody>
</table>

The particle physics motivations are discussed in Section 2.2; GHP and NPFP are abbreviations for the gauge hierarchy problem and new physics flavor problem, respectively. In the last five rows, $\checkmark\checkmark$ denotes detection signals that are generic for this class of dark matter candidate and $\checkmark$ denotes signals that are possible, but not generic. “Early Universe” includes phenomena such as BBN (Big Bang nucleosynthesis) and the CMB (cosmic microwave background); “Direct Detection” implies signatures from dark matter scattering off normal matter in the laboratory; “Indirect Detection” implies signatures of late time dark matter annihilation or decay; and “Particle Colliders” implies signatures of dark matter or its progenitors produced at colliders, such as the Large Hadron Collider (LHC). See the text for details.

The standard model problem will not be easy to achieve and will likely rely on synergistic progress along many lines of inquiry.

An outline of this review is provided by Table 1, which summarizes the dark matter candidates discussed here, along with their basic properties and opportunities for detection.

2. THE STANDARD MODEL OF PARTICLE PHYSICS

The standard model (SM) of particle physics is a spectacularly successful theory of elementary particles and their interactions. For a brief, pedagogical introduction, see, e.g., Herrero (1998). At the same time, it has deficiencies, and the open questions raised by the SM motivate many of the leading dark matter candidates and provide guidance for dark matter searches. I begin here with a brief review of the SM’s basic features and open problems, focusing on those that are most relevant for dark matter.

2.1. Particles

The particles of the SM are shown in Figure 1. They may be divided into three categories:

- **Spin 1/2 Fermions.** These matter particles include six flavors of quarks (up, down, charm, strange, bottom, and top), three flavors of charged leptons (electrons, muons, and taus), and three flavors of neutral leptons (the electron, muon, and tau neutrinos). These are grouped into three generations, as indicated in Figure 1.

- **Spin 1 Gauge Bosons.** These force-carrying particles include the photon $\gamma$, which mediates electromagnetism; eight gluons $g$, which mediate the strong force; and the $W$ and $Z$ gauge bosons, which mediate the weak interactions. The photon and gluons are massless, but the $W$ and $Z$ have masses 80 GeV and 91 GeV, respectively.

- **Spin 0 Higgs Boson.** The SM Higgs particle is a spin 0 boson. Although the Higgs boson has not yet been discovered, its mass is constrained by a variety of collider results. Assuming the SM, null results from direct searches at the LEP $e^+e^-$ collider require $m_H > 114.4$ GeV.
Figure 1
The particles of the standard model, represented by circles whose areas are proportional to their masses. The photon and gluon are massless. The Higgs boson has not yet been discovered—its mass has been taken in the allowed range of $114.4 \text{ GeV} < m_h < 186 \text{ GeV}$.

(LEP Higgs Boson Working Group 2003). Given this constraint, precision measurements of electroweak observables at LEP require $m_h < 186 \text{ GeV}$ (LEP Electroweak Working Group 2009). In addition, the Tevatron $p\bar{p}$ collider, currently running, excludes the region $162 \text{ GeV} < m_h < 166 \text{ GeV}$ (Aaltonen et al. 2010a). These bounds may be relaxed in extensions of the SM, but even in such theories, very general arguments require $m_h \lesssim 1 \text{ TeV}$ (see, e.g., Reina 2005).

None of these SM particles is a good dark matter candidate. Most of the matter particles are unstable, with lifetimes far shorter than the age of the Universe. The remaining particles are the six lightest: the electron, the up and down quarks, which may form stable protons and neutrons in nuclei, and the three neutrinos. Electrons may contribute significantly to dark matter only if they are neutralized through binding with protons, but protons (and neutrons) contribute to the baryonic energy density $\Omega_B$, which is too small to be all of dark matter. In addition, current upper bounds on neutrino masses from particle physics and cosmology imply that the neutrino relic density $\Omega_\nu \simeq \sum m_\nu/47 \text{ eV} \lesssim 0.012$ (Komatsu et al. 2010). The evidence for dark matter therefore requires particles beyond the SM.

2.2. Problems
In addition to the need for dark matter, other problems motivate physics beyond the SM. These problems are of two types. The first and most severe are experimental data that the SM cannot explain; at present, aside from the existence of dark matter, these are confined to the neutrino sector and are described in Section 2.2.3. The second are experimental data that can be explained, but only for seemingly unnatural choices of parameters. All of the remaining problems are of this type.

2.2.1. The gauge hierarchy problem. The gauge hierarchy problem is the question of why the physical Higgs boson mass $m_h$ is so small. What is the natural value for $m_h$? Three fundamental constants are known: the speed of light $c$, Planck’s constant $h$, and Newton’s gravitational constant $G_N$. One combination of these has dimensions of mass, the Planck mass $M_{Pl} \equiv \sqrt{hc/G_N} \simeq 1.2 \times 10^{19} \text{ GeV}$. We therefore expect dimensionful parameters to be either 0, if enforced by a symmetry, or of the order of $M_{Pl}$. In the SM, electroweak symmetry is broken, and the Higgs boson mass is nonzero. The gauge hierarchy problem is the question of why $m_h \sim 100 \text{ GeV} \ll M_{Pl}$. 

\begin{align*}
G_N: & \text{ Newton’s gravitational constant} \\
M_{Pl}: & \text{ Planck mass} \simeq 1.2 \times 10^{19} \text{ GeV}
\end{align*}
This problem is exacerbated in the SM by quantum corrections. The physical mass of the SM Higgs boson is \( m_h^2 = m^2_{1,0} + \Delta m^2_h \), where \( m^2_{1,0} \) is the tree-level mass, and

\[
\Delta m^2_h \sim \frac{\lambda^2}{16\pi^2} \int \frac{d^4 p}{p^2} \sim \frac{\lambda^2}{16\pi^2} \Lambda^2 \tag{4}
\]

is the quantum correction resulting from loop-level diagrams, where the integral is over the momenta of particles in the loops. The parameter \( \lambda \) is an \( O(1) \) dimensionless coupling, and \( \Lambda \) is the energy scale at which the SM is no longer a valid description of nature. Because \( \Delta m^2_h \) is proportional to \( \Lambda^2 \), it is natural to expect the Higgs mass to be pulled up to within an order of magnitude of \( \Lambda \) by quantum corrections. In the SM with \( \Lambda \sim M_{P\!P} \), this implies that \( m^2_{1,0} \) and \( \Delta m^2_h \) must cancel to 1 part in \( 10^{16} \) to yield the correct physical Higgs mass, which is hardly reasonable.

The gauge hierarchy problem may be eliminated if \( \Lambda \lesssim 1 \text{ TeV} \), implying new physics at the weak scale \( m_{\text{weak}} \sim 10 \text{ GeV} - \text{TeV} \). Alternatively, the Higgs boson may not be a fundamental scalar, but in this case, too, its structure requires new physics at the weak scale (Hill & Simmons 2003). For these reasons, every attempt to ameliorate the gauge hierarchy problem so far has implied new particles with mass around \( m_{\text{weak}} \). The gauge hierarchy problem is the leading motivation for dark matter candidates, such as WIMPs and superWIMPs, weakly and superweakly interacting massive particles (respectively), that are the topics of Sections 3 and 4 below.

2.2.2. The new physics flavor problem. The gauge hierarchy problem implies new particles with mass around \( m_{\text{weak}} \). Such particles typically create many new problems, however, because they may violate baryon number, lepton number, flavor, or CP, where C and P are the discrete transformations of charge conjugation and parity, respectively. These symmetries are either beautifully preserved or violated only slightly in the SM, but there is no guarantee that new \( m_{\text{weak}} \) particles will preserve them. This set of problems is collectively known as the new physics flavor problem.

The new physics flavor problem implies that not all solutions to the gauge hierarchy problem are equally elegant. For example, among supersymmetric theories, it implies that those that naturally predict very heavy squarks and sleptons, or those that predict squarks and sleptons that are highly degenerate across different generations, are favored, because these naturally suppress flavor-changing neutral currents below current constraints. This problem has implications for the direct detection of WIMPs, as discussed in Section 3.3, and motivates light gravitino dark matter, reviewed in Section 5, and some of the hidden sector dark matter models described in Section 6.

2.2.3. The neutrino mass problem. Fermion masses are described in quantum field theories by terms that couple left- and right-handed fields together. In the SM, however, there are no right-handed neutrino fields, and so the SM predicts that all neutrinos are massless. The observation of neutrino flavor oscillations (Fukuda et al. 1998, Ahmad et al. 2002), however, implies that the three neutrinos are nondegenerate, and so at least two are massive. Neutrino masses and mixing provide the most direct and compelling evidence that the SM of particle physics is incomplete, and this problem motivates sterile neutrino dark matter, discussed in Section 7.

2.2.4. The strong CP problem. The SM Lagrangian includes the term

\[ g_3^i (\theta_i / (32\pi^2))\epsilon^{\mu\nu\rho\sigma} G^i_{\mu\nu} G^i_{\rho\sigma}, \]

where \( g_3^i \) is the coupling of the strong interactions, \( \theta_i \) is an angle parameter, \( \epsilon^{\mu\nu\rho\sigma} \) is the totally antisymmetric 4-index tensor, and \( G^i_{\mu\nu} \) is the gluon field strength. This term contributes to CP-violating, flavor-conserving observables, such as the electric dipole moment (EDM) of the neutron. For \( \theta_i \sim 1 \), one expects \( d_e \sim 10^{-26} \text{ e cm} \). The neutron EDM has not yet been observed, but current constraints already imply \( d_e < 2.9 \times 10^{-26} \text{ e cm} \).
(Baker et al. 2006). This is therefore a fine-tuning problem of 1 part in $10^{10}$, and it motivates axions as dark matter candidates, to be discussed in Section 8.

### 2.2.5. Other problems.

In addition to the outstanding problems discussed above, there are other open questions raised by the SM. The SM flavor problem, distinct from the new physics flavor problem, is the puzzle of why the fermion masses have such different values, as evident in Figure 1. The grand unification problem is the problem of trying to understand the strong, weak, and electromagnetic interactions as different manifestations of a single underlying force. In addition, at any given time there are always experimental anomalies, measurements that do not agree with SM predictions. At present, the most compelling and persistent discrepancy is in the anomalous magnetic moment of the muon, which disagrees with the SM prediction at the level of $3.4\sigma$ (Hagiwara et al. 2007). Although the problems described in this paragraph do not typically motivate dark matter candidates on their own, they do sometimes play a supporting role, as discussed below.

Finally, note that $m_{h0}$ is only one of two dimensionful parameters in the SM: There is also the term $\lambda^4$, which contributes to dark energy or the cosmological constant. Equation 3 implies that the total energy density in dark energy is $\Lambda \simeq (2.76 \text{ meV})^4$. If the natural value of $\Lambda$ is $M_{\text{Pl}}^4$, it must cancel other contributions to 1 part in $10^{122}$, a fine-tuning that dwarfs even the gauge hierarchy problem. This is the cosmological constant problem. Although one might hope for a unified solution to the cosmological constant and dark matter problems, at present there is little indication that they are related, and I assume they are decoupled in this review.

### 3. WEAKLY INTERACTING MASSIVE PARTICLES

WIMPs have mass in the range $m_{\text{weak}} \sim 10 \text{ GeV-TeV}$ and tree-level interactions with the $W$ and $Z$ gauge bosons, but not with gluons or photons. WIMPs are the most studied dark matter candidates, as they are found in many particle physics theories, naturally have the correct relic density, and may be detected in many ways. In this Section, I discuss their production through thermal freeze out, the examples of neutralino and Kaluza-Klein dark matter, and their implications for direct detection, indirect detection, and particle colliders.

#### 3.1. Thermal Freeze Out

**3.1.1. The WIMP miracle.** If a WIMP exists and is stable, it is naturally produced with a relic density consistent with that required of dark matter. This tantalizing fact, sometimes referred to as the WIMP miracle, implies that particles that are motivated by the gauge hierarchy problem, a purely microphysical puzzle, are excellent dark matter candidates.

Dark matter may be produced in a simple and predictive manner as a thermal relic of the Big Bang (Zeldovich 1965, Chiu 1966, Steigman 1979, Scherrer & Turner 1986). The evolution of a thermal relic’s number density is shown in Figure 2. Initially the early Universe is dense and hot, and all particles are in thermal equilibrium. The Universe then cools to temperatures $T$ below the dark matter particle’s mass $m_X$, and the number of dark matter particles becomes Boltzmann suppressed, dropping exponentially as $e^{-m_X/T}$. The number of dark matter particles would drop to zero, except that, in addition to cooling, the Universe is also expanding. Eventually, the Universe becomes so large and the gas of dark matter particles becomes so dilute that they cannot find each other to annihilate. The dark matter particles then “freeze out,” with their number asymptotically approaching a constant, their thermal relic density. Note that freeze out, also known as chemical decoupling, is distinct from kinetic decoupling; after thermal freeze out, interactions that change
Figure 2
The comoving number density $Y$ (left) and resulting thermal relic density (right) of a 100-GeV, $P$-wave annihilating dark matter particle as a function of temperature $T$ (bottom) and time $t$ (top). The solid gray contour is for an annihilation cross section that yields the correct relic density, and the shaded regions are for cross sections that differ by $10$, $10^2$, and $10^3$ from this value. The dashed gray contour is the number density of a particle that remains in thermal equilibrium.

the number of dark matter particles become negligible, but interactions that mediate energy exchange between dark matter and other particles may remain efficient.

This process is described quantitatively by the Boltzmann equation

$$\frac{dn}{dt} = -3Hn - \langle \sigma A v \rangle (n^2 - n_{eq}^2),$$

where $n$ is the number density of the dark matter particle $X$, $H$ is the Hubble parameter, $\langle \sigma A v \rangle$ is the thermally averaged annihilation cross section, and $n_{eq}$ is the dark matter number density in thermal equilibrium. On the right-hand side of Equation 5, the first term accounts for dilution from expansion. The $n^2$ term arises from processes $XX \rightarrow SM SM$ that destroy $X$ particles, where $SM$ denotes SM particles, and the $n_{eq}^2$ term arises from the reverse process $SM SM \rightarrow XX$, which creates $X$ particles.

The thermal relic density is determined by solving the Boltzmann equation numerically. A rough analysis is highly instructive, however. Defining freeze out to be the time when $n(\sigma A v) = H$, we have

$$n_f \sim (m_X T_f)^{3/2} e^{-m_X/T_f} \sim \frac{T_f^3}{M_{Pl}(\sigma A v)},$$

where the subscripts $f$ denote quantities at freeze out. The ratio $x_f \equiv m_X / T_f$ appears in the exponential. It is, therefore, highly insensitive to the dark matter’s properties and may be considered a constant; a typical value is $x_f \sim 20$. The thermal relic density is, then,

$$\Omega_X = \frac{m_X n_0}{\rho_c} = \frac{m_X}{\rho_c} \frac{T_0^3}{T_f^3} n_0 \sim \frac{m_X}{\rho_c} \frac{1}{\rho_c} x_f \frac{T_0^3}{T_f^3} \sim x_f \frac{T_0^3}{M_{Pl}} (\sigma A v)^{-1},$$

$X$: General dark matter candidate
where \( \rho_c \) is the critical density and the subscripts 0 denote present-day quantities. The thermal relic density is insensitive to the dark matter mass \( m_X \) and inversely proportional to the annihilation cross section \( \langle \sigma v \rangle \).

Although \( m_X \) does not enter \( \Omega_X \) directly, in many theories it is the only mass scale that determines the annihilation cross section. On dimensional grounds, then, the cross section can be written

\[
\langle \sigma v \rangle = k \frac{g_{\text{weak}}^4}{16\pi^2m_X^2}(1 + v^2),
\]

where the factor \( v^2 \) is absent or present for \( S \)- or \( P \)-wave annihilation, respectively, and terms higher-order in \( v \) have been neglected. The constant \( g_{\text{weak}} \approx 0.65 \) is the weak interaction gauge coupling, and \( k \) parameterizes deviations from this estimate.

With this parameterization, given a choice of \( k \), the relic density is determined as a function of \( m_X \). The results are shown in Figure 3. The width of the band comes from considering both \( S \)- and \( P \)-wave annihilation, and from letting \( k \) vary from 1/2 to 2. A particle that makes up all of dark matter is predicted to have mass in the range \( m_X \sim 100 \text{ GeV} \)–1 \( \text{TeV} \); a particle that makes up 10\% of dark matter has mass \( m_X \sim 30 \text{ GeV} \)–300 \text{ GeV}. This is the WIMP miracle: Weak-scale particles make excellent dark matter candidates. I have neglected many details here, and there are models for which \( k \) lies outside our illustrative range, sometimes by as much as an order of magnitude or two. Nevertheless, the WIMP miracle implies that many models of particle physics easily provide viable dark matter candidates, and it is at present the strongest reason to expect that central problems in particle physics and astrophysics may in fact be related. Note also that, for those who find the aesthetic nature of the gauge hierarchy problem distasteful, the WIMP miracle independently provides a strong motivation for new particles at the weak scale.

### 3.1.2. Stability and the Large Electron-Positron Collider’s cosmological legacy.

The entire discussion of Section 3.1.1 assumes that the WIMP is stable. This might appear to be an unreasonable expectation; after all, all particles heavier than 1 \text{ GeV} in the SM decay on timescales far shorter than the age of the Universe.

In fact, however, there are already indications that if new particles exist at the weak scale, at least one of them should be stable. This is the cosmological legacy of LEP, the Large
Electron-Positron Collider that ran from 1989–2000. Generically, new particles introduced to solve the gauge hierarchy problem would be expected to induce new interactions,

\[
\text{SM SM} \rightarrow \text{NP} \rightarrow \text{SM SM},
\]

where SM and NP denote standard model and new particles, respectively. If the new particles are heavy, they cannot be produced directly, but their effects may nevertheless be seen as perturbations on the properties of SM particles. LEP, along with the Stanford Linear Collider, looked for the effects of these interactions and found none, constraining the mass scale of new particles to be above \(\sim 1-10 \text{ TeV} \), depending on the SM particles involved (see, e.g., Barbieri & Strumia 1999).

At the same time, to solve the gauge hierarchy problem, the new particles cannot be decoupled completely. At the very least, the new particles should modify the quantum corrections to the Higgs boson mass given in Equation 4. This implies that they must interact with the Higgs boson through couplings,

\[
h \leftrightarrow \text{NP NP},
\]

and their masses should not be significantly higher than \(m_{\text{weak}} \sim 10 \text{ GeV–TeV} \).

These apparently conflicting demands may be reconciled if there is a conserved discrete parity that requires all interactions to involve an even number of new particles [Cheng & Low 2003; J. Wudka, unpublished data (hep-ph/0307339)]. Such a conservation law would eliminate the problematic reactions of Equation 9, while preserving the desired interactions of Equation 10. As a side effect, the existence of a discrete parity implies that the lightest new particle cannot decay. The lightest new particle is therefore stable, as required for dark matter. Note that pair annihilation of dark matter particles is still allowed. The prototypical discrete parity is \(R\)-parity, proposed for supersymmetry long before the existence of LEP bounds (Farrar & Fayet 1978). However, the existence of LEP constraints implies that any new theory of the weak scale must confront this difficulty. The required discrete parity may be realized in many ways, depending on the new physics at the weak scale; an example in extra dimensions is given in Section 3.2.2.

### 3.1.3. Implications for detection

The WIMP miracle not only provides a model-independent motivation for dark matter at the weak scale, but it also has strong implications for how dark matter might be detected. For WIMPs \(X\) to have the observed relic density, they must annihilate to other particles. Assuming that these other particles are SM particles, the necessity of \(XX \rightarrow \text{SM SM}\) interactions suggests the following three promising strategies for dark matter detection:

- **Indirect detection:** If dark matter annihilated in the early Universe, it must also annihilate now through \(XX \rightarrow \text{SM SM}\), and the annihilation products may be detected.
- **Direct detection:** Dark matter can scatter off normal matter through \(X \text{SM} \rightarrow X \text{SM} \) interactions, depositing energy that may be observed in sensitive, low-background detectors.
- **Particle colliders:** Dark matter may be produced at particle colliders through \(\text{SM SM} \rightarrow XX\). Such events are undetectable, but are typically accompanied by related production mechanisms, such as \(\text{SM SM} \rightarrow XX + \{\text{SM}\}\), where \(\{\text{SM}\}\) denotes one or more SM particles. These events are observable and provide signatures of dark matter at colliders.

It is important to note that the WIMP miracle not only implies that such dark matter interactions must exist, it also implies that the dark matter–SM interactions must be efficient; although WIMPs may not be a significant amount of the dark matter, they certainly cannot have an energy density more than \(\Omega_{\text{DM}}\). Cosmology therefore provides lower bounds on interaction rates. This fact provides highly motivated targets for a diverse array of experimental searches that may be able to detect WIMPs and constrain their properties.
To summarize, viable particle physics theories designed to address the gauge hierarchy problem naturally (i) predict new particles with mass $\sim m_{\text{weak}}$ that (ii) are stable and (iii) have the thermal relic densities required to be dark matter. The convergence of particle physics and cosmological requirements for new states of matter has motivated many new proposals for dark matter. In the following section, I discuss some prominent examples.

### 3.2. Candidates

#### 3.2.1. Neutralinos.

The gauge hierarchy problem is most elegantly solved by supersymmetry. In supersymmetric extensions of the SM, every SM particle has a new, as-yet-undiscovered partner particle, which has the same quantum numbers and gauge interactions, but differs in spin by 1/2. The introduction of new particles with opposite spin-statistics from the known ones supplements the SM quantum corrections to the Higgs boson mass with opposite sign contributions, modifying Equation 4 to

$$
\Delta m^2 \sim \frac{\lambda^2}{16\pi^2} \int_{-\Lambda}^{\Lambda} \frac{d^4 p}{p^2} - \frac{\lambda^2}{16\pi^2} \int_{-\Lambda}^{\Lambda} \frac{d^4 p}{p^2} \sim \frac{\lambda^2}{16\pi^2} (m_{\text{SUSY}}^2 - m_{\text{SM}}^2) \ln \frac{\Lambda}{m_{\text{SUSY}}},
$$

(11)

where $m_{\text{SM}}$ and $m_{\text{SUSY}}$ are the masses of the SM particles and their superpartners. For $m_{\text{SUSY}} \sim m_{\text{weak}}$, this is at most an $O(1)$ correction, even for $\Lambda \sim M_{\text{Pl}}$. This by itself stabilizes, but does not solve, the gauge hierarchy problem; one must also understand why $m_{\text{SUSY}} \sim m_{\text{weak}} \ll M_{\text{Pl}}$. There are, however, a number of ways to generate such a hierarchy; for a review, see Shadmi & Shirman (2000). Given such a mechanism, the relation of Equation 11 implies that quantum effects will not destroy the hierarchy, and the gauge hierarchy problem may be considered truly solved.

Not surprisingly, the doubling of the SM particle spectrum has many implications for cosmology. For dark matter, it is natural to begin by listing all the new particles that are electrically neutral. For technical reasons, supersymmetric models require two Higgs bosons. The neutral supersymmetric particles are then

- Spin 3/2 Fermion: Gravitino $\tilde{G}$
- Spin 1/2 Fermions: $\tilde{B}, \tilde{W}, \tilde{H}_u, \tilde{H}_d \rightarrow$ Neutralinos $\chi_1, \chi_2, \chi_3, \chi_4$
- Spin 0 Scalars: Sneutrinos $\tilde{\nu}_e, \tilde{\nu}_\mu, \tilde{\nu}_\tau$

As indicated, the neutral spin 1/2 fermions mix to form four mass eigenstates, the neutralinos. The lightest of these, $\chi \equiv \chi_1$, is a WIMP dark matter candidate (Goldberg 1983, Ellis et al. 1984). The sneutrinos are not good dark matter candidates, as both their annihilation and scattering cross sections are large, and so they are underabundant or excluded by null results from direct detection experiments for all masses near $m_{\text{weak}}$ (Falk, Olive & Srednicki 1994; Arina & Fornengo 2007). The gravitino is not a WIMP, but it is a viable and fascinating dark matter candidate, as discussed in Sections 4 and 6.

A general supersymmetric extension of the SM contains many unknown parameters. To make progress, it is typical to consider specific models in which simplifying assumptions unify many parameters, and then study to what extent the conclusions may be generalized. The canonical model for supersymmetric studies is minimal supergravity, which is minimal in the sense that it includes the minimum number of particles and includes a large number of assumptions that
drastically reduce the number of independent model parameters. Minimal supergravity is defined by five parameters:

\[ m_0, M_{1/2}, A_0, \tan \beta, \text{sign}(\mu). \quad (15) \]

The most important parameters are the universal scalar mass \( m_0 \) and the universal gaugino mass \( M_{1/2} \), both defined at the scale of grand unified theories \( m_{\text{GUT}} \approx 2 \times 10^{16} \text{ GeV} \). The assumption of a universal gaugino mass and the choice of \( m_{\text{GUT}} \) are supported by the fact that the three SM gauge couplings unify at \( m_{\text{GUT}} \) in supersymmetric theories (Dimopoulos, Raby & Wilczek 1981). The assumption of scalar mass unification is much more ad hoc, but it does imply highly degenerate squarks and sleptons, which typically satisfies the constraints of the new physics flavor problem. Finally, the parameter \( A_0 \) governs the strength of cubic scalar particle interactions, and \( \tan \beta \) and \( \text{sign}(\mu) \) are parameters that enter the Higgs boson potential. For all but their most extreme values, these last three parameters have much less impact on collider and dark matter phenomenology than \( m_0 \) and \( M_{1/2} \).

In the context of minimal supergravity, the thermal relic density is given in the \((m_0, M_{1/2})\) plane for fixed values of \( A_0, \tan \beta, \) and \( \text{sign}(\mu) \) in Figure 4. Current constraints on \( \Omega_{\chi} \) are highly constraining, essentially reducing the cosmologically favored parameter space by one dimension. The region of parameter space with the correct neutralino relic density is further divided into three regions with distinct properties: the bulk region, the focus point region, and the coannihilation region. Of course, if one considers the full minimal supergravity parameter space, other points in the \((m_0, M_{1/2})\) plane are possible (see, e.g., Trotta et al. 2008); notably, at larger \( \tan \beta \) there is another favored region, known as the funnel region.

Note that for much of the region with \( m_0, M_{1/2} \lesssim 1 \text{ TeV} \), \( \Omega_{\chi} \) is too large. This is because neutralinos, although widely studied, are very special: They are Majorana fermions; that is, they

![Figure 4](https://example.com/figure4.png)

**Figure 4**

Regions of minimal supergravity \((m_0, M_{1/2})\) parameter space for fixed \( A_0 = 0, \tan \beta = 10, \) and \( \mu > 0 \). The green (dark yellow) region is cosmologically favored with \( 0.20 < \Omega_{\chi} < 0.28 \) \((0.2 < \Omega_{\chi} < 0.6)\). The names of cosmologically favored regions (focus point, bulk, and coannihilation) are indicated, along with regions with too much and too little dark matter. The lower right red shaded region is excluded by collider bounds on chargino masses; the upper left red region is excluded by the presence of a stable charged particle. Contours are for neutralino dark matter mass \( m_{\chi} \) in gigaelectronvolts. Adapted from Feng, Matchev & Wilczek (2001).
are their own antiparticles. If the initial state neutralinos are in an S-wave state, the Pauli exclusion principle implies that the initial state has total spin $S = 0$ and total angular momentum $J = 0$. Annihilation to fermion pairs with total spin $S = 1$, such as $\tilde{\chi}_R \tilde{\chi}_R$, is therefore $P$-wave suppressed, with an extra factor of $v^2 \sim 0.1$ in the annihilation cross section. As a result, $\Omega_x$ is typically too large, and the correct $\Omega_x$ is achieved for relatively light neutralinos, as evident in Figure 4.

3.2.2. Kaluza-Klein dark matter. An alternative possibility for new weak-scale physics is extra dimensions. The idea that there may be extra spatial dimensions is an old one, going back at least as far as the work of Kaluza and Klein in the 1920s (Klein 1926). Their original idea is untenable, but it has many modern descendants, of which the closest living relative is universal extra dimensions (UED) (Appelquist, Cheng & Dobrescu 2001).

In UED, all particles propagate in flat, compact extra dimensions of size $10^{-18}$ m or smaller. In the simplest UED model, minimal UED, there is one extra dimension of size $R$ compactified on a circle, with points $y$ and $-y$ identified, where $y$ is the coordinate of the extra dimension. Every SM particle has an infinite number of partner particles, with one at every Kaluza-Klein (KK) level $n$ with mass $\sim nR^{-1}$. In contrast to supersymmetry, these partner particles have the same spin. As a result, UED models do not solve the gauge hierarchy problem; in fact, their couplings become large and nonperturbative at energies far below the Planck scale. The motivation to consider UED models is that they provide an interesting and qualitatively different alternative to supersymmetry, but it assumes that UED are a low-energy approximation to a more complete theory that resolves the gauge hierarchy problem and is well-defined up to the Planck scale.

Minimal UED parameter space is extremely simple, as it is completely determined by only two parameters: $m_h$, the mass of the SM Higgs boson, and $R$, the compactification radius. For the Higgs boson mass, the direct search constraints on the SM also apply in UED and require $m_h > 114.4$ GeV (LEP Higgs Boson Working Group 2003). However, the indirect bounds are significantly weakened by the existence of many levels of KK particles, and require only $m_h < 900$ GeV ($300$ GeV) for $R^{-1} = 250$ GeV (1 TeV) at 90% confidence level (CL) (Appelquist & Yee 2003).

The simplest UED models preserve a discrete parity known as KK parity, which implies that the lightest KK particle (LKP) is stable and a possible dark matter candidate (Cheng, Feng & Matchev 2002; Servant & Tait 2003). The LKP is typically $B^1$, the level 1 partner of the hypercharge gauge boson. The regions of parameter space with the correct $B^1$ thermal relic density have been investigated in a series of increasingly sophisticated studies (Servant & Tait 2003; Burnell & Kribs 2006; Kakizaki, Matsumoto & Senami 2006; Kong & Matchev 2006); the end results are shown in Figure 5. As can be seen, the required LKP mass is $600$ GeV $\lesssim m_B^1 \lesssim 1.4$ TeV, a heavier range than for neutralinos. This is because LKPs annihilation is through S-wave processes, and so is not $P$-wave suppressed, in contrast to neutralinos. Nevertheless, the required dark matter mass is still $\sim 1$ TeV, as expected given the WIMP miracle.

3.2.3. Others. Neutralinos are the prototypical WIMP, and KK dark matter provides an instructive example of WIMPs that differ in important aspects from neutralinos. There are many other examples, however. In the recent years leading up to the start of the Large Hadron Collider (LHC), there has been a proliferation of electroweak theories and an accompanying proliferation of WIMP candidates. These include branons in theories with large extra dimensions (Cembranos, Dobado & Maroto 2003a, b), $T$-odd particles in little Higgs theories (Cheng & Low 2003, Birkedal et al. 2006), and excited states in theories with warped extra dimensions (Agashe & Servant 2004). As with all WIMPs, these are astrophysically equivalent, in that they are
produced through thermal freeze out and are cold and collisionless, but their implications for direct detection, indirect detection, and particle colliders may differ significantly.

### 3.3. Direct Detection

As discussed in Section 3.1.3, WIMP dark matter may be detected by its scattering off normal matter through processes $X \ SM \rightarrow X SM$. Given a typical WIMP mass of $m_X \sim 100$ GeV and WIMP velocity $v \sim 10^{-3}$, the deposited recoil energy is at most $\sim 100$ keV, requiring highly sensitive, low-background detectors placed deep underground. Such detectors are insensitive to very strongly interacting dark matter, which would be stopped in the atmosphere or Earth and would be undetectable underground. However, such dark matter would be seen by rocket and other space-borne experiments or would settle to the core of the Earth, leading to other fascinating and bizarre implications. Taken together, a diverse quilt of constraints now excludes large scattering cross sections for a wide range of dark matter masses (Mack, Beacom & Bertone 2007; Albuquerque & Heros 2010), and we may concentrate on the weak cross section frontier probed by underground detectors.

The field of direct detection is extremely active, with sensitivities increasing by two orders of magnitude in the past decade and bright prospects for continued rapid improvement (Gaitskell 2004, HEPAP/AAAC DMSAG Subpanel 2007). WIMP scattering may be through spin-independent couplings, such as interactions $\bar{X} X \bar{q} q$, or spin-dependent couplings, such as interactions $\bar{X} \gamma^\mu \gamma^5 X \bar{q} \gamma^\nu \gamma^5 q$, which reduce to spin-spin couplings $S_X \cdot S_q$ in the nonrelativistic limit (Goodman & Witten 1985). The current state of affairs is summarized in Figure 6 for spin-independent searches and Figure 7 for spin-dependent searches. These Figures also include scattering cross section predictions for neutralino dark matter. For comparison, the predictions for $B^5$ KK dark matter in UED for both spin-independent and spin-dependent cross sections are given in Figure 8. These Figures assume a Maxwellian velocity distribution and local dark matter density of $\rho = 0.3$ GeV cm$^{-3}$; the impacts of halo modeling and Galactic substructure on direct detection limits have been explored by Green (2002) and Kamionkowski & Koushiappas (2008), respectively.

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**Figure 5**

Regions of minimal universal extra dimensions parameter space with the correct relic density. The light green (medium green) shaded region has $\Omega h^2 = 0.099 \pm 0.020$ (0.010). The dark blue shaded region is excluded because the lightest Kaluza-Klein particle (LKP) is charged. From Kakizaki, Matsumoto & Senami (2006).
For spin-independent scattering, there are both an observed signal from DAMA and null results from many other experiments. Putting aside DAMA for the moment, as can be seen in Figures 6 and 8, current bounds exclude some of the parameter space of supersymmetry and UED, but do not test the bulk of either parameter space. The experiments are improving rapidly, however, and in the coming year, sensitivities to cross sections of $\sigma_{SI} \sim 10^{-45} - 10^{-44}$ cm$^2$ are possible.

How significant will this progress be? As evident in Figure 6, supersymmetry predictions may be arbitrarily small. However, many well-known supersymmetric theories predict $\sigma_{SI} \sim 10^{-44}$ cm$^2$. In general, supersymmetric theories suffer from the new physics flavor problem: the introduction of squarks and sleptons with generic flavor mixing and weak scale masses induces contributions to $K - \bar{K}$ mixing, $\mu \rightarrow e\gamma$, the electric dipole moments of the neutron and electron, and a host of other flavor- or CP-violating observables that badly violate known constraints. One generic solution to this problem is to assume heavy squarks and sleptons, with masses above a TeV, so that they decouple and do not affect low-energy observables. This solution is realized in the focus point region of minimal supergravity, and is also found in many other models with greatly varying motivations (Feng, Matchev & Moroi 2000a,b).

These models have profound implications for dark matter searches. In general, the dominant contributions to neutralino annihilation are $\chi \chi \rightarrow q\bar{q}, l\bar{l}$ through $t$-channel squarks and sleptons,
Upper bounds on spin-dependent weakly interacting massive particle (WIMP)-proton cross sections $\sigma_{SD}$ from CDMS (Ahmed et al. 2009b), COUPP (Behnke et al. 2008), KIMS (Lee et al. 2007), Super-K (Desai et al. 2004), and IceCube (Abbasi et al. 2009), along with preliminary limits from AMANDA (Braun & Hubert 2009) and the projected 10-year sensitivity of IceCube with DeepCore. The shaded regions are predictions for neutralino dark matter in the general minimal supersymmetric standard model with $0.05 < \Omega \chi^2 < 0.20$. From Braun & Hubert (2009).

In the next year or so, then, direct detection should test all supersymmetric scenarios with the correct relic density in which the new physics flavor problem is solved by decoupled squarks and sleptons. So far, direct detection experiments have trimmed a few fingernails off the body of supersymmetry parameter space, but if nothing is seen in the coming few years, it is arms and legs that will have been lopped off.

In addition to the limits described above, experiments by the DAMA Collaboration continue to find a signal in annual modulation (Drukier, Freese & Spergel 1986) with period and maximum at the expected values (Bernabei et al. 2008a). From a theorist’s viewpoint, the DAMA/LIBRA result has been puzzling, because the signal, if interpreted as spin-independent elastic scattering, seemingly implied dark matter masses and scattering cross sections that have been excluded by...
Figure 8
Predicted spin-independent weakly interacting massive particle (WIMP)-nucleon cross sections (yellow shaded, brown lines) and spin-dependent WIMP-proton cross sections (blue shaded, dark blue lines) in units of pb = 10^{-16} cm^2 for B^1 Kaluza-Klein dark matter in universal extra dimensions with a universal KK quark mass m_{B^1}. The predictions are for m_B = 120 GeV and 0.01 \leq r = (m_{B^1} - m_{B^1}) / m_{B^1} \leq 0.5, with contours for specific intermediate r labeled. From Cheng, Feng & Matchev (2002).

other experiments. Inelastic scattering, in which dark matter is assumed to scatter through X SM \rightarrow X' SM, where X' is another new particle that is ∼100 keV heavier than X, has been put forward as one solution (Tucker-Smith & Weiner 2001). More recently, astrophysics (Gondolo & Gelmini 2005) and channeling (Bernabei et al. 2008b, Drobyshevski 2008), a condensed matter effect that effectively lowers the threshold for crystalline detectors, have been proposed as possible remedies to allow elastic scattering to explain DAMA without violating other constraints. If these indications are correct, the favored parameters are m_X ∼ 1–10 GeV and \sigma_{SI} ∼ 10^{-41}–10^{-39} cm^2. This interpretation is supported by unexplained events recently reported by the Coherent Germanium Neutrino Technology (CoGeNT) direct detection search, which, if interpreted as a dark matter signal, are best fit by dark matter with m_X ∼ 9 GeV and \sigma_{SI} ∼ 6.7 \times 10^{-5} pb (Aalseth et al. 2010). This mass is lower than typically expected for WIMPs, but even massless neutralinos are allowed if one relaxes the constraint of gaugino mass unification (Dreiner et al. 2009). The cross section is, however, very large; it may be achieved in corners of minimal supersymmetric standard model (MSSM) parameter space (Bottino et al. 2008), but is more easily explained in completely different frameworks, such as those discussed in Section 6.

Spin-dependent scattering provides an independent method to search for dark matter. At the moment, the leading direct detection experiments, such as Cryogenic Dark Matter Search (CDMS), Chicagoland Observatory for Underground Particle Physics (COUPP), and the Korea Invisible Mass Search (KIMS), are less promising in terms of probing the heart of supersymmetric and UED WIMP parameter space, as seen in Figures 7 and 8. In addition, given some fairly reasonable assumptions, indirect detection experiments looking for dark matter annihilation to neutrinos in the Sun provide more stringent constraints, as is discussed in the following section.
3.4. Indirect Detection

After freeze out, dark matter pair annihilation becomes greatly suppressed. However, even if its impact on the dark matter relic density is negligible, dark matter annihilation continues and may be observable. Dark matter may therefore be detected indirectly: dark matter pair-annihilates somewhere, producing something, which is detected somehow. There are many indirect detection methods being pursued. Their relative sensitivities are highly dependent on what WIMP candidate is being considered, and the systematic uncertainties and difficulties in determining backgrounds also vary greatly from one method to another.

Searches for neutrinos are unique among indirect searches in that they are, given certain assumptions, probes of scattering cross sections, not annihilation cross sections, and so compete directly with the direct detection searches described in Section 3.3. The idea behind neutrino searches is the following: When WIMPs pass through the Sun or the Earth, they may scatter and be slowed below escape velocity. Once captured, they then settle to the center, where their densities and annihilation rates are greatly enhanced. Although most of their annihilation products are immediately absorbed, neutrinos are not. Some of the resulting neutrinos then travel to the surface of the Earth, where they may convert to charged leptons through $\nu_q \rightarrow \ell q'$, and the charged leptons may be detected.

The neutrino flux depends on the WIMP density, which is determined by the competing processes of capture and annihilation. If $N$ is the number of WIMPs captured in the Earth or Sun, $N = C - \dot{A} N^2$, where $C$ is the capture rate and $\dot{A}$ is the total annihilation cross section times relative velocity per volume. The present WIMP annihilation rate is, then, $\Gamma_A = \dot{A} N^2/2 = C \tanh^2(\sqrt{CA t_\odot})/2$, where $t_\odot \simeq 4.5$ Gyr is the age of the Solar System. For most WIMP models, a very large collecting body such as the Sun has reached equilibrium, and so $\Gamma_A \approx C/2$. The annihilation rate alone does not completely determine the differential neutrino flux—one must also make assumptions about how the neutrinos are produced. However, if one assumes, say, that WIMPs annihilate to $b \bar{b}$ or $W^+ W^-$, which then decay to neutrinos, as is true in many neutralino models, the neutrino signal is completely determined by the capture rate $C$, that is, the scattering cross section.

Under fairly general conditions, then, neutrino searches are directly comparable to direct detection. The Super-Kamioka Nucleon Decay Experiments (Super-Kamiokande), IceCube Neutrino Observatory (IceCube), and Antarctic Muon and Neutrino Detector Array (AMANDA) collaborations have looked for excesses of neutrinos from the Sun with energies in the range $10 \text{ GeV} \lesssim E_\nu \lesssim 1 \text{ TeV}$. Given the assumptions specified above, their null results provide the leading bounds on spin-dependent scattering cross sections, as seen in Figure 7. These experiments are just beginning to probe relevant regions of supersymmetric and UED parameter space.

Neutrino searches are also sensitive to spin-independent cross sections. For typical WIMP masses, they are not competitive with direct searches, but future neutrino searches at Super-Kamiokande may have lower thresholds and so provide leading bounds on low-mass WIMPs. In this way, Super-Kamiokande may test the DAMA and CoGeNT signal regions at high $\sigma_{\text{SI}}$ and $m_X \sim 1$–10 GeV (Feng et al. 2009b; Hooper et al. 2009; Kumar, Learned & Smith 2009).

In addition to neutrinos, there are many other particles that may be signals of dark matter annihilation. In contrast to direct detection, there have been many reported anomalies in indirect detection, and some of these have been interpreted as possible evidence for dark matter. The most prominent recent example is the detection of positrons and electrons with energies between 10 GeV and 1 TeV by the Payload for Antimatter/Matter Exploration and Light-nuclei Astrophysics (PAMELA) (Adriani et al. 2009), Advanced Thin Ionization Calorimeter (ATIC) (Chang et al. 2008), and Fermi Large Area Telescope (Fermi LAT) (Abdo et al. 2009).
collaborations. These data are shown in Figure 9 and reveal an excess above an estimate of the expected background, as modeled by GALPROP (Strong et al. 2009).

These data have several plausible astrophysical explanations. The ATIC and Fermi experiments are unable to distinguish positrons from electrons, and so constrain the total $e^+ + e^−$ flux. As seen in Figure 9, the ATIC “bump” is not confirmed by the Fermi LAT data, which have much higher statistics. The Fermi data may be explained by modifying the spectral index of the cosmic ray background (Grasso et al. 2009). This exacerbates the PAMELA discrepancy, but the PAMELA data, with or without the modified spectral index, are consistent with expectations from pulsars derived both before (Boulares 1989, Zhang & Cheng 2001) and after (Profumo 2008; Hooper, Blasi & Serpico 2009; Yuksel, Kistler & Stanev 2009) the PAMELA data (see Figure 9), and may also have other astrophysical explanations (Biermann et al. 2009; Dado & Dar 2009; Katz et al. 2009).

Despite the astrophysical explanations, one may explore the possibility that the positron excesses arise from dark matter annihilation. The energies of the excess, around $m_{\text{weak}}$, are as expected for WIMPs. Unfortunately, the observed fluxes are far larger than expected for generic WIMPs. For a WIMP annihilating through S-wave processes to have the desired thermal relic density, its annihilation cross section must be $\sigma_{\text{th}} \equiv \langle \sigma v \rangle \approx 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$. This must be enhanced by two or three orders of magnitude to explain the positron data, as shown in Figure 10. Astrophysical boosts from substructure are unable to accommodate such large enhancements, and so one must look to particle physics.

A seemingly attractive solution is to postulate that dark matter interacts with a light force carrier $\phi$ with fine structure constant $\alpha_X \equiv \lambda^2/(4\pi)$. For massless $\phi$, this enhances the annihilation cross section by the Sommerfeld enhancement factor

$$S = \frac{\pi \alpha_X/v_{\text{rel}}}{1 - e^{-\alpha_X/m_X/v_{\text{rel}}}},$$

\hspace{1cm} (16)

an effect first derived for the case of $e^+ + e^−$ annihilation (Sommerfeld 1931). For massive $\phi$, $S$ is typically cut off at a value $\propto \alpha_X m_X/m_\phi$ (Hisano, Matsumoto & Nojiri 2003; Cirelli, Strumia & Tamburini 2007; Arkani-Hamed et al. 2009; Cirelli et al. 2009). The relative velocity of
The annihilation cross section enhancement factor $S$ required to explain the PAMELA and Fermi data, as a function of dark matter mass $m_X$ (shaded regions) (Bergstrom, Edsjo & Zaharijas 2009), along with upper bounds on $S$ from the requirement that the dark matter has the right thermal relic density. From Feng, Kaplinghat & Yu (2009).

colliding dark matter particles is $v_{rel} \sim 1/3$ at freeze out and $v_{rel} \sim 10^{-3}$ now. The Sommerfeld enhancement therefore provides an elegant mechanism for boosting annihilations now. The case $m_\phi = 0$ is excluded by constraints from dark matter annihilation in protohalos with $v_{rel} \sim 10^{-8}$ (Kamionkowski & Profumo 2008). However, taking $m_X \sim 1 \text{ TeV}$ and $m_\phi \sim \text{MeV} - \text{GeV}$, and assuming $\langle \sigma v \rangle \approx \sigma_{\text{th}}$, one may seemingly still generate $S \sim 10^3$ to explain the positron excesses, whereas the cutoff allows one to satisfy the protohalo constraint.

Unfortunately, for the annihilation cross section for $XX \rightarrow \phi\phi$ to give the correct relic density, $\alpha_X$ cannot be too large, which bounds $S$ from above. Even ignoring the $S$ cutoff for massive $\phi$, the resulting constraints exclude the possibility that, with standard astrophysical assumptions, Sommerfeld enhancement alone can explain the PAMELA and Fermi excesses, as shown in Figure 10. For particular choices of $\alpha_X$, $m_X$, and $m_\phi$, $S$ may in fact be resonantly enhanced, but these enhancements also reduce the thermal relic density (Dent, Dutta & Scherrer 2009; Zavala, Vogelsberger & White 2009) and, in fact, their overall effect is to increase the discrepancy.

There are other proposed dark matter explanations: for example, the annihilation cross section may be boosted by resonances from states with mass $\sim 2m_X$ (Feldman, Liu & Nath 2009; Guo & Wu 2009; Ibe, Murayama & Yanagida 2009; Ibe & Yu 2009), or the dark matter may be produced not by thermal freeze out, but by decays (Arvanitaki et al. 2009). At present, however, the dark matter explanations are considerably more exotic than the astrophysical ones. Additional data from, for example, Fermi and the Alpha Magnetic Spectrometer (AMS), an antimatter detector to be placed on the International Space Station, may be able to distinguish the various proposed explanations for the positron excesses, as well as be sensitive to canonical WIMP models, but it remains to be seen whether the astrophysical backgrounds may be sufficiently well understood for these experiments to realize their dark matter search potential.

In addition to neutrinos from the Sun and positrons from the galactic halo, there are several other promising indirect detection search strategies. Searches for antiprotons and antideuterons...
from WIMP annihilation in the galactic halo provide complementary searches, as they are sensitive to dark matter candidates that annihilate primarily to quarks. In addition, searches for gamma rays by space-based experiments, such as Fermi and AMS, and by ground-based atmospheric Cherenkov telescopes are also promising. The most striking gamma ray signal would be mono-energetic photons from $XX \rightarrow \gamma\gamma$, but because WIMPs cannot be charged, these processes are loop-induced and typically highly suppressed. More commonly, gamma rays are produced when WIMPs annihilate to other particles, which then radiate photons, leading to a smooth distribution of gamma ray energies. However, photons point back to their source, providing a powerful diagnostic. Possible targets for gamma ray searches are the center of the Galaxy, where signal rates are high but backgrounds are also high and potentially hard to estimate, and dwarf galaxies, where signal rates are lower, but backgrounds are also expected to be low.

### 3.5. Particle Colliders

If WIMPs are the dark matter, what can colliders tell us? Given the energy of the LHC and the requirement that WIMPs have mass $\sim m_{\text{weak}}$ and interact through the weak force, WIMPs will almost certainly be produced at the LHC. Unfortunately, direct WIMP production of $XX$ pairs is invisible. The next best targets are mono-jet or mono-photon signals from $XXj$ and $XX\gamma$ production, respectively, where the jet $j$ or photon comes from initial state radiation. At the International Linear Collider, a proposed high-energy $e^+e^-$ collider, such signals can be disentangled from background, using the fact that the initial state particles have definite energy and may be polarized, which provides a useful diagnostic (Birkedal, Matchev & Perelstein 2004). Unfortunately, these features are missing at hadron colliders, where the initial state protons have fixed energy but the quarks and gluons do not. As a result, at the Tevatron and LHC, the mono-jet and mono-photon signals are completely obscured by backgrounds such as $Zj$ and $Z\gamma$ followed by $Z \rightarrow \nu\bar{\nu}$ (Feng, Su & Takayama 2006).

Searches for dark matter at the LHC therefore rely on indirect production. For example, in supersymmetry, the LHC typically produces pairs of squarks and gluinos. These then decay through some cascade chain, eventually ending up in neutralino WIMPs, which escape the detector. Their existence is registered through the signature of missing energy and momentum, a signal that is a staple of searches for physics beyond the SM.

Although the observation of missing particles is consistent with the production of dark matter, it is far from compelling evidence. The observation of missing particles only implies that a particle was produced that was stable enough to exit the detector, typically implying a lifetime $\tau \gtrsim 10^{-7}$ s, a far cry from the criterion $\tau \gtrsim 10^{17}$ s required for dark matter.

Clearly more is needed. In the past few years, there has been a great deal of progress in this direction. The main point of this progress has been to show that colliders can perform detailed studies of new physics, and this can constrain the dark matter candidate’s properties so strongly that the candidate’s thermal relic density can be precisely determined. The consistency of this density with the cosmologically observed density would then be strong evidence that the particle produced at colliders is, in fact, the cosmological dark matter.

This approach is analogous to the well-known case of BBN. For BBN, data from nuclear physics experiments stringently constrain cross sections involving the light nuclei. Along with the assumption of a cooling and expanding Universe, this allows one to predict the light element abundances left over from the Big Bang, and the consistency of these predictions with observations gives us confidence that the light elements were actually created in this way. For dark matter, the idea is that particle physics experiments at the LHC may stringently constrain cross sections involving dark matter and related particles. Along with the assumption of a cooling and expanding...
Constraints in the \((m_\chi, \Omega_1)\) plane from the Large Hadron Collider (LHC) and the International Linear Collider (ILC), and from the Wilkinson Microwave Anisotropy Probe (WMAP) and Planck satellites (Feng 2005, Baltz et al. 2006). WMAP and Planck measure \(\Omega_1\), but are insensitive to the dark matter mass \(m_\chi\); the collider experiments bound both. These results are for LCC1, a supersymmetric model with minimal supergravity parameters \([m_0, M_1/2, \tan \beta, A_0, \text{sign}(\mu)] = [100 \text{ GeV}, 250 \text{ GeV}, 10, -100 \text{ GeV}, +]\).

Universe, these microscopic data allow one to predict the dark matter relic density, basically by following the relic density curves of Figure 2. This thermal relic density may be compared to the observed density of dark matter, and their consistency would give us confidence that dark matter is actually produced in this way and is made of the particles produced at the collider.

How well can the LHC do? The answer depends sensitively on the underlying dark matter scenario, but several qualitatively different cases have now been studied (Allanach et al. 2004; Birkedal et al. 2005; Moroi, Shimizu & Yotsuyanagi 2005; Baltz et al. 2006). The results of one (exemplary) case study are given in Figure 11. In conjunction with other cosmological observations, the Wilkinson Microwave Anisotropy Probe (WMAP) satellite constrains the dark matter relic density \(\Omega_1\) to a fractional uncertainty of \(\pm 8\%\). Its successor, Planck, is expected to sharpen this to \(\pm 2\%\). Of course, CMB experiments do not constrain the dark matter mass. At the same time, precision studies at the LHC can determine so many of the supersymmetric model parameters that the neutralino mass can be determined to \(\pm 5\ \text{GeV}\), and the thermal relic density can be predicted to \(\pm 20\%\). Measurements at the International Linear Collider could improve these constraints on mass and relic density to \(\pm 50\ \text{MeV}\) and \(\pm 3\%\), respectively.

Consistency between the particle physics predictions and the cosmological observations would provide compelling evidence that the particle produced at the LHC is in fact dark matter. Along the way, the colliders also determine the dark matter’s mass, spin, and many other properties. In this way, colliders may finally help solve the question of the microscopic identity of dark matter. Note also that, just as BBN gives us confidence that we understand the Universe back to 1 s after the Big Bang and temperatures of 1 MeV, such dark matter studies should provide a window on the era of dark matter freeze out at 1 ns after the Big Bang and temperatures of \(\sim 10\ \text{GeV}\). Of course, the thermal relic density prediction from colliders and the cosmological observations need
not be consistent. In this case, there are many possible lines of inquiry, depending on which is larger.

4. SUPERWIMPS

The WIMP miracle might appear to require that dark matter have weak interactions if its relic density is naturally to be in the right range. This is not true, however—in recent years, two other mechanisms have been shown to be viable and lead to dark matter particles that also exploit the WIMP miracle to have the correct relic density, but have vastly different interactions and implications for detection. These two possibilities are the topics of this Section and Section 6.

In this Section, I discuss superWIMPs, superweakly interacting massive particles, which have the desired relic density, but have interactions that are much weaker than weak. The extremely weak interactions of superWIMPs might naively be thought to be a nightmare for searches for dark matter. In fact, superWIMP scenarios predict signals from cosmic rays, at colliders, and in astrophysics that can be far more striking than in WIMP scenarios, making superWIMPs highly amenable to experimental investigation.

4.1. Production Mechanisms

4.1.1. Decays. In the superWIMP framework, dark matter is produced in late decays: WIMPs freeze out as usual in the early Universe, but later decay to produce superWIMPs, which form the dark matter that exists today (Feng, Rajaraman & Takayama 2003b,c). Because superWIMPs are very weakly interacting, they have no impact on WIMP freeze out in the early Universe, and the WIMPs decouple, as usual, with a thermal relic density \( \Omega_{\text{WIMP}} \sim \Omega_{\text{DM}} \). Assuming that each WIMP decay produces one superWIMP, the relic density of superWIMPs is

\[
\Omega_{\text{SWIMP}} = \frac{m_{\text{SWIMP}}}{m_{\text{WIMP}}} \Omega_{\text{WIMP}}.
\]

SuperWIMPs therefore inherit their relic density from WIMPs, and for \( m_{\text{SWIMP}} \sim m_{\text{WIMP}} \), the WIMP miracle also implies that superWIMPs are produced in the desired amount to be much or all of dark matter. The evolution of number densities is shown in Figure 12. The WIMP decay may be very late by particle physics standards. For example, if the superWIMP interacts only gravitationally, as is true of many well-known candidates, the natural timescale for WIMPs decaying to superWIMPs is \( 1/(G_N m_{\text{weak}}^3) \sim 10^3 - 10^7 \) s.

Because the WIMP is unstable and not the dark matter, it need not be neutral in this context—to preserve the naturalness of the superWIMP relic density, all that is required is \( \Omega_{\text{WIMP}} \sim \Omega_{\text{DM}} \). In the case of supersymmetry, for example, the WIMP may be a neutralino, but it may also be a charged slepton. Even though charged sleptons interact with photons, on dimensional grounds, their annihilation cross sections are also necessarily governed by the weak scale, and so are \( G_N^4 m_{\text{weak}}^2 \), implying roughly the same relic densities as their neutral counterparts. Of course, whether the WIMP is charged or not determines the properties of the other particles produced in WIMP decay, which has strong consequences for observations, as I discuss below.

4.1.2. Reheating. SuperWIMPs may also be produced after reheating, when the energy of the inflaton potential is transferred to SM and other particles. This creates a hot thermal bath, and, if the temperature is high enough, may be a significant source of superWIMPs (Krauss 1983; Nanopoulos, Olive & Srednicki 1983; Ellis, Kim & Nanopoulos 1984; Khlopov & Linde 1984; Juszkiewicz, Silk & Stebbins 1985).
Figure 12

In super weakly interacting massive particle (superWIMP) scenarios, WIMPs freeze out as usual, but then decay to superWIMPs that are the dark matter. This Figure shows the WIMP comoving number density \( Y \) (left) and the superWIMP relic density (right) as functions of temperature \( T \) (bottom) and time \( t \) (top). The WIMP is a 1-TeV, \( S \)-wave annihilating particle with lifetime \( 10^3 \) s, and the superWIMP has mass 100 GeV.

After reheating, the Universe is characterized by three rates: the interaction rate of particles that have SM interactions, \( \sigma_{SM} n \); the expansion rate, \( H \); and the rate of interactions involving a superWIMP, \( \sigma_{SWIMP} n \). Here \( n \) is the number density of SM particles. After reheating, the Universe is expected to have a temperature well below the Planck scale, but still well above SM masses. Assuming the superWIMP is gravitationally interacting, dimensional analysis implies that these rates are hierarchically separated:

\[
\sigma_{SM} n \sim T \gg H \sim T^2 / M_{Pl} \gg \sigma_{SWIMP} n \sim T^3 / M_{Pl}^2.
\] (18)

This implies a very simple picture: After reheating, particles with SM interactions are in thermal equilibrium with each other. Occasionally these interact to produce a superWIMP. The produced superWIMPs then propagate through the Universe essentially without interacting and without annihilating, surviving to the present day.

To determine the superWIMP abundance, I turn once again to the Boltzmann equation of Equation 5, where now \( n \) is the number density of superWIMPs. To be concrete, consider the case of gravitino superWIMPs. In this case, the source term \( n^2 \) arises from interactions that produce superWIMPs, such as \( gg \rightarrow \tilde{g} \tilde{G} \). In contrast to our previous application of the Boltzmann equation in Section 3.1.1, however, here the sink term \( n^2 \) is negligible. Changing variables with \( t \rightarrow T \) and \( n \rightarrow Y \equiv n / s \), where \( s \) is the entropy density, we find

\[
\frac{dY}{dT} = -\frac{(\sigma_{\tilde{G} v})}{HTs} n^2.
\] (19)

The right-hand side is independent of \( T \), because \( n \propto T^3 \), \( H \propto T^2 \), and \( s \propto T^3 \). We thus find an extremely simple relation—the superWIMP relic number density is linearly proportional to the reheating temperature \( T_R \).

The constant of proportionality is the gravitino production cross section. Including all such production mechanisms, the gravitino relic density can be determined as a function of reheating temperature \( T_R \) and gravitino mass. For gravitino mass \( m_{\tilde{G}} \lesssim 100 \) GeV, the constraint on \( \Omega_{DM} \) requires \( T_R \lesssim 10^{10} \) GeV (Bolz, Brandenburg & Buchmuller 2001). Of course, if this bound is nearly saturated, gravitinos produced after reheating may be a significant component of dark matter, adding to the relic density from decays.
4.2. Candidates

4.2.1. Weak-scale gravitinos. The superWIMP scenario is realized in many particle physics models. The prototypical superWIMP is the gravitino ˜G (Feng, Rajaraman & Takayama 2003b,c; Buchmuller et al. 2004; Ellis et al. 2004; Wang & Yang 2004; Roszkowski, Ruiz de Austri & Choi 2005). Gravitinos are the spin 3/2 superpartners of gravitons, and they exist in all supersymmetric theories. The gravitino’s mass is

\[ m_{\tilde{G}} = \frac{F}{\sqrt{3} M^*_s}, \quad (20) \]

where \( F \) is the supersymmetry-breaking scale squared and \( M^*_s = (8\pi G_N)^{-1/2} \approx 2.4 \times 10^{18} \text{ GeV} \) is the reduced Planck mass. In the simplest supersymmetric models, where supersymmetry is transmitted to SM superpartners through gravitational interactions, the masses of SM superpartners are

\[ \tilde{m} \sim \frac{F}{M^*_s}. \quad (21) \]

A solution to the gauge hierarchy problem requires \( F \sim (10^{11} \text{ GeV})^2 \), and so all superpartners and the gravitino have weak-scale masses. The precise ordering of masses depends on unknown, presumably \( O(1) \), constants in Equation 21. There is no theoretical reason to expect the gravitino to be heavier or lighter than the lightest SM superpartner, and so in roughly half of the parameter space, the gravitino is the lightest supersymmetric particle (LSP). Its stability is guaranteed by \( R \)-parity conservation, and because \( m_{\tilde{G}} \approx \tilde{m} \), the gravitino relic density is naturally \( \Omega_{\text{gravitino}} \sim \Omega_{\text{DM}} \).

In gravitino superWIMP scenarios, the role of the decaying WIMP is played by the next-to-lightest supersymmetric particle (NLSP), a charged slepton, sneutrino, chargino, or neutralino. The gravitino couples SM particles to their superpartners through gravitino-sfermion-fermion interactions,

\[ L = -\frac{1}{\sqrt{2} M^*_s} \partial_\mu \tilde{f} \gamma^n \gamma^\nu \tilde{G}_\mu, \quad (22) \]

and gravitino-gaugino-gauge boson interactions,

\[ L = -\frac{i}{8M^*_s} \tilde{G}_\mu [\gamma^n, \gamma^\mu] \gamma^n \tilde{F}_{\nu\rho}. \quad (23) \]

The presence of \( M^*_s \) in Equations 22 and 23 implies that gravitinos interact only gravitationally, a property dictated by the fact that they are the superpartners of gravitons. These interactions determine the NLSP decay lifetime. As an example, if the NLSP is a stau, a superpartner of the tau lepton, its lifetime is

\[ \tau(\tilde{\tau} \to \tau \tilde{G}) = \frac{6}{G_N m_\tau^2} \left[ 1 - \frac{m_\tau^2}{m_{\tilde{G}}^2} \right]^{-4} \approx 3.6 \times 10^7 \text{s} \left[ \frac{100 \text{ GeV}}{m_{\tilde{G}}} \right]^4 \left[ \frac{m_{\tilde{G}}}{100 \text{ GeV}} \right], \quad (24) \]

where the approximate expression holds for \( m_{\tilde{G}}/m_\tau \approx 1 \). Decay lifetimes of the order of hours to months are perfectly natural. At the same time, the lifetime is quite sensitive to the underlying parameters and may be much longer for degenerate \( \tilde{\tau} \to \tilde{G} \) pairs, or much shorter for light gravitinos.

4.2.2. Others. In addition to gravitinos, other well-motivated examples of superWIMPs include axinos (Rajagopal, Turner & Wilczek 1991; Covi, Kim & Roszkowski 1999; Covi et al. 2001), the supersymmetric partners of axions, particles introduced to resolve the strong CP problem described in Section 2.2.4. Axions may also be cold dark matter (see Section 8), and the possibility...
that both axions and axinos contribute to dark matter is one of the better motivated multicomponent dark matter scenarios (Baer & Box 2009). UED models also have superWIMP candidates in the form of KK graviton and axion states (Feng, Rajaraman & Takayama 2003a). One of these may be the lightest KK state; in fact, in minimal UED, the KK graviton is the lightest KK state for all $R^{-1} < 800$ GeV, where $R$ is the compactification radius (Cembranos, Feng & Strigari 2007). If one of these is the lightest KK state, it is stabilized by KK-parity conservation and has properties very similar to its supersymmetric analog. Other superWIMP candidates include quintessinos in supersymmetric theories (Bi, Li & Zhang 2004), stable particles in models that simultaneously address the problem of baryon asymmetry [R. Kitano and I. Low, unpublished manuscript (hep-ph/0503112)], and other particles produced in decays, where the decay time is greatly lengthened by mass degeneracies (Strigari, Kaplinghat & Bullock 2007; Cembranos & Strigari 2008).

In summary, there are many superWIMP candidates that possess all of the key virtues of WIMPs: They exist in the same well-motivated frameworks and, because they inherit their relic density from WIMPs, are also naturally produced with the desired relic density. However, they have completely different implications for detection.

4.3. Indirect Detection

SuperWIMPs are so weakly interacting that they cannot be detected by direct searches, and their annihilation cross sections are so suppressed that their annihilation signal rates are completely negligible. However, if the decaying WIMP is charged, the superWIMP scenario implies long-lived charged particles with striking implications for indirect detection.

One interesting possibility is that long-lived charged particles may be produced by ultrahigh energy cosmic rays, resulting in exotic signals in cosmic ray and cosmic neutrino experiments (Albuquerque, Burdman & Chacko 2004; Bi et al. 2004). As an example, in the gravitino superWIMP scenario with a stau NLSP, ultrahigh energy neutrinos may produce events with two long-lived staus through $\nu q \rightarrow \tilde{\tau} \tilde{q}'$ followed by the decay $\tilde{q}' \rightarrow \tau$. The metastable staus then propagate to neutrino telescopes (Huang et al. 2006), where they have a typical transverse separation of hundreds of meters. They may therefore be detected above background as events with two upward-going, extremely high-energy-charged tracks in experiments such as IceCube.

4.4. Particle Colliders

Particle colliders may also find evidence for superWIMP scenarios. This evidence may come in one of two forms. Collider experiments may see long-lived, charged particles. Given the stringent bounds on charged dark matter, such particles presumably decay, and their decay products may be superWIMPs. Alternatively, colliders may find seemingly stable particles, but the precision studies described in Section 3.5 may imply that these particles have a thermal relic density that is too large. These two possibilities are not mutually exclusive. In fact, the discovery of long-lived, charged particles with too-large predicted relic density is a distinct possibility and would strongly motivate superWIMP dark matter.

As an example, again consider a gravitino superWIMP with a charged slepton NLSP. (The possibility of a neutralino NLSP is essentially excluded by considerations of BBN, as discussed in Section 4.5.2.) In the slepton NLSP scenario, supersymmetric events at colliders are not characterized by missing energy and momentum as predicted in WIMP dark matter scenarios, but rather by pairs of heavy, long-lived, charged particles. Such particles lead to spectacular signals and require far less luminosity for discovery than missing energy signals (Drees & Tata 1990, Rajaraman & Smith 2007).
To determine the superWIMP relic density of Equation 17, we must determine the superWIMP’s mass. This is not easy, because the WIMP lifetime may be very large, implying that superWIMPs are typically produced long after the WIMPs have escaped collider detectors. At the same time, because some sleptons are slowly moving and highly ionizing, they may be trapped and studied. As an example, sleptons may be trapped in water tanks placed outside collider detectors. These water tanks may then be drained periodically to underground reservoirs where slepton decays can be observed in quiet environments. The number of sleptons that may be trapped is model-dependent, but a 1-m-thick tank of water may trap as many as a thousand sleptons per year (Feng & Smith 2005). Other possibilities for capturing sleptons include using the LHC detectors themselves as the slepton traps (Hamaguchi et al. 2004), or carefully tracking sleptons as they exit the detector and digging them out of the walls of the detector halls, giving new meaning to the phrase data mining (De Roeck et al. 2007).

If thousands of sleptons are trapped, the slepton lifetime may be determined to the few percent level simply by counting the number of slepton decays as a function of time. The slepton mass is constrained by analysis of the collider event kinematics. Furthermore, the outgoing lepton energy can be measured, and this provides a high-precision measurement of the gravitino mass and, therefore, a determination of the gravitino relic density through Equation 17. Consistency at the percent level with the observed dark matter relic density provides strong evidence that dark matter is indeed composed of gravitino superWIMPs.

Perhaps as interesting, the determination of \( \tau \), \( m_{\tilde{G}} \), and \( m_l \) in Equation 24 implies that one can differentiate the various superWIMP candidates (Brandenburg et al. 2005) and determine Newton’s constant on the scale of fundamental particles (Buchmuller et al. 2004; Feng, Rajaraman & Takayama 2004). According to conventional wisdom, particle colliders are insensitive to gravity, because it is such a weak force. However, this is not true—if \( G_N \) enters in a decay time, one can achieve the desired sensitivity simply by waiting a long time. In this case, one can measure the force of gravity between two test particles with masses \( \sim 10^{-27} \) kg, a regime that has never before been probed. If this force is consistent with gravity, these studies should show that the newly discovered particle is indeed interacting gravitationally, as is required for the gravitino to be the graviton’s superpartner, and demonstrate that gravity is in fact extended to supergravity in nature.

### 4.5. Astrophysical Signals

Because superWIMPs are very weakly interacting, the decays of WIMPs to superWIMPs may be very late and have an observable effect on BBN and the CMB. In addition, in contrast to WIMPs, superWIMP dark matter may behave as warm dark matter.

#### 4.5.1. Cosmic microwave background

When WIMPs decay to superWIMPs, the accompanying particles may distort the frequency dependence of the CMB away from its ideal black body spectrum (Hu & Silk 1993; Feng, Rajaraman & Takayama 2003c; Lamon & Durrer 2006). The impact on the CMB is determined by the NLSP lifetime and the energy released in visible decay products when the WIMP decays. The energy release is conveniently expressed in terms of

\[
\zeta_{\text{EM}} \equiv \epsilon_{\text{EM}} Y_{\text{NLSP}}
\]

for electromagnetic energy, with a similar expression for hadronic energy. Here \( \epsilon_{\text{EM}} \) is the initial electromagnetic energy released in NLSP decay and \( Y_{\text{NLSP}} = n_{\text{NLSP}}/n_\gamma \) is the NLSP number density just before it decays, normalized to the background photon number density \( n_\gamma = 2 \zeta(3) T^3 / \pi^2 \).

Once the NLSP is specified, and assuming superWIMPs from late decays make up all of the dark matter, with \( \Omega_\tilde{G} = \Omega_{\text{DM}} = 0.23 \), both the lifetime and energy release are determined by
Figure 13

Predicted values of weakly interacting massive particle (WIMP) lifetime $\tau$ and electromagnetic energy release $\zeta_{\text{EM}} \equiv \varepsilon_{\text{EM}} f_{\text{NLSP}}^2$ in the $\tilde{B}$ (left) and $\tilde{\tau}$ (right) superWIMP scenarios for $m_{\text{SWIMP}} = 100$ GeV, 300 GeV, 500 GeV, 1 TeV, and 3 TeV (top to bottom) and $\Delta m = m_{\text{WIMP}} - m_{\text{SWIMP}} = 600$ GeV, 400 GeV, 200 GeV, and 100 GeV (left to right). The contours are for $\mu$, which parameterizes the distortion of the cosmic microwave background from a Planckian spectrum. From Feng, Rajaraman & Takayama (2003c).

Only two parameters: $m_{\tilde{G}}$ and $m_{\text{NLSP}}$. The results for neutralino and slepton NLSPs are given in Figure 13.

For the decay times of interest with redshifts $z \sim 10^5$ to $10^7$, the resulting photons interact efficiently through $\gamma e^- \rightarrow \gamma e^-$ and $eX \rightarrow eX\gamma$, where $X$ is an ion, but photon number is conserved, because double Compton scattering $\gamma e^- \rightarrow \gamma \gamma e^-$ is inefficient. The spectrum therefore relaxes to statistical but not thermodynamic equilibrium, resulting in a Bose-Einstein distribution function,

$$f_\gamma(E) = \frac{1}{e^{E/(kT)} - 1},$$

with chemical potential $\mu \neq 0$. Figure 13 also includes contours of $\mu$. The current bound is $\mu < 9 \times 10^{-5}$ (Fixsen et al. 1996). Although there are at present no indications of deviations from a black body spectrum, current limits are already sensitive to the superWIMP scenario, and future improvements may further probe superWIMP parameter space.

4.5.2. Big Bang nucleosynthesis. Late time energy release after $t \sim 1$ s also destroys and creates light elements, potentially distorting the predictions of standard BBN. The impact depends sensitively on what the decaying NLSP is. For example, in the neutralino NLSP case, the neutralino decays generically through $\chi \rightarrow Z\tilde{G}, b\tilde{G}, \gamma\tilde{G}$. The first two modes lead to hadrons, which are very dangerous. Constraints from BBN on hadronic energy release essentially exclude the neutralino WIMP scenario, allowing only the fine-tuned case in which the neutralino is photino-like, $\chi \approx \tilde{\gamma}$,
Figure 14

Allowed values for the stau mass and lifetime in gravitino superweakly interacting massive particle (superWIMP) scenarios scanning over minimal supergravity parameters with \( \tan \beta = 50 \) and assuming gravitinos are produced both after reheating and in late decays. The gray dots represent models that satisfy collider constraints; the green dots represent models that also satisfy all Big Bang nucleosynthesis (BBN) constraints; the blue dots represent models that are allowed for slightly loosened BBN constraints on \(^6\text{Li}/^7\text{Li}\). From Bailly et al. (2009).

in which case the decays to \( Z^\prime G \) and \( b^\prime G \) are suppressed (Feng, Su & Takayama 2004a,b). In the charged slepton NLSP case, the decaying WIMP may first bind with nuclei, which may enhance the effect of its decays on BBN (Kaplinghat & Rajaraman 2006; Kawasaki, Kohri & Moroi 2007; Kohri & Takayama 2007; Pospelov 2007; Takayama 2008).

BBN constraints on the gravitino superWIMP possibility have been considered in a number of studies. The results of one study, which considered minimal supergravity models with a stau NLSP decaying to a gravitino superWIMP, are given in Figure 14. Without BBN constraints, extremely large stau lifetimes are possible. The BBN constraints typically exclude the largest lifetimes [although there are interesting exceptions (Ratz, Schmidt-Hoberg & Winkler 2008)]. Nevertheless, lifetimes as large as \( 10^4 \) s are still allowed for all stau masses, and even larger lifetimes are possible for light staus with mass \( \sim 100 \) GeV. Models with large lifetimes and light staus are the most promising for the collider studies described in Section 4.4, and BBN constraints do not exclude these scenarios.

Finally, late decays to superWIMPs may in fact improve the current disagreement of standard BBN predictions with the observed \(^7\text{Li}\) and \(^6\text{Li}\) abundances, although this typically requires that the decaying slepton be heavy, with mass above 1 TeV (Cumberbatch et al. 2007; Jittoh et al. 2007; Bailly, Jedamzik & Moultaka 2009). For a review, see Jedamzik & Pospelov (2009).

4.5.3. Small-scale structure. In contrast to WIMPs, superWIMPs are produced with large velocities at late times. This has two, a priori independent, effects. First, the velocity dispersion reduces the phase space density, smoothing out cusps in dark matter halos. Second, such
particles damp the linear power spectrum, reducing power on small scales (Lin et al. 2000, Sigurdson & Kamionkowski 2004, Cembranos et al. 2005, Kaplinghat 2005; Profumo et al. 2005; Jedamzik, Lemoine & Moulata 2006; Borzumati, Bringmann & Ullio 2008). As seen in Figure 15, superWIMPs may suppress small-scale structure as effectively as a 1-keV sterile neutrino, the prototypical warm dark matter candidate (see Section 7). Some superWIMP scenarios may therefore be differentiated from standard cold dark matter scenarios by their impact on small-scale structure; for a review, see Primack (2009).

5. LIGHT GRAVITINOS

The gravitino dark matter candidates discussed in Section 4 have masses around $m_{\text{weak}}$. Other well-motivated, if somewhat problematic, candidates are light gravitinos, with masses in the range of 1 eV–1 keV and very different implications for experiments.

5.1. Thermal Production

5.1.1. Gauge-mediated supersymmetry breaking. Low-energy supersymmetry elegantly addresses the gauge hierarchy problem but does not by itself solve the new physics flavor problem. In fact, the goal of solving the new physics flavor problem is the prime driver in the field of supersymmetric model building and motivates a particularly elegant subset of supersymmetric theories known as gauge-mediated supersymmetry breaking (GMSB) models (Dimopoulos & Raby 1981; Dine, Fischler & Srednicki 1981b; Alvarez-Gaume, Claudson & Wise 1982; Nappi & Ovrut 1982; Dine, Nelson & Shirman 1995; Dine et al. 1996). In these models, supersymmetry-breaking is transmitted from a supersymmetry-breaking sector to the MSSM by so-called messenger particles...
through both gauge interactions and gravity. The resulting squark and slepton mass matrices, in 3 \times 3 generation space, are of the form

\[
m^2_\tilde{f} = \begin{pmatrix}
m^2 \text{GMSB} & 0 & 0 \\
0 & m^2 \text{GMSB} & 0 \\
0 & 0 & m^2 \text{GMSB}
\end{pmatrix} + \begin{pmatrix}m^2 \text{grav} & \sim m^2 \text{grav} & \sim m^2 \text{grav} \\
\sim m^2 \text{grav} & \sim m^2 \text{grav} & \sim m^2 \text{grav} \\
\sim m^2 \text{grav} & \sim m^2 \text{grav} & \sim m^2 \text{grav}
\end{pmatrix},
\] (27)

where

\[
m_{\text{GMSB}} \sim \frac{g^2}{16\pi^2} \frac{F}{M_m}
\text{ and } m_{\text{grav}} \sim \frac{F}{M_*}.
\] (28)

The parameter \(g\) denotes gauge coupling constants, \(F\) is the supersymmetry-breaking scale squared, \(M_*\) is the reduced Planck mass, and \(M_m\) is another mass scale determined by the supersymmetry-breaking sector and is related to the mass of the messenger particles.

The essential feature is that the GMSB contributions are determined by gauge coupling constants only and so are generation-blind. They therefore do not mediate flavor-changing effects, and if they are dominant, such theories ameliorate the new physics flavor problem. For them to be dominant, one assumes \(M_m \ll M_*\) and \(F \ll (10^{11} \text{ GeV})^2\) subject to the constraint \(F/M_m \sim 100 \text{ TeV}\), so that the superpartner masses are at the weak scale, but the flavor-violating gravity contributions are negligible.

As seen in Equation 20, however, \(m_{\text{grav}} \sim m_{\tilde{G}}\), that is, the gravity contributions to the squark and slepton masses are the same size as the gravitino mass. In GMSB scenarios, then, the LSP is the gravitino. To sufficiently suppress flavor-violating effects, one typically requires \(m_{\text{grav}}, m_{\tilde{G}} \lesssim 1 \text{ GeV}\). As a result, WIMPs and superWIMPs are typically not viable dark matter candidates in GMSB models: WIMPs decay through \(R\)-parity conserving interactions such as \(\chi \rightarrow \gamma \tilde{G}\), and superWIMPs are underabundant, because \(m_{\tilde{G}} \ll m_{\text{WIMP}}\) implies \(\Omega_{\text{SWIMP}} \ll \Omega_{\text{WIMP}}\).

### 5.1.2. Relic density.

Light gravitinos may be dark matter candidates in GMSB models, however (Pagels & Primack 1982). As with neutrinos, light gravitinos may be in thermal equilibrium in the early hot Universe. They then decouple, with relic density

\[
\Omega_{\tilde{G}}^0 \approx 0.25 \frac{m_{\tilde{G}}}{100 \text{ eV}}.
\] (29)

When originally proposed, \(\Omega_{\text{DM}} \sim 1\) was possible, and constraints from structure formation allowed \(m_{\tilde{G}} \sim 100 \text{ eV}–1 \text{ keV}\). Such “keV gravitinos” were then viable dark matter candidates. There is no theoretical reason to favor the 100 eV–1 keV mass range for gravitinos, and so this scenario does not naturally explain the relic density in the way that the WIMP miracle does. In contrast to WIMPs and superWIMPs, however, light gravitinos are well motivated by their presence in models that solve not only the gauge hierarchy problem, but also the new physics flavor problem.

The light gravitino scenario has become much less simple in recent years, however. The allowed value for the dark matter relic density has been reduced to \(\Omega_{\text{DM}} \lesssim 0.23\). In addition, there are much more stringent limits on how hot dark matter can be. Among the strongest bounds are those from Lyman-\(\alpha\) forest observations, which constrain the distribution of gas between distant objects and us. Observations of density fluctuations on relatively small scales imply that dark matter should not have erased power on these scales. Lyman-\(\alpha\) constraints therefore require that the bulk of dark matter be sufficiently cold, implying \(m_{\tilde{G}} \gtrsim 2 \text{ keV}\) (Seljak et al. 2006, Viel et al. 2006). Together, these developments have closed the window on the minimal light gravitino dark matter scenario.
There are, however, at least two viable extensions. In the one-component gravitino scenario, sometimes abbreviated ΛWDM, the gravitino has mass $\gtrsim 2$ keV and is cold enough to agree with Lyman-α constraints, but its thermal relic density is either not realized, for example, because of a low reheating temperature, or is significantly diluted, for example, through late entropy production (Baltz & Murayama 2003). Alternatively, in the two-component gravitino scenario, typically denoted ΛCWDM, the gravitino has mass $\lesssim 16$ eV (Viel et al. 2005), but it is a sufficiently small portion of the dark matter to be consistent with structure formation constraints, provided another particle contributes an additional and dominant cold or warm component.

5.2. Particle Colliders

Remarkably, the ΛWDM and ΛCWDM scenarios may be differentiated at particle colliders. In contrast to weak-scale gravitinos, light gravitino interactions are stronger than gravitational, as they are enhanced by their spin 1/2 longitudinal Goldstino components. These interactions depend on the supersymmetry-breaking scale $F$ and are stronger for lighter gravitinos. For example, a Bino-like neutralino has decay width

$$\Gamma(\tilde{B} \rightarrow \gamma \tilde{G}) = \frac{\cos^2 \theta_W m_{\tilde{B}}}{16\pi F^2},$$

where $\theta_W$ is the weak mixing angle, corresponding to a decay length

$$c \tau \simeq 22 \text{ cm} \left[\frac{m_{\tilde{G}}}{100 \text{ eV}}\right]^2 \left[\frac{100 \text{ GeV}}{m_{\tilde{B}}}\right]^3.$$  

The two light gravitino scenarios therefore predict decay lengths that are either shorter or longer than typical sizes of particle detectors. In a Bino LSP GMSB scenario, supersymmetry events should be seen through missing energy in the ΛWDM scenario, but would be characterized by two high-energy photons in the ΛCWDM scenario. Such diphoton events are the subject of ongoing searches at the Tevatron (Aaltonen et al. 2010b) and will be spectacular at the LHC. Similar results hold for the stau NLSP scenario and the decay $\tilde{\tau} \rightarrow \tau \tilde{G}$: Supersymmetry events will appear with pairs of metastable heavy charged particles in the ΛWDM scenario, but will be characterized by two high-energy taus in the ΛCWDM scenario. The observation of these various event types, when interpreted in the gravitino dark matter framework, may therefore have strong cosmological implications, for example, indicating an era of late entropy production in the ΛWDM case, or strongly implying the existence of another, dominant, form of dark matter in the ΛCWDM scenario.

6. HIDDEN DARK MATTER

As noted in Section 1, despite great recent progress, all solid evidence for dark matter is gravitational. There is also strong evidence against dark matter having strong or electromagnetic interactions. A logical possibility, then, is hidden dark matter, that is, dark matter that has no SM gauge interactions. Hidden dark matter has been explored for decades and brings with it a great deal of model building freedom, leading to a large and diverse class of candidates (Kobzarev, Okun & Pomeranchuk 1966; Berezhiani, Dolgov & Mohapatra 1996; Blinnikov & Khlopov 1982; Foot, Lew & Volkas 1991; Hodges 1993). Unfortunately, this freedom comes at a cost: by considering hidden dark matter, one typically loses (i) connections to the central problems of particle physics discussed in Section 2.2, (ii) the WIMP miracle, and (iii) predictivity, because most hidden dark
matter candidates have no nongravitational signals, which are most likely required if we are to identify dark matter.

Recently, however, some hidden dark matter models have been shown to have some, or even all, of the three properties listed above, putting them on more solid footing and providing extra structure and motivation for this framework. In this Section, I first consider the general possibility of hidden sectors, but then focus on this subset of hidden dark matter candidates and explore their properties and implications for detection.

6.1. Thermal Freeze Out

6.1.1. Constraints on temperature and degrees of freedom. The thermal history of hidden sectors may differ from that of the visible sector. However, the hidden sector’s temperature, along with its “size,” is constrained, to the extent that it affects the cosmological history of the visible sector.

One of the leading constraints on hidden sectors is provided by BBN. The success of BBN is highly sensitive to the expansion rate of the Universe at time \( t_{\text{BBN}} \approx 1 - 1.000 \) s. Light degrees of freedom in a hidden sector change the expansion rate of the Universe and thereby impact BBN, even if they have no SM interactions. The constraint is conventionally quoted as a bound on \( n_{\text{eff}} \), the effective number of light neutrino species, and may be taken to be \( n_{\text{eff}} = 3.24 \pm 1.2 \) (95% CL) (Cyburt et al. 2005, Fields & Sarkar 2006, Ciarcelluti & Lepidi 2008). This implies

\[
g_4(T_{\text{BBN}}^h)(T_{\text{BBN}}^h/T_{\text{BBN}}) = \frac{7}{8} \cdot 2 \cdot (n_{\text{eff}} - 3) \leq 2.52 \text{ (95\% CL)},
\]

where \( T_{\text{BBN}}^h \) and \( T_{\text{BBN}} \) are the temperatures of the hidden and visible sectors at time \( t_{\text{BBN}} \). This is a significant constraint (Kolb, Seckel & Turner 1985); for example, Equation 32 excludes a hidden sector that is an exact copy of the SM with \( g_4(T_{\text{BBN}}^h) = 10.75 \), assuming it has the same temperature as the visible sector, so \( T_{\text{BBN}}^h = T_{\text{BBN}} \).

As evident in Equation 32, however, this statement is highly sensitive to the hidden sector’s temperature. If the observable and hidden sectors are not in thermal contact, the hidden sector may be colder than the observable sector. This would be the case if, for example, the inflaton couplings to the observable and hidden sectors are not identical, so that they reheat to different temperatures (Hodges 1993; Berezhiani, Dolgov & Mohapatra 1996). Alternatively, the observable and hidden sectors may initially have the same temperature, either because they have the same inflaton couplings or because they are in thermal contact, but may cool independently and have different temperatures at later times. For hidden sector temperatures that are now half of the observable sector’s temperature, hundreds of degrees of freedom, equivalent to several copies of the SM or MSSM, may be accommodated.

6.1.2. The WIMPless miracle. It is desirable for hidden dark matter to have naturally the correct relic density, just as in the case of WIMPs. One way to achieve this goal would be to duplicate the couplings and mass scales of the visible sector in the hidden sector so that the WIMP miracle is satisfied in the hidden sector. Given the discussion above, this is certainly possible if the hidden sector has fewer light degrees of freedom than the visible sector or is slightly colder.

At the same time, this possibility is both rather unmotivated and far too rigid. As discussed in Section 3.1.1, the thermal relic density of a stable particle with mass \( m_X \) annihilating through
interactions with couplings $g_X$ is

$$\Omega_X \sim \langle \sigma v \rangle^{-1} \sim \frac{m_X^2}{g_X^4}.$$  \hfill (33)

The WIMP miracle is the fact that, for $m_X \sim m_{\text{weak}}$ and $g_X \sim g_{\text{weak}} \simeq 0.65$, $\Omega_X$ is roughly $\Omega_{\text{DM}} \approx 0.23$.

Equation 33 makes clear, however, that the thermal relic density fixes only one combination of the dark matter’s mass and coupling, and other combinations of $(m_X, g_X)$ can also give the correct $\Omega_X$. In the SM, $g_X \sim g_{\text{weak}}$ is the only choice available, but in a general hidden sector, with its own matter content and gauge forces, other values of $(m_X, g_X)$ may be realized. Such models generalize the WIMP miracle to the “WIMPless miracle”: dark matter that naturally has the correct relic density, but does not necessarily have a weak-scale mass or weak interactions (Feng & Kumar 2008).

### 6.2. Candidates

The WIMPless miracle is naturally realized in particle physics frameworks that have several other motivations. As an example, consider the supersymmetric models with GMSB described previously in Section 5.1.1. These models necessarily have several sectors, as shown in Figure 16. The supersymmetry-breaking sector includes the fields that break supersymmetry dynamically and the messenger particles that mediate this breaking to other sectors through gauge interactions. The MSSM sector includes the fields of supersymmetric extension of the SM. In addition, supersymmetry breaking may be mediated to one or more hidden sectors. The hidden sectors are not strictly necessary, but there is no reason to prevent them, and hidden sectors are ubiquitous in such models originating in string theory.

As described in Section 5.1.1, the essential feature of GMSB models is that they elegantly address the new physics flavor problem by introducing generation-independent squark and slepton...
masses of the form

$$m \sim \frac{g^2}{16\pi^2} \frac{F}{M_m}.$$  

(34)

The generic feature is that superpartner masses are proportional to gauge couplings squared times the ratio $F/M_m$, which is a property of the supersymmetry-breaking sector. With analogous couplings of the hidden sector fields to hidden messengers, the hidden sector superpartner masses are

$$m_X \sim \frac{g_X^2}{16\pi^2} \frac{F}{M_m},$$  

(35)

where $g_X$ is the relevant hidden sector gauge coupling. As a result,

$$\frac{m_X}{g_X^2} \sim \frac{m}{g^2} \sim \frac{F}{16\pi^2 M_m},$$  

(36)

that is, $m_X/g_X^2$ is determined solely by the supersymmetry-breaking sector. As this is exactly the combination of parameters that determines the thermal relic density of Equation 33, the hidden sector automatically includes a dark matter candidate that has the desired thermal relic density, irrespective of its mass. This has been verified numerically for a concrete hidden sector model; the results are shown in Figure 17. This property relies on the relation $m_X \propto g_X^2$, which is common to other frameworks for new physics that avoid flavor-changing problems, such as anomaly mediated supersymmetry breaking. The “coincidence” required for WIMPless dark matter may also be found in other settings; see, e.g., Hooper & Zurek (2008).

WIMPless and other hidden sector models also naturally open the possibility of dark forces in the hidden sector. In the WIMPless scenarios just described, this possibility arises naturally if one attempts to understand why the hidden sector particle is stable. This is an important question; after all, in these GMSB models, all SM superpartners decay to the gravitino. In the hidden sector, an elegant way to stabilize the dark matter is through U(1) charge conservation. This possibility

![Figure 17](image-url)  

Figure 17  
Contours of $\Omega_X h^2 = 0.11$ in the $(m_X, g_X)$ plane for hidden to observable reheating temperature ratios $T_{RH}/T_{RH} = 0.8$ (upper solid green curve) and 0.3 (lower solid green curve), where the hidden sector is a 1-generation flavor-free version of the minimal supersymmetric standard model. Also plotted are lines of $m_{\text{weak}} = (m_X/g_X^2)g^2 = 100$ GeV (upper dashed blue curve) and 1 TeV (lower dashed blue curve). The weakly interacting massive particle–less dark matter (WIMPless DM) hidden models generalize the WIMP miracle to a family of models with other dark matter masses and couplings. From Feng, Tu & Yu (2008).
necessarily implies massless gauge bosons in the hidden sector. Alternatively, the hidden sector may have light, but not massless, force carriers, as described in Section 3.4. In all of these cases, the dynamics of the hidden sector may have many interesting astrophysical implications, some of which are discussed in Section 6.6.

In summary, hidden sector dark matter models may in fact be motivated by leading problems in particle physics, and may even have naturally the correct relic density, through a generalization of the WIMP miracle to the WIMPless miracle. In fact, the third virtue discussed in Section 6, predictivity, may also be restored, and I now describe nongravitational signals of hidden dark matter.

6.3. Direct Detection

The decoupling of the WIMP miracle from WIMPs has many possible implications and observable consequences. In the case that the dark matter is truly hidden, it implies that there are no prospects for direct or indirect detection. Signals must be found in astrophysical observations, as in the case of superWIMPs. Alternatively, there may be connector sectors containing particles that mediate interactions between the SM and the hidden sector through nongauge (Yukawa) interactions (see Figure 16). Such connectors may generate many signals with energies and rates typically unavailable to WIMPs.

As an example, first consider direct detection. As discussed in Section 3.3, the DAMA and CoGeNT signals may be explained without violating other bounds if the dark matter mass and spin-independent cross section are in the ranges \((m_X, \sigma_{SI}) \sim (1-10 \text{ GeV}, 10^{-41}-10^{-39} \text{ cm}^2)\). Such masses are low for conventional WIMPs, and the cross section is also very high. In WIMPless models, however, where the thermal relic density is achieved for a variety of dark matter masses, such masses are perfectly natural. Furthermore, a WIMPless particle \(X\) may couple to the SM through Yukawa interactions

\[
\mathcal{L} = \lambda_f X \bar{Y}_L f_l + \lambda_f X \bar{Y}_R f_R,
\]  

(37)

where \(Y\) is a vector-like connector fermion, and \(f\) is a SM fermion. Taking \(f\) to be the \(b\) quark, and the \(Y\) mass to be 400 GeV, consistent with current bounds, these couplings generate spin-independent scattering cross sections given in Figure 18. Thus, WIMPless dark matter may explain the DAMA and CoGeNT results. Other proposed hidden dark matter explanations of DAMA and CoGeNT include those of Foot (2008) and Kim & Shin (2009).

6.4. Indirect Detection

WIMPless dark matter also provides new target signals for indirect detection. For WIMPs, annihilation cross sections determine both the thermal relic density and indirect detection signals. The thermal relic density therefore constrains the rates of indirect detection signals. In the WIMPless case, however, this connection is weakened, because the thermal relic density is governed by hidden sector annihilation and gauge interactions, whereas the indirect detection signals are governed by the interactions of Equation 37.

This provides a wealth of new opportunities for indirect detection experiments looking for photons, positrons, and other annihilation products. As an example, WIMPless dark matter may be detected through its annihilation to neutrinos in the Sun by experiments such as Super-Kamiokande. Although such rates depend on the competing cross sections for capture and annihilation, the Sun has almost certainly reached its equilibrium state, and the annihilation rate is determined by the scattering cross section (Desai et al. 2004). The prospects for Super-Kamiokande may
therefore be compared to direct detection rates (Desai et al. 2004; Feng et al. 2009b; Hooper et al. 2009; Kumar, Learned & Smith 2009). The results are given in Figure 18. In the near future, Super-Kamiokande and other neutrino detectors may be able to probe the low-mass regions corresponding to the DAMA and CoGeNT signals.

6.5. Particle Colliders

If hidden dark matter does not interact with SM particles, there are no collider signals. However, there may be connector particles. Because these necessarily have SM interactions, they may be produced with large cross sections at colliders, and because they necessarily have hidden charge, their decays may be nonstandard, leading to unusual signatures.

As an example, consider the connector sector interactions specified in Equation 37. In the hadronic version with $f = q$, the $Y$ particles necessarily have strong interactions, and so will be similar to fourth-generation quarks; for $f = \ell$, the $Y$ particles are similar to fourth-generation leptons. The existence of fourth-generation quarks and leptons is constrained by direct collider searches and also by precision electroweak measurements from LEP and the Stanford Linear Collider, but is far from excluded (Kribs et al. 2007). Fourth-generation quarks with masses in the range $300 \text{ GeV} \lesssim m_{Y^+} \lesssim 600 \text{ GeV}$ are consistent with all data. Strongly interacting connector particles with mass in this range are produced in large numbers at the LHC, and also...
at the Tevatron. At the same time, such connector particles are unlike standard fourth-generation quarks, which dominantly decay through charged-current modes, such as $t' \to Wb$ and $t' \to Wt$. Connector particles decay through $T' \to tX$ and $B' \to bX$, similar to squarks, except that squarks typically decay through cascades, which produce leptons. Hidden sector dark matter therefore provides new motivation for relatively simple signatures with missing energy carried away by the hidden dark matter (Alwall et al. 2010). Hidden sectors and connectors may also impact the properties of SM particles, with consequences for colliders running below the energy frontier (McKeen 2009).

Hidden sector gauge forces may also have other observable effects. For example, hidden photons may mix with SM photons through kinetic mixing terms $F_{\mu\nu} F_{h\mu\nu}$, leading to fractionally charged particles (Holdom 1986) that are subject to a wide variety of probes (Davidson, Hannestad & Raffelt 2000; Perl, Lee & Loomba 2004).

### 6.6. Astrophysical Signals

As explained in Section 6.2, an elegant way to stabilize a hidden sector dark matter candidate is through hidden charge conservation, much like the electron is stabilized by U(1) charge conservation in the SM. This requires that the dark matter have hidden charge and interact through hidden photons or other gauge bosons. More generally, hidden dark matter may interact through massive, but light, force carriers. In both cases, the hidden dark matter has significant self-interactions. Velocity-independent (“hard sphere”) self-interactions have been extensively studied, for example, in the strongly self-interacting framework of Spergel & Steinhardt (2000). Recent work on hidden dark matter has motivated new interest in velocity-dependent cross sections, namely, the classic Coulomb scattering cross section

$$\frac{d\sigma}{d\Omega} = \frac{\alpha_X^2}{m_X^2 e^2 \sin^2 \theta}$$

and its generalization to Yukawa scattering for massive gauge bosons.

Charged hidden dark matter has many astrophysical implications: (i) bound state formation and Sommerfeld-enhanced annihilation after chemical freeze out may reduce its relic density (Dent, Dutta & Scherrer 2009; Zavala, Vogelsberger & White 2009); (ii) similar effects greatly enhance dark matter annihilation in protohalos at redshifts of $z \sim 30$ (Kamionkowski & Profumo 2008); (iii) Compton scattering off hidden photons delays kinetic decoupling, suppressing small-scale structure (Feng et al. 2009a); and (iv) Rutherford scattering makes such dark matter collisional (Ackerman et al. 2009, Feng et al. 2009a).

The last possibility, of collisional dark matter, may lead to a number of observable effects. A well-known probe of dark matter self-interactions is provided by the Bullet Cluster, a rare system where a subcluster is seen to be moving through a larger cluster with relative velocity $\sim 4,500 \text{ km s}^{-1}$ (Clowe et al. 2006). Through observations in the optical and X-ray bandwidths and strong and weak gravitational lensing observations, it is clear that dark matter tracks the behavior of stars, which are collisionless, rather than the gas. These observations have allowed stringent bounds to be placed on the dark matter self-interaction strength. For velocity-independent cross sections, the Bullet Cluster observations imply $\sigma_{\text{DM}}/m_X \lesssim 3,000 \text{ GeV}^{-1}$ ($\sigma_{\text{DM}}/m_X \lesssim 0.7 \text{ cm}^{2} \text{ g}^{-1}$). These are the most direct constraints on the self-interaction of dark matter. They have been adapted to the case of velocity-dependent cross sections, leading to the bounds on dark matter mass $m_X$ and coupling strength $\alpha_X$ shown in Figure 19.

Self-interactions also allow dark matter particles to transfer energy. Self-interactions that are strong enough to create $O(1)$ changes in the velocities of dark matter particles isotropize the
velocity dispersion and create spherical halos. These expectations are borne out by simulations of self-interacting dark matter in the hard sphere limit (Spergel & Steinhardt 2000, Yoshida et al. 2000, Dave et al. 2001). The existence of elliptical dark matter halos may therefore also constrain self-interactions (Miralda-Escude 2000). The average rate for dark matter particles to change velocities by \( \mathcal{O}(1) \) factors is

\[
\Gamma_k = \int d^3v_1d^3v_2 f(v_1)f(v_2)(n_X v_{\text{rel}}\sigma_T)(v_{\text{rel}}^2/v_0^2),
\]

where \( f(v) = e^{-v^2/v_0^2}/(v_0\sqrt{\pi}) \) is the dark matter’s assumed (Maxwellian) velocity distribution, \( n_X \) is its number density, \( v_{\text{rel}} = |v_1 - v_2| \), and \( \sigma_T = \int d\Omega (d\sigma/d\Omega)(1-\cos\theta) \) is the energy transfer cross section, where \( \theta \) is the scattering angle in the center-of-mass frame. X-ray observations have established the ellipticity of the dark matter halo of the elliptical galaxy NGC 720 (Buote et al. 2002, Humphrey et al. 2006), and requiring \( \Gamma_k^{-1} > 10^{10} \) Gyr for this system also constrains self-interacting hidden dark matter, as shown in Figure 19. Note that these constraints are much stronger than those from the Bullet Cluster: for elliptical halos with dark matter velocities \( v \sim 10^{-3} \), the cross section is greatly enhanced relative to the Bullet Cluster with its larger velocities.

The possibility that dark matter is stabilized by hidden charge conservation also motivates other astrophysical signals, such as time delays of light passing through dark matter; see, e.g., Gardner (2010).

### 7. Sterile Neutrinos

The evidence for neutrino mass described in Section 2.2.3 requires new physics beyond the SM. This problem may be resolved by adding right-handed neutrinos \( \nu^R \equiv \nu^\alpha_R \), so that neutrinos may get mass through the same mechanism that generates masses for the quarks and charged leptons. For the mass terms to be allowed under the symmetries of the SM, the right-handed neutrinos must have no SM gauge interactions. One may therefore also add a gauge-invariant term to the Lagrangian involving only two right-handed neutrinos—the so-called Majorana mass term.
The SM is therefore extended to include $N$ sterile neutrinos by adding the terms

$$L_{\nu} = \bar{q}i\gamma^\mu \partial_\mu q - (\lambda_{\nu}^\mu \bar{L}_i \nu^\mu \phi + \text{h.c.}) - \frac{1}{2} M_{\alpha\beta} \bar{\nu}_\alpha \nu_\beta,$$

where $\lambda_{\nu}^\mu$ are the neutrino Yukawa couplings, $M_{\alpha\beta}$ is the Majorana mass matrix, and $\alpha, \beta = 1, \ldots, N$, where $N \geq 2$ so that at least two neutrino states are massive. When electroweak symmetry is broken, the Higgs field gets a vacuum expectation value. The neutrino mass eigenstates are then determined by diagonalizing the complete $(3 + N) \times (3 + N)$ neutrino mass matrix,

$$m_{\nu} = \begin{pmatrix} 0 & \lambda_{\nu}^\mu (\phi) \\ \lambda_{\nu}^\mu (\phi) & M_{\alpha\beta} \end{pmatrix}.$$

Mass eigenstates that are dominantly linear combinations of left-handed neutrinos are called active neutrinos, and those that are dominated by right-handed neutrino components are called sterile neutrinos.

An elegant idea for explaining the very small neutrino masses is the seesaw mechanism. In this framework, one assumes $\lambda_{\nu} \sim O(1)$ and $M \gg \langle \phi \rangle$. There are then $N$ large neutrino masses $\sim M$, and three small neutrino masses $\sim \lambda_{\nu}^2 / M$. For $M \sim 10^{14}$ GeV, near the grand unification scale, one gets the desired light neutrino masses. In this case, sterile neutrinos are beyond the range of experiments and are not dark matter candidates.

However, given the range of fermion masses illustrated in Figure 1, there is clearly a range of Yukawa couplings in the SM, and there is no strong reason to assume $\lambda_{\nu} \sim O(1)$. In general, one may, then, have light sterile neutrinos, which may be dark matter candidates. I denote this neutrino $\nu_s$, with mass $m_s$ and mixing angle $\theta$ defined by

$$\nu_s = \cos \theta \nu_R + \sin \theta \nu_L,$$

where $\nu_R (\nu_L)$ is a linear combination of right-handed (left-handed) gauge eigenstates.

### 7.1. Production Mechanisms

Sterile neutrinos may be produced in a number of ways. The relic density depends on the sterile neutrino mass and mixing angle, and all of the mechanisms require very small masses and mixing angles for sterile neutrinos to be viable dark matter candidates. These parameters are not independently motivated by other theoretical arguments, and so sterile neutrinos do not naturally have the right relic density. At the same time, sterile neutrinos with these masses and mixings may explain some observations, described in Sections 7.2 and 7.3, which may be taken as observational evidence for these parameters.

Sterile neutrinos may be produced by oscillations at temperatures $T \sim 100$ MeV (Dodelson & Widrow 1994). Sterile neutrinos were never in thermal equilibrium, but the resulting distribution is near thermal. The results of numerical studies may be approximated by

$$\Omega_{\nu_s} \approx 0.2 \frac{\sin^2 2\theta}{10^{-8}} \left[ \frac{m_s}{3 \text{ keV}} \right]^{1.8}.$$

This is shown in Figure 20 as the $L = 0$ contour. This production mechanism is always present, and the region to the right of this contour is excluded by overclosure.

The sterile neutrino relic abundance may be enhanced if the Universe has a nonzero lepton number asymmetry

$$L = \frac{n_{\nu_s} - n_{\bar{\nu}_s}}{n_\gamma}.$$
Regions of the sterile neutrino dark matter ($\sin^2 2\theta, m_s$) parameter plane. On the $L = 0$ ($L = 0.003, 0.01, 0.1$) contours (red line), sterile neutrinos produced by oscillations (resonance production) have relic densities consistent with being all of the dark matter. The gray region to the right of the $L = 0$ contour is excluded by overclosure. The regions denoted “X-ray background” and “Cluster X-ray” are excluded by null searches for X-rays from $\nu_s \rightarrow \gamma \nu_L$; the aqua shaded region is the projected reach of future X-ray searches. The orange “Fornax” and purple regions are favored to explain a core in the Fornax dwarf galaxy and pulsar kicks, respectively. The Tremaine-Gunn phase space density bound (red region) and a variety of Lyman-$\alpha$ forest constraints (yellow regions) on small-scale structure place lower bounds on $m_s$ as shown. From Abazajian & Koushiappas (2006).

For values of $L \gtrsim 10^{-3}$ that are nevertheless small enough to be well within current limits from BBN, this can allow sterile neutrinos to be all of the dark matter for smaller mixing angles and masses, as shown in Figure 20 (Shi & Fuller 1999). For further work on the relic density in both the $L = 0$ and $L > 0$ scenarios, see Aska, Laine & Shaposhnikov (2007); Laine & Shaposhnikov (2008).

Sterile neutrinos may also be produced at higher temperatures, for example, in the decay of heavy particles. One example follows from introducing a singlet Higgs boson field $S$, which couples to right-handed neutrinos through $-\frac{1}{2} \lambda S \bar{\nu}_s \nu_s$. When $S$ gets a vacuum expectation value, this term becomes a Majorana mass term. At temperatures of $T \sim m_S$, this term also produces sterile neutrinos through the decays $S \rightarrow \tilde{\nu}_L \nu_L$, and this may be a significant source of colder sterile neutrinos (Kusenko 2006, Shaposhnikov & Tkachev 2006, Petraki & Kusenko 2008).

7.2. Indirect Detection

The dominant decay of sterile neutrinos is through $\nu_s \rightarrow \nu_L \bar{\nu}_L \nu_L$. However, sterile neutrinos may also decay through a loop-level process to a photon and an active neutrino with branching ratio
\[ 27\alpha/(8\pi) \approx 1/128. \] The radiative decay width is (Pal & Wolfenstein 1982)

\[ \Gamma(v_s \to \gamma v_a) = \frac{9\alpha}{2048\pi^4} G_F^2 \sin^2 2\theta m_s^5 \approx \frac{1}{1.5 \times 10^{17} \text{s}} \sin^2 2\theta \left( \frac{m_s}{\text{keV}} \right)^5. \] (45)

For the allowed sterile neutrino parameters, the sterile neutrino’s lifetime is much longer than the age of the Universe, as required for it to be dark matter.

At the same time, even if a small fraction of sterile neutrinos decay, this may be observed. Because the radiative decay is two-body, the signal is a mono-energetic flux of X-rays with energy \( E_\gamma \approx m_s/2 \). Such signals may be seen by the XMM-Newton, Chandra X-ray, and Suzaku observatories. Null results exclude the upper right shaded region of Figure 20, and these constraints have been updated in later analyses (see, e.g., Abazajian 2009, Laine & Shaposhnikov 2008). There is also reported evidence of a signal in Chandra data, consistent with \((m_s, \sin^2 2\theta) \sim (5 \text{ keV}, 3 \times 10^{-9})\), in the heart of the allowed parameter space (Loewenstein & Kusenko 2010, Boyarsky et al. 2010). Future observations from the International X-ray Observatory may extend sensitivities to the entire range of parameters plotted in Figure 20 (Abazajian 2009).

### 7.3. Astrophysical Signals

Sterile neutrinos are the classic warm dark matter candidate. Their warmth depends on the production mechanism, however. For the three production mechanisms discussed in Section 7.1, the sterile neutrino free-streaming length is roughly

\[ \lambda_{FS} \approx R \frac{\text{keV}}{m_s}, \] (46)

where \( R = 0.9, 0.6, \) and \( 0.2 \) Mpc for production from oscillations, \( L \)-enhanced production (depending on \( L \)), and production through Higgs decay, respectively (Kusenko 2009). This implies that bounds on small-scale structure, for example, through Lyman-\( \alpha \) constraints, depend on the production mechanism. For production by oscillations, current bounds require \( m_s \gtrsim 10 \text{ keV} \), effectively excluding this production mechanism as a source for all of dark matter (see Figure 20). For colder production mechanisms, however, the Lyman-\( \alpha \) bounds on \( m_s \) are weaker, and these mechanisms may viably produce all of the dark matter. However, for much of sterile neutrino parameter space, power on small scales is reduced, providing an observable difference from vanilla cold dark matter. For further discussion of small-scale structure constraints on sterile neutrinos, see Abazajian & Kousshiappas (2006), Abazajian (2009), Boyarsky et al. (2009), and Primack (2009).

In addition to its impact on small structure and the X-ray spectrum, sterile neutrinos may have other astrophysical effects, for example, on the velocity distribution of pulsars and on the formation of the first stars. For reviews, see Boyarsky, Ruchayskiy & Shaposhnikov (2009) and Kusenko (2009).

### 8. AXIONS

Axions are motivated by the strong CP problem described in Section 2.2.4 (Peccei & Quinn 1977, Weinberg 1978, Wilczek 1978). The axion solution follows from introducing a new pseudoscalar field \( a \) with coupling

\[ \mathcal{L}_a = - \frac{g_2^2}{32\pi^2} f_a a_{\mu\nu\rho\sigma} G_{\mu\nu}^a G_{\rho\sigma}^a. \] (47)
where \( f_a \) is a new mass scale, the axion decay constant. This term makes the coefficient of \( \epsilon^{\mu\nu\rho\sigma} G_{\mu \nu}^{\alpha} G_{\rho \sigma}^{\alpha} \) dynamical. The vacuum energy depends on this coefficient, and it relaxes to a minimum where the EDM of the neutron is very small and consistent with current bounds.

The allowed parameters for axions imply that they are extremely light and weakly interacting, providing yet another qualitatively different dark matter candidate well motivated by particle physics (Abbott & Sikivie 1983; Dine & Fischler 1983; Preskill, Wise & Wilczek 1983). For a general review of axions, see, e.g., Asztalos et al. (2006).

### 8.1. Production Mechanisms

The axion’s mass and interactions are determined by \( f_a \) up to model-dependent constants that are typically \( O(1) \). The axion’s mass is

\[
m_a = \sqrt{m_u m_d \frac{f_a f_a}{m_u + m_d}} \approx 6 \mu \text{eV} \left( \frac{10^{12} \text{ GeV}}{f_a} \right),
\]

where \( m_u \simeq 4 \text{ MeV}, m_d \simeq 8 \text{ MeV}, \) and \( m_a \simeq 135 \text{ MeV} \) are the up quark, down quark, and pion masses, respectively, and \( f_a \simeq 93 \text{ MeV} \) is the pion decay constant.

Axions interact with gluons, through the term of Equation 47, and also with fermions. At loop-level, they also interact with photons through the coupling

\[
L_{a\gamma\gamma} = -g_\gamma a \frac{\alpha}{4 \pi} \vec{E} \cdot \vec{B} \equiv -g_{a\gamma\gamma} a \vec{E} \cdot \vec{B},
\]

where \( \alpha \) is the fine-structure constant and \( g_\gamma \) is a model-dependent parameter. For two well-known possibilities, the KSVZ (Kim 1979; Shifman, Vainshtein & Zakharov 1980) and DFSZ (Zhitnitsky 1980; Dine, Fischler & Srednicki 1981a) axions, \( g_\gamma \) is \(-0.97 \) and \( 0.36 \), respectively.

The axion’s mass is bounded by several independent constraints. The coupling of Equation 49 implies that axions decay with lifetime

\[
\tau(a \rightarrow \gamma\gamma) = \frac{64\pi}{g_{a\gamma\gamma}^2 m_a^2} \simeq 8.8 \times 10^{13} \text{s} \left( \frac{\text{eV}}{m_a} \right)^2.
\]

For axions to live longer than the age of the Universe, \( m_a \lesssim 20 \text{ eV} \). Other astrophysical bounds are even more stringent. In particular, axions may be produced in astrophysical bodies and then escape, leading to a new source of energy loss. Constraints from the longevity of red giants and the observed length of the neutrino pulse from Supernova 1987a, along with other astrophysical constraints, require \( f_a \gtrsim 10^8 \text{ GeV} \), implying \( m_a \lesssim 10 \text{ meV} \) (Raffelt 2008).

There are several possible production mechanisms for axion dark matter. A priori the most straightforward is thermal production, as in the case of light gravitinos and sterile neutrinos. Unfortunately, axions produced thermally would have a relic density of \( \Omega_a^0 \sim 0.22 (m_a/80 \text{ eV}) \) and be hot dark matter. In addition, Equation 50 implies that axions with mass \( \sim 80 \text{ eV} \) have lifetimes shorter than the age of the Universe, and so this mechanism cannot produce axions that are the bulk of dark matter.

There are, however, several nonthermal production mechanisms linked to the rich cosmological history of the axion field. As the Universe cools to a temperature \( T \sim f_a \), the axion field takes values that vary from place to place. This is known as the Peccei-Quinn (PQ) phase transition. Although the value of the axion field now is fixed to minimize the vacuum energy and solve the strong CP problem, at temperatures \( T \gtrsim 1 \text{ GeV} \), other effects dominate the vacuum energy, and all values of the axion field are equally possible.

If inflation occurs after the PQ phase transition, then our observable Universe lies in a patch with a single value of the axion field. At \( T \sim 1 \text{ GeV} \), the axion field then relaxes to its minimum.
This “vacuum realignment” generates a relic density (Bae, Huh & Kim 2008),

\[ \Omega_a \approx 0.4 \theta_i^2 \left( \frac{f_a}{10^{12} \text{ GeV}} \right)^{1.18}, \]  

(51)

where \( \theta_i \) is the initial vacuum misalignment angle, assuming the relic density is not diluted by late entropy production. The requirement \( \Omega_a \lesssim \Omega_{\text{DM}} \) implies \( f_a \lesssim 10^{12} \text{ GeV} \theta_i^{-2} \).

However, inflation may occur before the PQ phase transition. This has two effects. Our observable Universe then consists of a mixture of many patches with different \( \theta_i \), and the relic density from vacuum realignment is that given in Equation 51, but with an effective \( \theta_i \sim \mathcal{O}(1) \). In addition, because many different patches are observable, the boundaries between patches, topological defects such as domain walls and axionic strings generated during the PQ phase transition, may have observable effects. Production from domain wall decay is expected to be subdominant (Chang, Hagmann & Sikivie 1999) to vacuum realignment, but the relic density of axions radiated by axionic strings may be of the same order or even an order of magnitude larger (Battye & Shellard 1994; Yamaguchi, Kawasaki & Yokoyama 1999; Hagmann, Chang & Sikivie 2001).

To summarize, if inflation occurs after the PQ transition, the allowed window of axion parameter space is roughly

\[ \begin{align*}
10^{12} \text{ GeV} \theta_i^{-2} & \gtrsim f_a \gtrsim 10^{9} \text{ GeV} \\
6 \mu \text{eV} \theta_i^2 & \lesssim m_a \lesssim 6 \text{ meV},
\end{align*} \]  

(52)

where \( \theta_i \) is an arbitrary constant less than 1. If inflation occurs before, then Equation 52 applies with \( \theta_i \sim 1 \), and axion string production may imply a slightly stronger upper bound on \( f_a \).

The lower bound on \( m_a \) arises from requiring that axions do not overclose the Universe. When this bound is saturated, axions may be all of the dark matter, and so this is the preferred target region for dark matter searches. In contrast to WIMPs and superWIMPs, axions do not naturally have the correct relic density: There is a range of possible \( m_a \), and there is no reason a priori to be in the allowed window or near its lower boundary.

Note, however, that, if inflation occurred after the PQ transition, the lower bound on \( m_a \) depends sensitively on \( \theta_i \). In this case, if \( \theta_i \ll 1 \), axions may be all of the dark matter even for smaller \( m_a \) and larger \( f_a \). This latter possibility has some theoretical attractions, as it implies \( f_a \) near \( m_{\text{GUT}} \approx 10^{16} \text{ GeV} \) may be allowed and provides an avenue for anthropic selection effects to favor axion densities near the observed value (Linde 1988, Tegmark et al. 2006). However, if axions are even lighter and more weakly coupled than naively expected, they will be beyond detection for the foreseeable future.

### 8.2. Direct Detection

Axions may be detected directly by looking for their scattering with SM particles in the laboratory. Current and projected limits from direct detection axion experiments are shown in Figure 21, along with the theoretical predictions for KSVZ and DFSZ axions.

For cosmological axions, given all of the caveats discussed above, the favored region of axion parameter space, in which axions may be all of the dark matter, may be taken to be \( 1 \mu \text{eV} \lesssim m_a \lesssim 100 \mu \text{eV} \). In this region, the leading experimental results are from the Axion Dark Matter Experiment (ADMX). ADMX searches for cosmological axions by looking for the resonantly enhanced conversion of dark matter axions to photons through scattering off a background magnetic field, the Primakoff process \( ay^* \rightarrow \gamma \) (Sikivie 1983). This is a scanning experiment—one must run at a given frequency to be sensitive to axions of a given mass. Once the desired sensitivity in coupling \( g_{a\gamma\gamma} \) has been reached, one then moves to another frequency. Theoretical
9. CONCLUSIONS

Current observations support a remarkably simple model of the Universe consisting of baryons, dark matter, and dark energy, supplemented by initial conditions determined by an early epoch of inflation. If scientific progress is characterized by periods of confusion, which are resolved by neat and tidy models, which are then launched back into confusion by further data, the current era is most definitely of the neat and tidy sort.

Dark matter may be the area that launches us back into confusion with further data. The microscopic properties of dark matter are as much of a mystery now as they were in the 1930s. In the next few years, however, searches for dark matter through a variety of means discussed here may discover or exclude many of the most promising candidates.

At its core, the dark matter problem is highly interdisciplinary. Rather than attempt a summary of this review, I close with some optimistic, but plausible, scenarios for the future in which experiments from both particle physics and astrophysics are required to identify dark matter. Consider the following examples:

- Scenario 1: Direct detection experiments see a dark matter signal in spin-independent scattering. This result is confirmed by the LHC, which sees a missing energy signal that is followed up by precision measurements pointing to a 800-GeV KK gauge boson. Further LHC studies constrain the KK particle’s predicted thermal relic density to be identical at the percent level with \( \Omega_{\rm DM} \), establishing a new standard cosmology in which the dark matter is
composed entirely of KK dark matter, cosmology is standard back to 1 ns after the Big Bang, and the Universe has extra dimensions. Direct and indirect detection rates are then used to constrain halo profiles and substructure, ushering in a new era of dark matter astronomy.

- **Scenario 2**: The LHC discovers heavy, charged particles that are apparently stable. Together the LHC and International Linear Collider determine that the new particles are staus, predicted by supersymmetry. Detailed follow-up studies show that, if these staus are absolutely stable, their thermal relic density is larger than the total mass of the Universe! This paradox is resolved by further studies that show that staus decay on timescales of a month to gravitinos. Careful studies of the decays determine that the amount of gravitinos in the Universe is exactly that required to be dark matter, providing strong quantitative evidence that dark matter is entirely in the form of gravitinos, and providing empirical support for supergravity and string theory.

- **Scenario 3**: An X-ray experiment discovers a line signal. Assuming this results from decaying sterile neutrinos, the photon energy determines the neutrino’s mass \( m = 2E_{\gamma} \), the intensity determines the neutrino mixing angle \( I \propto \sin^2 \theta \), and the image morphology determines the dark matter’s spatial distribution. From the mass and radial distribution, theorists determine the free-streaming length. This favors production from Higgs decays over production by oscillations, leading to predictions of nonstandard Higgs phenomenology, which are then confirmed at the LHC. Additional information on neutrino parameters from the LHC strengthens the hypothesis of sterile neutrino dark matter, and the energy distribution of the narrow spectral line is then used to study the expansion history of the Universe and dark energy.

These scenarios are, of course, highly speculative and idealized, but they illustrate that, even in ideal scenarios that are studied and understood, close interactions between many subfields are required. At the same time, if any of the ideas discussed here is correct, there are promising prospects for the combination of detection methods in particle physics and astrophysics to identify dark matter in the not-so-distant future.

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The author is not aware of any affiliations, memberships, funding, or financial holdings that might be perceived as affecting the objectivity of this review.

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